

$b \rightarrow s\gamma$, electron EDM and electroweak baryogenesis: a study in general 2HDM

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We study inclusive $b \rightarrow s\gamma$ decay in the context of electron EDM and baryogenesis. The *general* 2HDM (i.e. without Z_2) that possesses an extra set of Yukawa matrices can drive electroweak baryogenesis via $\lambda_t \text{Im}\rho_{tt}$, where ρ_{tt} is the extra diagonal top Yukawa coupling, with the e EDM constraint evaded by an exquisite flavor cancellation mechanism. We touch upon the current status of direct search for exotic H , A and H^+ scalars at the LHC, while for the plethora of flavor observables in g 2HDM, we focus on $b \rightarrow s\gamma$, pointing out *chiral* enhancement of a $\rho_{tt}\rho_{bb}$ effect in g 2HDM, which can bring in a CPV phase. We first explore the inclusive $\mathcal{B}(b \rightarrow s\gamma)$ rate, then showcase the progress that Belle II can make in the future, illustrating a potential 3σ effect for the inclusive $B^+ \rightarrow X_s^+ \gamma$ vs $B^0 \rightarrow X_s^0 \gamma$ CPV rate difference, ΔA_{CP} . Especially if e EDM emerges swiftly, perhaps one should pursue further upgrade beyond Belle II.

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1. Introduction: tension, & $t \rightarrow ch$

A three-way tension exists in present day particle physics: to have the more testable electroweak baryogenesis (EWBG), one needs very large CP violation (CPV) beyond the Standard Model (BSM), which runs into tension with No New Physics (\mathcal{NNP}) observed so far at the LHC.

Second, be it ACME [1] or JILA [2], electron EDM at the L.E. precision frontier provide sanity checks on large BSM-CPV, with stringent bound of $|d_e| < 0.41 \times 10^{-29} e \text{ cm}$ [2]. Finally, it can be said that these ‘‘tabletop’’ experiments are competing head-on with the behemoth LHC.

But it is fair to say that EWBG ought to be pursued while LHC is still running!

We advocate [3] the *general* two Higgs doublet model ($g2HDM$); unlike the usual 2HDM with Z_2 symmetry, it has a second set of Yukawa matrices that possess flavor changing neutral couplings (FCNC). With no theorem against a second Higgs, 2HDM should be a no-brainer, but we move the well-known NFC condition of Glashow-Weinberg off its pedestal, as it is nothing but *ad hoc*.

A hallmark of $g2HDM$ would be $t \rightarrow ch$ [4], with h the observed SM-like Higgs boson. Remarkably, besides flavor-hierarchies, *Nature* seems to throw in the emergent *alignment* phenomenon (small h - H mixing, i.e. $c_\gamma \equiv \cos \gamma$ is small, with H the exotic CP -even scalar) to protect this decay, with current limit at 0.00043 [5]. The combined coupling $\rho_{tc}c_\gamma$ now barely allows ρ_{tc} at $O(1)$.

2. General 2HDM: EWBG & $eEDM$

We do not show the $g2HDM$ Higgs potential (see e.g. the brief review of Ref. [6]), but note that the convention is to take the Higgs basis where only one doublet, Φ , gives v.e.v., as without Z_2 , one cannot distinguish Φ from Φ' . A minimization condition cancels the soft $\Phi^\dagger \Phi'$ term against half the $|\Phi|^2 \Phi^\dagger \Phi'$ term, with the latter $\eta_6/2$ quartic coupling playing the unique role of Φ - Φ' mixing.

One advantage of $g2HDM$ is that $O(1)$ quartics η_i can lead to [7] 1st order phase transition (1st O PhT), one of the Sakharov conditions. It was then argued [8] that the exotic $H/A/H^\pm$ bosons would likely be sub-TeV in mass, ripe for search at the LHC. The Yukawa couplings are

$$-\frac{1}{\sqrt{2}} \sum_{f=u,d,\ell} \bar{f}_i \left[(-\lambda_i^f \delta_{ij} s_\gamma + \rho_{ij}^f c_\gamma) h + (\lambda_i^f \delta_{ij} c_\gamma + \rho_{ij}^f s_\gamma) H - i \text{sgn}(Q_f) \rho_{ij}^f A \right] R f_j - \bar{u}_i \left[(V \rho^d)_{ij} R - (\rho^{u\dagger} V)_{ij} L \right] d_j H^+ - \bar{\nu}_i \rho_{ij}^\ell R \ell_j H^+ + h.c., \quad (1)$$

with generation indices i, j summed over, $L, R = (1 \mp \gamma_5)/2$ are projections, V the CKM matrix, with the lepton matrix taken as unity. With c_γ small (with $s_\gamma \rightarrow -1$), the h couplings are close to diagonal, while extra ρ^f matrices are associated more with exotic scalars. An interesting aspect of H^\pm couplings in Eq. (1) is that, by expanding $\rho^{u\dagger} V$, one finds $H^+ \rightarrow c\bar{b}, t\bar{b}$ couplings are $\rho_{tc} V_{tb}$ and $\rho_{tt} V_{tb}$, resp., so unlike in 2HDM-II, $H^+ \rightarrow c\bar{b}$ is not CKM suppressed [9].

One highlight of $g2HDM$ is that $\lambda_t \text{Im} \rho_{tt}$ can drive EWBG robustly [10], while the leading two-loop Barr-Zee diagram for $eEDM$ can be exquisitely cancelled [11] by flavor hierarchies quite effectively: the ρ matrices *know* the SM flavor structure. In a recent paper [12, 13] we revisited this cancellation mechanism and explored the larger range of

$$\text{Re} \rho_{tt} = \text{Im} \rho_{tt} = -0.1, -0.2, -0.3, \quad (2)$$

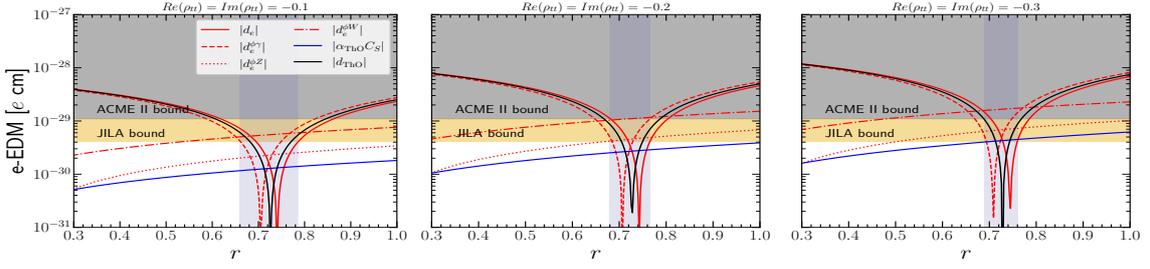


Figure 1: Cancellation of $eEDM$ [11] for $m_H, m_A, m_{H^\pm} = 500$ GeV, $c_\gamma = 0.1$, and $|\rho_{tt}| \cong 0.14, 0.28, 0.42$.

as illustrated in Fig. 1. Although the allowed range in loop function r shrinks for larger $|\rho_{tt}|$, it was stressed that especially for $|\rho_{tt}| \cong 0.42$, $eEDM$ could emerge rather swiftly. It could then be followed by $nEDM$ at PSI [14] in *just* a few years. But a “new” cancellation mechanism [12] was also illustrated for $nEDM$ itself through the unknown phase of ρ_{uu} , and the *second-whammy* from $nEDM$ could take up to even two decades to pan out, but is still quite exciting.

3. H, A, H^\pm Search & Flavor Frontiers

Sub-TeV exotic scalars should clearly be searched for at the LHC, while the *flavor* frontier is also quite promising. Here we limit ourselves to $b \rightarrow s\gamma$ for the latter, but let us first address a question: If there is a second Higgs doublet with a host of quartic and Yukawa couplings,

“Why is $g2HDM$ hiding so well?”

Exploring this question, we *guessed* [15] a “rule of thumb” for flavor control:

$$\rho_{ii} \lesssim \mathcal{O}(\lambda_i), \quad \rho_{1i} \lesssim \mathcal{O}(\lambda_1), \quad \rho_{3j} \lesssim \mathcal{O}(\lambda_3) \quad (j \neq 1), \quad (3)$$

which echoes the $eEDM$ cancellation mechanism: the ρ^f ($f = u, d, \ell$) matrices “*know*” the SM flavor structure, which roughly addresses the question we raised above.

Leading Search Modes at the LHC.— With $t \rightarrow ch$ suppressed by c_γ , it is natural to pursue $H/A/H^\pm$ direct production, gaining a $s_\gamma \rightarrow -1$ factor. The leading processes are [16]

$$cg \rightarrow tH/tA \rightarrow tt\bar{c}, tt\bar{t}, \quad (4)$$

where the second step follows from $H/A \rightarrow t\bar{c}, t\bar{t}$ decay via ρ_{tc} and ρ_{tt} couplings. Noting that $H^\pm \rightarrow c\bar{b}, t\bar{b}$ have the same V_{tb} factor and hence on equal footing, it was found that [9]

$$cg \rightarrow bH^+ \rightarrow bt\bar{b}, \quad (5)$$

may be more efficient, with production via ρ_{tc} and H^\pm decay via ρ_{tt} , bypassing the heavy associated top in Eq. (4). Both ATLAS [17] and CMS [18] have studied process (4), where the CMS study limits to $tt\bar{c}$ final state only. No signal is found so far, which might be expected, and one awaits adding Run 3 data. Process (5) apparently has not been studied yet, which we look forward to.

4. Chiral-enhanced $b \rightarrow s\gamma$ Observables

The $b \rightarrow s\gamma$ process as a probe of H^+ effects in 2HDM-I and II [19] still provides the best respective bounds on m_{H^+} . Here we are interested in the effects in $g2HDM$ [20], finding

$$\delta C_{7,8}^{(0)}(\mu) = \frac{|\rho_{tt}|^2}{3|\lambda_t|^2} F_{7,8}^{(1)}(x_t) - \frac{\rho_{tt}\rho_{bb}}{\lambda_t\lambda_b} F_{7,8}^{(2)}(x_t), \quad (6)$$

where $x_t = m_t(\mu)^2/m_{H^+}^2$ is at heavy scale μ . The $\lambda_{t,b}$ couplings in the denominators are actually *masses*, hence the second term is m_t/m_b -enhanced, as it is rooted in *chiral* H^+ couplings. Since $|\rho_{bb}| \sim 0.1$ can also drive $EWBG$, it can be probed by $b \rightarrow s\gamma$ via chiral enhancement as well.

Defining $\phi \equiv \arg \rho_{tt}\rho_{bb} = \phi_{tt} + \phi_{bb}$, we use Flavio v2.4.0 [21] to estimate $b \rightarrow s\gamma$ observables, with WCs at heavy scale $\mu \sim m_{H^+}$ evolved down to the physical scale. We consider the well-measured inclusive $\mathcal{B}(B \rightarrow X_s\gamma)$, and the inclusive CPV difference [22],

$$\Delta A_{CP}(b \rightarrow s\gamma) \equiv A_{CP}(B^+ \rightarrow X_s^+\gamma) - A_{CP}(B^0 \rightarrow X_s^0\gamma), \quad (7)$$

for the future, where the projection of Belle II physics book is used. We use HFLAV'21 for current data. Note that the error in $\mathcal{B}(B \rightarrow X_s\gamma)$ improves by less than a factor of two with full Belle II data. What's notable then is the projected order of magnitude improvement in ΔA_{CP} . Although the current sign from HFLAV'21 is insignificant, the numerics of Fig. 2 corresponds to the HFLAV'21 value in the Table below.

Observable	HFLAV'21	Belle II (5 ab^{-1})	Belle II (50 ab^{-1})
$\mathcal{B}(B \rightarrow X_s\gamma)$	$(3.49 \pm 0.19) \times 10^{-4}$	$(3.49 \pm 0.14) \times 10^{-4}$	$(3.49 \pm 0.11) \times 10^{-4}$
ΔA_{CP}	$(3.70 \pm 2.80) \times 10^{-2}$	$(0 \pm 0.98) \times 10^{-2}$	$(0 \pm 0.30) \times 10^{-2}$

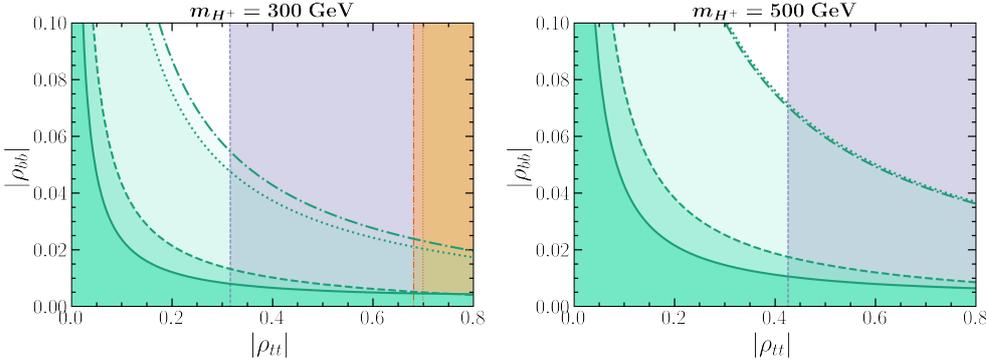


Figure 2: Results for phase $\phi = 0$ (solid), $\pm\pi/2$ (dot-dash/dots), π (dash), *allowed region* (green) from combined $b \rightarrow s\gamma$ observables, and *ruled out regions* from B_s mixing (purple) and $B_s \rightarrow \mu\mu$ (orange).

Combined $b \rightarrow s\gamma$ Observables.— The impact of current $\mathcal{B}(B \rightarrow X_s\gamma)$ is plotted in Fig. 2 at LO.¹ We see that the curves for $\phi = 0, \pi$ (and also for $\pm\pi/2$) are not so different. Of some interest is that, if $|\rho_{tt}|$ turns out rather small, it could be $\rho_{bb} \sim 0.1$ that drives $EWBG$, which is *also* probed by the chiral enhancement effect through Eq. (6), as one can see from Fig. 2 for $|\rho_{tt}| < 0.05$.

¹Things appear quite different at NLO, implying potential future work; difference for $\phi = \pm\pi/2$ is also larger at NLO.

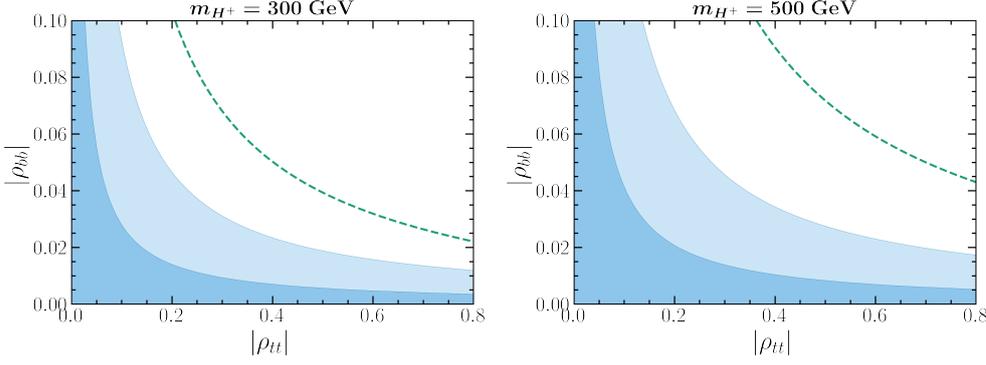


Figure 3: For $\phi = \pm\pi/2$, (light) blue shaded region allowed by null ΔA_{CP} with (5) 50 ab^{-1} Belle II data, with green dash-dot line the individual $\mathcal{B}(B \rightarrow X_s \gamma)$ lower bound. All are 1σ constraints.

ΔA_{CP} Present and Future.— More promising may be the CPV observable ΔA_{CP} , Eq. (7), the CPV difference of inclusive B^+ vs B^0 radiative decays, which we plot in Fig. 3. Only the *null* sensitivity is shown for maximal phase $\phi = \pm\pi/2$, hence we look forward to the actual measurement!

Not knowing what ΔA_{CP} values might turn up, we explore Eq. (2), the allowed $|\rho_{tt}|$ values for $eEDM$ cancellation, but set maximal phase $\phi = \pm\pi/2$ and show in Table 1. Comparing with the Table above Fig. 2, we see that for $|\rho_{tt}| \simeq 0.42$ with maximal phase $\phi = \pm\pi/2$, there could be an almost 3σ effect! Especially for the case where $eEDM$ emerges real soon, whether one has an echo from $nEDM$ or not, if a 3σ effect emerges with full Belle II data, one may face the question of “To B-III or Not to B-III?”, i.e. whether to probe CPV further in $b \rightarrow s\gamma$.

m_{H^+}	$ \rho_{tt} =x, \rho_{bb} =0.02$			$ \rho_{tt} =0.05, \rho_{bb} =0.1$
	$x = 0.1\sqrt{2}$	$x = 0.2\sqrt{2}$	$x = 0.3\sqrt{2}$	
300 GeV	$\mp(3.041 \pm 0.046)$	$\mp(6.026 \pm 0.091)$	$\mp(8.902 \pm 0.134)$	$\mp(5.352 \pm 0.080)$
500 GeV	$\mp(2.055 \pm 0.031)$	$\mp(4.097 \pm 0.063)$	$\mp(6.111 \pm 0.093)$	$\mp(3.628 \pm 0.055)$

Table 1: In units of 10^{-3} , for maximal phase $\phi = \phi_{tt} + \phi_{bb} = \pm\pi/2$.

On the other hand, if ΔA_{CP} stays consistent with zero with full Belle II data, it could be pointing at $\Delta A_{CP} \sim 0$, which may support the GUT scenario, that the phase of ρ_{bb} cancels against ρ_{tt} , as suggested by $eEDM$ cancellation mechanism, and the usual view that ℓ and d -type quarks are grouped together under GUTs.

5. Summary

Rather than accepting the “ \mathcal{NNP} ” fate, we advocate $g2HDM$ where the exotic H , A and H^+ scalars could well be $\mathcal{O}(500)$ GeV in mass, responsible for EWBG while accommodating $eEDM$ — and could be verified at the LHC, which would be *fantastic!* Thrown in as bonus would be a bunch of FPCP processes [15].

In this talk we covered only the $b \rightarrow s\gamma$ process, the well known probe of H^+ in SUSY-type 2HDM-II. We illustrate the power of $b \rightarrow s\gamma$ to probe both ρ_{tt} - and ρ_{bb} -EWBG through *chiral*

enhancement. Currently, the inclusive rate is the best measured, but we advocate that Belle II can measure ΔA_{CP} in the future to possibly provide a crosscheck on $eEDM$ and $EWBG$!

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