

Analysis of semileptonic $B \rightarrow a_1(1260)\ell^- \bar{\nu}_\ell$ process within SMEFT framework

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Motivated by the prospects of the ongoing B meson experiments, we study the exclusive $B \rightarrow a_1(1260)\ell^- \bar{\nu}_\ell$ process within the Standard model effective field theory formalism. The new physics parameters are constrained by using the experimental branching fractions of the (semi)leptonic $B \rightarrow \ell \bar{\nu}$ and $B \rightarrow (\pi, \rho, \omega)\ell \bar{\nu}$ processes (where $\ell = e, \mu, \tau$) which undergoes $b \rightarrow u\ell \bar{\nu}$ quark level transitions. We then study a comprehensive angular coefficient analysis of the exclusive $B \rightarrow a_1(1260)\ell^- \bar{\nu}_\ell$ process in the Standard model and in the presence of various new physics operators.

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1. Introduction

The discrepancy between the SM prediction and the experimental measurement have been observed in various $b \rightarrow u\ell\nu$ quark level transition decays. The measurement of the branching ratio of the leptonic $B \rightarrow \tau\nu$ process, observed in Ref. [1] by Belle and BaBar collaborations [2], is not in good agreement with the SM values. An upper bound on the branching fraction of $B \rightarrow \pi\tau\nu$ was reported to be 2.5×10^{-4} by Belle collaboration[3]. Additionally, the branching ratios of the exclusive $B \rightarrow \mu\nu$ and $B \rightarrow (\pi, \rho, \omega)\mu\nu$ decays still show mild deviations from their SM results. Inspired by these differences of the measurement values from the SM expectations, we study the $B \rightarrow a_1\ell\nu$ mode in this work. The observations by BaBar and Belle collaborations [4] in the charmless hadronic $B^0 \rightarrow a_1(1260)\pi$ decay channel helps us to probe the detailed theoretical study in exclusive semileptonic $B \rightarrow a_1\ell\nu$ decay mode. In principle, the $B \rightarrow a_1\ell\nu$ decay mode can be easily access in B factory experiments in near future. In this work, our aim is to explore the consequences of a model independent effective theory formalism so called the Standard model effective field theory (SMEFT) approach on the exclusive semileptonic $B \rightarrow a_1\ell\nu$ decay mode. We mainly study the angular coefficient structure in the SM as well as in the presence of SMEFT NP operators.

2. Theoretical Framework

The SMEFT Lagrangian at dim - 6 level can be expressed as [5]:

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}}^{(4)} + \frac{1}{\Lambda^2} \sum_i C_i \mathcal{O}_i,$$

where $\mathcal{L}_{\text{SM}}^{(4)}$ is the SM Lagrangian and Λ is the NP scale. The relevant SMEFT dimension - six operators contriuting to $b \rightarrow u\ell\nu$ processes \mathcal{O}_i can be obtained by integrating out the heavy NP particles. The EFT WCs in terms of the dim - 6 SMEFT operators, the above Wilson coefficients get modified and can be expressed as follows

$$C_{V_L}^{(\ell)} = -\frac{V_{ud}}{V_{ub}} \frac{v^2}{\Lambda^2} \left[\tilde{C}_{\ell q}^{(3)} \right]_{\ell\ell 13}, \quad C_{V_R}^{(\ell)} = \frac{1}{2V_{ub}} \frac{v^2}{\Lambda^2} \left[\tilde{C}_{\phi ud} \right]_{13}, \quad (1)$$

$$C_{S_L}^{(\ell)} = -\frac{1}{2V_{ub}} \frac{v^2}{\Lambda^2} \left[\tilde{C}_{\ell equ}^{(1)} \right]_{\ell\ell 31}^*, \quad C_{S_R}^{(\ell)} = -\frac{V_{ud}}{2V_{ub}} \frac{v^2}{\Lambda^2} \left[C_{\ell edq} \right]_{\ell\ell 31}^*, \quad (2)$$

$$C_T^{(\ell)} = -\frac{1}{2V_{ub}} \frac{v^2}{\Lambda^2} \left[\tilde{C}_{\ell equ}^{(3)} \right]_{\ell\ell 31}^*. \quad (3)$$

The four dimensional differential decay distribution amplitude is given as follows

$$\begin{aligned}
 \frac{d^4\Gamma(\bar{B} \rightarrow a_1(\rightarrow \rho_{\parallel(\perp)}\pi)\ell^- \bar{\nu}_\ell)}{dq^2 d\cos\theta d\phi d\cos\theta_V} &= \mathcal{N}_{a_1}^{\parallel(\perp)} |\vec{p}_{a_1}| \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left\{ I_{1s,\parallel(\perp)}^{a_1} \sin^2\theta_V + I_{1c,\parallel(\perp)}^{a_1} (3 + \cos 2\theta_V) \right. \\
 &+ \left(I_{2s,\parallel(\perp)}^{a_1} \sin^2\theta_V + I_{2c,\parallel(\perp)}^{a_1} (3 + \cos 2\theta_V) \right) \cos 2\theta \\
 &+ I_{3,\parallel(\perp)}^{a_1} \sin^2\theta_V \sin^2\theta \cos 2\phi + I_{4,\parallel(\perp)}^{a_1} \sin 2\theta_V \sin 2\theta \cos \phi \\
 &+ I_{5,\parallel(\perp)}^{a_1} \sin 2\theta_V \sin \theta \cos \phi \\
 &+ \left(I_{6s,\parallel(\perp)}^{a_1} \sin^2\theta_V + I_{6c,\parallel(\perp)}^{a_1} (3 + \cos 2\theta_V) \right) \cos \theta \\
 &+ \left. I_{7,\parallel(\perp)}^{a_1} \sin 2\theta_V \sin \theta \sin \phi \right\}. \tag{4}
 \end{aligned}$$

The symbol \perp and \parallel refer to the transverse and longitudinal polarizations of ρ meson. The angular coefficient functions in the SM and NP can be obtained from Ref. [6].

3. Constraint on the new physics couplings

Using the data of the $B \rightarrow (\mu, \tau)\nu$, $B \rightarrow \pi(\mu, \tau)\nu$ and $B \rightarrow (\rho, \omega)(\mu, \tau)\nu$ decays, we perform a naive χ^2 analysis to constraint the NP SMEFT coefficient. We obtained the SMEFT new physics couplings where the input parameters are considered from the Ref. [1]. We study the presence of only the (vector+scalar \pm tensor) operator in this analysis. The SMEFT couplings are given below.

SMEFT couplings	Best fit (μ mode)
$[\tilde{C}_{\ell q}^{(3)}]_{\ell\ell 13}, ([\tilde{C}_{\ell q}^{(3)}]_{\ell\ell 13}, [\tilde{C}_{\ell equ}^{(1)}]_{\ell\ell 31})$	0.013, (0.016, 0.001)
$[\tilde{C}_{\ell equ}^{(3)}]_{\ell\ell 31}, ([\tilde{C}_{\ell q}^{(3)}]_{\ell\ell 13}, [\tilde{C}_{\ell edq}^{(3)}]_{\ell\ell 31})$	-0.0008, (0.015, 0.004)
$[\tilde{C}_{\ell equ}^{(1)}]_{\ell\ell 31}, ([\tilde{C}_{\ell q}^{(3)}]_{\ell\ell 13}, [\tilde{C}_{\ell equ}^{(3)}]_{\ell\ell 31})$	-0.004, (0.113, 0.003)
$[\tilde{C}_{\ell edq}^{(3)}]_{\ell\ell 31}, ([\tilde{C}_{\ell equ}^{(1)}]_{\ell\ell 31}, [\tilde{C}_{\ell equ}^{(3)}]_{\ell\ell 31})$	0.005, (-0.004, -0.001)
$([\tilde{C}_{\ell edq}^{(3)}]_{\ell\ell 31}, [\tilde{C}_{\ell equ}^{(3)}]_{\ell\ell 31})$	(0.006, -0.001)
$([\tilde{C}_{\ell equ}^{(1)}]_{\ell\ell 31}, [\tilde{C}_{\ell edq}^{(3)}]_{\ell\ell 31})$	(0.002, 0.0015)

Table 1: Best fit values of SMEFT coefficients at m_b scale, under the constraints from $b \rightarrow u\ell\nu$ modes.

4. Angular coefficients analysis: $B \rightarrow a_1(\rightarrow \rho_{\parallel}\pi)\mu\bar{\nu}$

We focus on the longitudinal analysis of $B \rightarrow a_1(1260)\ell\bar{\nu}$ process. The coefficient functions $I_{(1s,\parallel)}^{a_1}$, $I_{(2s,\parallel)}^{a_1}$, $I_{(2c,\parallel)}^{a_1}$, $I_{(3,\parallel)}^{a_1}$, $I_{(4,\parallel)}^{a_1}$, $I_{(6s,\parallel)}^{a_1}$, and $I_{(1c,\parallel)}^{a_1}$ are independent of the tensor coefficient \tilde{C}_T , providing the only the scalar and vector effects. The $I_{(6s,\parallel)}^{a_1}$ displays a significant deviation in the presence of NP couplings whereas the others lies within 1σ of the SM contribution. The effect of scalar, vector and tensor couplings on $I_{(5,\parallel)}^{a_1}$ are distinguished slightly at low q^2 region. However,

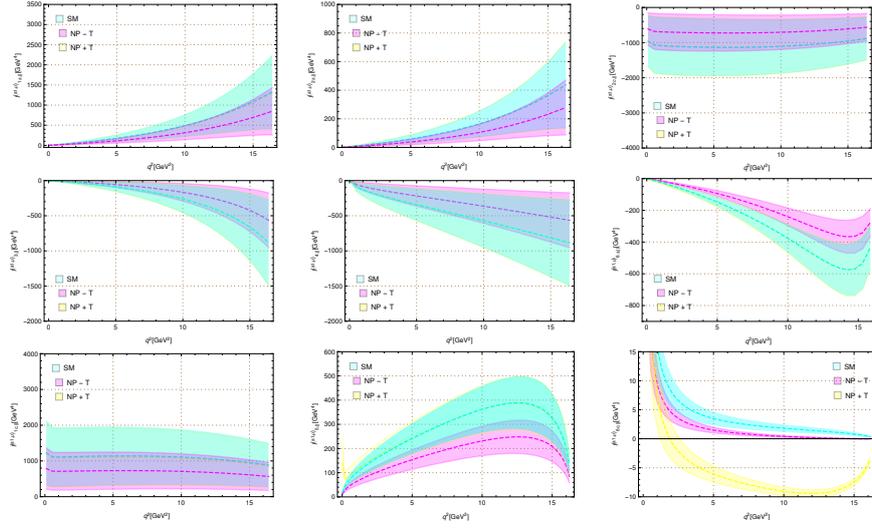


Figure 1: The q^2 dependency of the angular coefficients of $B \rightarrow a_1(\rho||\pi)\mu\bar{\nu}$ decay mode in SM (cyan), scalar+vector (magenta) [NP-T] and scalar+vector + tensor contribution (yellow) [NP+T].

the impact without tensor are clearly remarked from the SM contribution though the central value aways from the 1σ bound of SM. In bottom-right panel of Fig. 1, the variation of $I_{(6s,||)}^{a_1}$ w.r.t q^2 with tensor coefficient provides a large deviation from the SM.

5. Conclusion

The theoretical study of $B \rightarrow a_1(1260)\ell\bar{\nu}$ process requires an assessment of the accuracy of hadronic uncertainties. The $B^0 \rightarrow a_1^\pm\pi^\mp$ mode observed by BABAR and Belle Collaboration indicates to study the semileptonic decays in future.

References

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