

## Mixing and CPV in charm decays at LHCb

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After Run 2, LHCb has collected the world's largest sample of charmed hadrons. This sample is further investigated to understand the  $CP$  violation observed in charm decays in 2019. The measurement of the time-integrated  $CP$  asymmetry in  $D^0 \rightarrow K^- K^+$  decays,  $\mathcal{A}_{CP}(K^- K^+)$ , and its combination with the observed  $\Delta A_{CP} = \mathcal{A}_{CP}(K^- K^+) - \mathcal{A}_{CP}(\pi^- \pi^+)$  are presented in this document, reporting the first evidence of  $CP$  violation in  $D^0 \rightarrow \pi^- \pi^+$ . Due to the variation of the strong phase across the Dalitz plane, multi-body decays have unique features for  $CP$  violation searches. The decays  $D_{(s)}^+ \rightarrow K^- K^+ K^+$  and  $D^0 \rightarrow \pi^- \pi^+ \pi^0$  have been also investigated with model-independent approaches, reporting no evidence for  $CP$  violation in these decay modes.

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## 1. Introduction

One of the three necessary conditions for baryon asymmetry in the Universe is the noninvariance of the fundamental interactions under the simultaneous transformation of the charge conjugation ( $C$ ) and parity ( $P$ ) operators, referred to as  $CP$  violation (CPV) [1]. In the Standard Model (SM) of particle physics, the Cabibbo-Kobayashi-Maskawa [2, 3] formalism describes  $CP$  violation through an irreducible phase in the quark-mixing matrix.  $CP$  violation in charm decays is suppressed by the SM with expected asymmetries on the order of  $10^{-3}$  or below [2–4], making room for new physics enhancements. However, predictions are hard to compute due to the low-energy strong interaction effects [5]. The direct  $CP$  asymmetry in a decay  $D \rightarrow f$  corresponds to

$$\mathcal{A}_{CP} = \frac{|A_f|^2 - |\bar{A}_{\bar{f}}|^2}{|A_f|^2 + |\bar{A}_{\bar{f}}|^2}, \quad (1)$$

where  $A_f$  ( $\bar{A}_{\bar{f}}$ ) is the amplitude connecting the initial state  $D$  ( $\bar{D}$ ) to the final state  $f$  ( $\bar{f}$ ). Most decay processes receive contributions from multiple amplitudes, *i.e.*  $A_f = \sum_j |A_j| e^{-i(\delta_j + \phi_j)}$  and  $\bar{A}_{\bar{f}} = \sum_j |A_j| e^{-i(\delta_j - \phi_j)}$ , where  $\delta_j$  and  $\phi_j$  are the strong and weak phases, respectively. Thus,  $\mathcal{A}_{CP}$  can be written as

$$\mathcal{A}_{CP} = \frac{-2 \sum_{i,j} |A_i| |A_j| \sin(\delta_i - \delta_j) \sin(\phi_i - \phi_j)}{\sum_i |A_i|^2 + \sum_{i \neq j} |A_i| |A_j| \cos(\delta_i - \delta_j) \cos(\phi_i - \phi_j)} \quad (2)$$

revealing that  $CP$  violation appears as a result of the interference among at least two processes with both different weak and strong phases. Decays with  $c \rightarrow u$  transitions are the most interesting channel, as more contributions, such as the so-called tree, penguin, or rescattering amplitudes, can appear.

The recent observation of  $CP$  violation in the charm quark sector [6] stimulates a wide discussion to understand its nature. The discovery measurement used the difference between two time-integrated  $CP$ -violating asymmetries of Cabibbo-suppressed  $D^0$  decays,  $\Delta A_{CP} = \mathcal{A}_{CP}(K^- K^+) - \mathcal{A}_{CP}(\pi^- \pi^+)$ , found to be  $\Delta A_{CP} = (-15.4 \pm 2.9) \times 10^{-4}$ . Further precise measurements may resolve the intricate theoretical debate on whether the observed value is consistent with the SM [7–11].

This document presents the measurement of the time-integrated  $CP$  asymmetry in  $D^0 \rightarrow K^- K^+$  decays. Combining the measurement with  $\Delta A_{CP}$  it is possible to quantify the amount of  $CP$  violation in the decay amplitude for  $D^0 \rightarrow \pi^- \pi^+$  decays and provide important insight in the breaking of  $U$ -spin symmetry. Furthermore, the decays  $D_{(s)}^+ \rightarrow K^- K^+ K^+$  and  $D^0 \rightarrow \pi^- \pi^+ \pi^0$  have been investigated with model independent approaches.

## 2. Direct $CP$ asymmetries in $D^0 \rightarrow K^- K^+$ and $D^0 \rightarrow \pi^- \pi^+$ decays

The measurement of  $\mathcal{A}_{CP}(K^- K^+)$  is performed using proton-proton ( $pp$ ) collision data collected with the LHCb detector during Run 2 ( $\sqrt{s} = 13$  TeV,  $5.7 \text{ fb}^{-1}$ ) [12]. Previous attempts are reported in Refs. [13, 14]. The neutral charm mesons considered are produced in the strong-interaction decays  $D^{*+} \rightarrow D^0 \pi^+$ , where the charge of the accompanying ‘‘tagging’’ pion ( $\pi_{\text{tag}}^+$ ) is used to identify the

flavour of the  $D^0$  meson at production. The measured asymmetry,  $A(K^-K^+)$ , is defined as

$$A(K^-K^+) \equiv \frac{N(D^{*+} \rightarrow D^0\pi^+) - N(D^{*-} \rightarrow \bar{D}^0\pi^-)}{N(D^{*+} \rightarrow D^0\pi^+) + N(D^{*-} \rightarrow \bar{D}^0\pi^-)}, \quad (3)$$

where  $N$  denotes the observed signal yield in the data, and the  $D^0$  meson decays into  $K^-K^+$ . This asymmetry can be approximated<sup>1</sup> as

$$A(K^-K^+) \approx \mathcal{A}_{CP}(K^-K^+) + A_P(D^{*+}) + A_D(\pi_{\text{tag}}^+), \quad (4)$$

where  $A_P(D^{*+})$  is the production asymmetry arising from the different hadronization probabilities between  $D^{*+}$  and  $D^{*-}$  mesons in  $pp$  collisions, and  $A_D(\pi_{\text{tag}}^+)$  is the instrumental asymmetry due to different reconstruction efficiencies of positive and negative pions. These nuisance asymmetries are removed exploiting Cabibbo-favoured decays, where  $CP$  violation is assumed to be negligible. Two calibration procedures, denoted as  $C_{D^+}$  and  $C_{D_s^+}$ , are used. Namely, the  $C_{D^+}$  procedure uses  $D^{*+} \rightarrow D^0(\rightarrow K^-\pi^+)\pi^+$ ,  $D^+ \rightarrow K^-\pi^+\pi^+$  and  $D^+ \rightarrow \bar{K}^0(\rightarrow \pi^-\pi^+)\pi^+$  decays; while the  $C_{D_s^+}$  procedure uses  $D^{*+} \rightarrow D^0(\rightarrow K^-\pi^+)\pi^+$ ,  $D_s^+ \rightarrow \phi(\rightarrow K^-K^+)\pi^+$  and  $D_s^+ \rightarrow \bar{K}^0(\rightarrow \pi^-\pi^+)K^+$  decays. The time-integrated  $CP$  asymmetry,  $\mathcal{A}_{CP}(K^-K^+)$ , is obtained for each of the two calibration procedures individually, by combining the measured asymmetries as follows

$$\begin{aligned} C_{D^+} : \mathcal{A}_{CP}(K^-K^+) &= A(K^-K^+) - A(K^-\pi^+) + A(K^-\pi^+\pi^+) - A(\bar{K}^0\pi^+) + A(\bar{K}^0), \\ C_{D_s^+} : \mathcal{A}_{CP}(K^-K^+) &= A(K^-K^+) - A(K^-\pi^+) + A(\phi\pi^+) - A(\bar{K}^0K^+) + A(\bar{K}^0). \end{aligned} \quad (5)$$

Given that the individual nuisance asymmetries depend on the kinematics of the corresponding particles, per-candidate weights are applied to all the data samples to equalize the kinematics of  $D^{*+}$ ,  $D^+$  and  $D_s^+$  mesons and the kaons and pions in the final state. This ensures a proper cancellation in Eq. 5.

Fits to the invariant mass distributions are used to extract the measured asymmetries in each decay mode. The signal yields, together with the statistical reduction factor<sup>2</sup> are reported in Table 1. It is possible to notice that the precision of the measurements is dominated by the modes with a  $\bar{K}^0$  in the final state, due to the low reconstruction efficiency of the neutral kaon combined with the impact of the weighting procedure.

The resulting values for  $\mathcal{A}_{CP}(K^-K^+)$  for both calibration procedures are found to be in agreement within one standard deviation. Their average is

$$\mathcal{A}_{CP}(K^-K^+) = [6.8 \pm 5.4 \text{ (stat)} \pm 1.6 \text{ (syst)}] \times 10^{-4},$$

consistent with the previous results [13, 14].

A combination of all the time-integrated  $CP$  asymmetries in  $D^0 \rightarrow K^-K^+$  measured by the LHCb collaboration to date is performed, including  $\Delta A_{CP}$  [6] and possible effects from time-dependant

<sup>1</sup>The equation is valid up to corrections of  $O(10^{-6})$  assuming individual terms of  $O(10^{-2})$  or less [12].

<sup>2</sup>The reduction factor is defined as  $(\sum_{i=1}^K w_i)^2 / (N \cdot \sum_{i=1}^K w_i^2)$ , where  $K$  is the total number of candidates and  $w_i$  includes background-subtraction and kinematic weights. These factors are for illustrative purposes only and indicate the hypothetical fraction of signal events that would provide the same statistical power as the weighted data sample.

CP violation [15]. The combination leads to

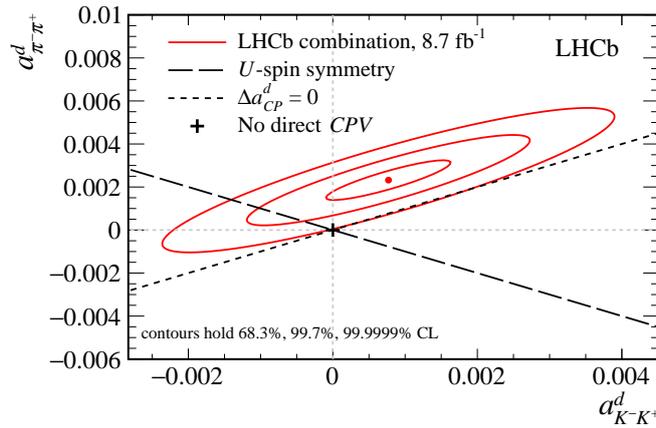
$$a_{K^-K^+}^d = (7.7 \pm 5.7) \times 10^{-4},$$

$$a_{\pi^-\pi^+}^d = (23.2 \pm 6.1) \times 10^{-4},$$

where the uncertainties include systematic and statistical contributions with a correlation coefficient of 0.88. Figure 1 shows the central values and the confidence regions in the  $(a_{K^-K^+}^d, a_{\pi^-\pi^+}^d)$  plane for this combination. The direct CP asymmetries deviate from zero by 1.4 and 3.8 standard deviations for  $D^0 \rightarrow K^-K^+$  and  $D^0 \rightarrow \pi^-\pi^+$  decays, respectively. This is the first evidence for direct CP violation in the  $D^0 \rightarrow \pi^-\pi^+$  decay.  $U$ -spin symmetry implies  $a_{K^-K^+}^d + a_{\pi^-\pi^+}^d = 0$ . A value of  $a_{K^-K^+}^d + a_{\pi^-\pi^+}^d = (30.8 \pm 11.4) \times 10^{-4}$  has been found, corresponding to a departure from  $U$ -spin symmetry of 2.7 standard deviations.

Decay mode	Signal yield [ $10^6$ ]		Red. factor	
	$C_{D^+}$	$C_{D_s^+}$	$C_{D^+}$	$C_{D_s^+}$
$D^0 \rightarrow K^-K^+$	37	37	0.72	0.76
$D^0 \rightarrow K^-\pi^+$	58	56	0.33	0.76
$D^+ \rightarrow K^-\pi^+\pi^+$	188	–	0.23	–
$D^+ \rightarrow \bar{K}^0\pi^+$	6	–	0.25	–
$D_s^+ \rightarrow \phi\pi^+$	–	43	–	0.55
$D_s^+ \rightarrow \bar{K}^0K^+$	–	5	–	0.70

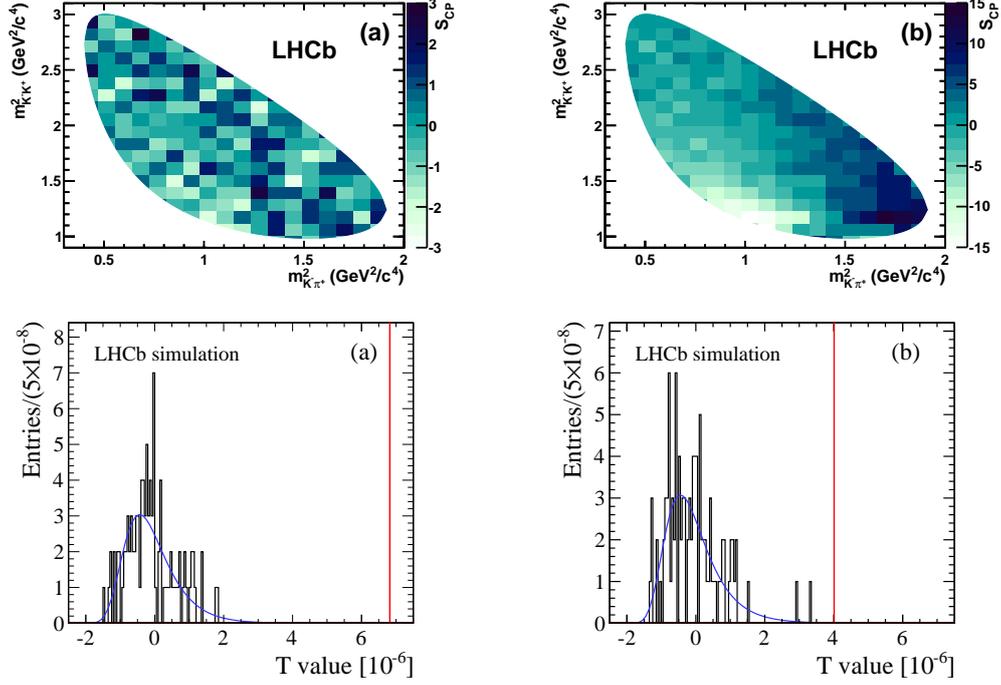
**Table 1:** Signal yields and statistical reduction factors arising from the kinematic weighting of the sample for the various decay modes and both calibration procedures.



**Figure 1:** Central values and two-dimensional confidence regions in the  $(a_{K^-K^+}^d, a_{\pi^-\pi^+}^d)$  plane for the combination. The lines  $a_{K^-K^+}^d - a_{\pi^-\pi^+}^d = 0$  for the  $\Delta A_{CP}$  observable and  $a_{K^-K^+}^d + a_{\pi^-\pi^+}^d = 0$  for the  $U$ -spin symmetry are also shown.

### 3. Search for CP violation in $D_{(s)}^+ \rightarrow K^- K^+ K^+$ and $D^0 \rightarrow \pi^- \pi^+ \pi^0$ decays

Given the dependance of  $\mathcal{A}_{CP}$  on strong phases (Eq. 2), multi-body decays are the perfect tool for search of new physics effects through the interference with the intermediate resonances. As an example, Fig. 2 (top) shows the distribution of a local CPV estimator,  $S^{CP}$ , in simulated  $D^+ \rightarrow K^- K^+ \pi^+$  data with and without the injection of a CP-violating new physics interfering with the  $\phi$  resonance. Currently, two model-independent approaches are used at LHCb. They are



**Figure 2:** (top)  $S^{CP}$  across the Dalitz plot in a Monte Carlo pseudo-experiment for  $D^+ \rightarrow K^- K^+ \pi^+$  decays with (left) no CPV and (right) a  $4^\circ$  CPV in the  $\phi\pi$  phase. Note the difference in colour scale between (left) and (right). Reproduced from Ref. [16]. (bottom) Distribution of permutation  $T$  values for the simulated sample for  $D^0 \rightarrow \pi^- \pi^+ \pi^0$  decays and showing the nominal  $T$  value as a vertical line for (left) 2% CP violation in the amplitude and (right)  $1^\circ$  phase CP violation of the  $\rho^+$  resonance. Reproduced from Ref. [17].

the so-called ‘‘Miranda method’’ and the ‘‘Energy test’’ being a binned and unbinned approach, respectively. These strategies are not able to measure a CP-violating observable as  $\mathcal{A}_{CP}$  but they will report a  $p$ -value related to the probability of the observed data being consistent with the CP-symmetry conservation hypothesis.

The Miranda method consists in dividing the phase-space in different sub-regions and calculating  $S_{CP}^i$  in each bin  $i$  (as described in Fig. 2 (top)). The local CPV estimator can be defined as

$$S_{CP}^i = \frac{N^i(D) - \alpha N^i(\bar{D})}{\sqrt{\alpha(\delta_{N^i(D)}^2) + \delta_{N^i(\bar{D})}^2}} \quad \text{with } \alpha = \frac{\sum_i^{N_{bins}} N^i(D)}{\sum_i^{N_{bins}} N^i(\bar{D})} \quad (6)$$

where  $N^i(D)$  and  $N^i(\bar{D})$  are the yields for the  $D \rightarrow f$  and  $\bar{D} \rightarrow \bar{f}$  decays candidates for each bin  $i$  and  $N_{bins}$  is the number of sub-regions. The  $p$ -value of the observed data is calculated considering

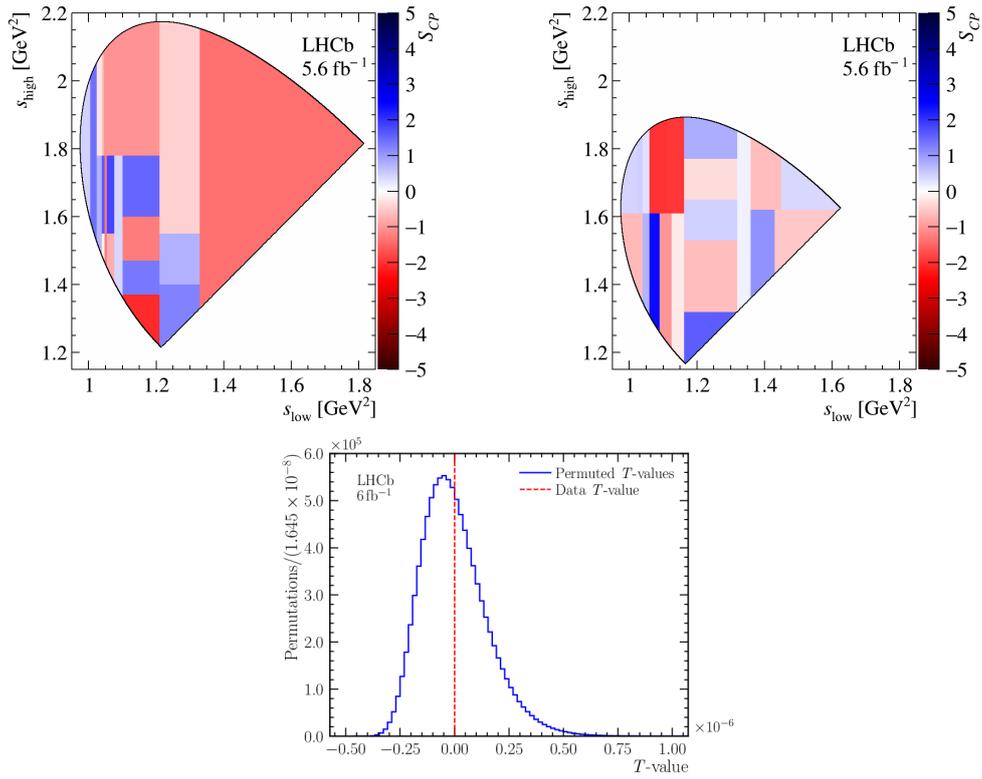
the  $\chi^2$  of  $\mathcal{S}_{CP}$ , *i.e.*  $\chi^2 = \sum_i^{N_{bins}} \mathcal{S}_{CP}^i$ , with a number of degrees of freedom corresponding to  $N_{bins} - 1$ .

The Energy test method relies on the test statistic  $T$  being sensitive to both local and global asymmetries, as shown in Fig. 2 (bottom). The  $p$ -value is obtained by comparing the  $T$  value observed in data to the distribution of  $T$ , obtained from permutation samples, where the flavour is randomly assigned. The test statistic is defined as

$$T = \sum_{i,j>i}^n \frac{\psi_{ij}}{n(n-1)} + \sum_{i,j>i}^{\bar{n}} \frac{\psi_{ij}}{\bar{n}(\bar{n}-1)} - \sum_{i,j}^{\frac{n,\bar{n}}{n\bar{n}}} \frac{\psi_{ij}}{n\bar{n}}, \quad (7)$$

representing the difference among the average difference of events with the same flavour and the one among events with opposite flavour. In particular,  $n$  and  $\bar{n}$  are the yields for the  $D \rightarrow f$  and  $\bar{D} \rightarrow \bar{f}$  decays candidates. The distance among a pair of events  $ij$  in the phase-space is defined as  $d_{ij} = |(m_{12}^{2,j} - m_{12}^{2,i}, m_{23}^{2,j} - m_{23}^{2,i}, m_{13}^{2,j} - m_{13}^{2,i})|$ , where  $m_{lk}^{2,i}$  represents the squared invariant mass of two of the three particles in the final state for each candidate  $i$ . The metric function is defined as  $\psi_{ij} = e^{-d_{ij}^2/2\sigma^2}$  where  $\sigma$  is related to the sensitivity of the test and its value is optimized with simulated samples.

The two presented approaches have been used in the latest searches for CPV, investigating  $D_{(s)}^+ \rightarrow K^- K^+ K^+$  and  $D^0 \rightarrow \pi^- \pi^+ \pi^0$  decays, using respectively the Miranda method and the Energy test [18, 19]. These analysis are performed using proton-proton ( $pp$ ) collision data collected with the LHCb detector during Run 2 ( $\sqrt{s} = 13$  TeV,  $5.7 \text{ fb}^{-1}$ ). While a search was already carried out in  $D^0 \rightarrow \pi^- \pi^+ \pi^0$  decays with Run 1 data [17], the  $D_{(s)}^+ \rightarrow K^- K^+ K^+$  decays are investigated for the first time. In both the analysis, the model-independent approaches are also applied to Cabibbo-favoured decays with similar kinematic distributions, *i.e.*  $D_s^+ \rightarrow K^- K^+ \pi^+$  and  $D^0 \rightarrow K^- \pi^+ \pi^0$  decays, as a cross-check. In the analysis for  $D_{(s)}^+ \rightarrow K^- K^+ K^+$  decays the phase-space is divided in 21 physically-motivated bins to increase the sensitivity of  $\mathcal{S}_{CP}$ . The observed yields are about  $0.97 \cdot 10^6$  and  $1.27 \cdot 10^6$  candidates for the  $D_s^+$  and the  $D^+$  decays, respectively.  $\mathcal{S}_{CP}^i$  is measured in each bin and represented in Fig. 3 (top). The  $p$ -values results to be 13.3% and 31.6% for  $D_s^+$  and  $D^+$  decays, respectively, stating no evidence for CP violation in these decays. In the Energy test with  $D^0 \rightarrow \pi^- \pi^+ \pi^0$  decays the best value for  $\sigma$  has been found to be  $0.2 \text{ (GeV}/c^2)^2$  thanks to simulated data. The final result is shown in Fig. 3 (bottom), reporting a  $p$ -value = 62% and thus no evidence for CP violation in this decay.



**Figure 3:** (top)  $S_{CP}$  values across the Dalitz plot for (left)  $D_s^+ \rightarrow K^- K^+ K^+$  and (right)  $D^+ \rightarrow K^- K^+ K^+$  signal candidates using 21 bins [18]. (bottom) Distribution of  $T$ -values obtained by running the energy test over the final signal  $D^0 \rightarrow \pi^- \pi^+ \pi^0$  sample (red dashed line) superimposed on the corresponding distribution for the  $CP$ -symmetry hypothesis, obtained from flavour-randomised permutations of the same data sample [19].

## References

- [1] A. D. Sakharov, *Violation of CP Invariance, C asymmetry, and baryon asymmetry of the universe*, *Pisma Zh. Eksp. Teor. Fiz.* **5** (1967) 32.
- [2] N. Cabibbo, *Unitary symmetry and leptonic decays*, *Phys. Rev. Lett.* **10** (1963) 531.
- [3] M. Kobayashi and T. Maskawa, *CP-violation in the renormalizable theory of weak interaction*, *Prog. Theor. Phys.* **49** (1973) 652.
- [4] S. L. Glashow, J. Iliopoulos and L. Maiani, *Weak Interactions with Lepton-Hadron Symmetry*, *Phys. Rev. D* **2** (1970) 1285.
- [5] M. Golden and B. Grinstein, *Enhanced CP Violations in Hadronic Charm Decays*, *Phys. Lett. B* **222** (1989) 501.
- [6] LHCb COLLABORATION collaboration, *Observation of CP violation in charm decays*, *Phys. Rev. Lett.* **122** (2019) 211803 LHCb-PAPER-2019-006 CERN-EP-2019-042, [[1903.08726](#)].
- [7] H.-Y. Cheng and C.-W. Chiang, *Revisiting CP violation in  $D \rightarrow PP$  and  $VP$  decays*, *Phys. Rev. D* **100** (2019) 093002 [[1909.03063](#)].
- [8] A. Dery and Y. Nir, *Implications of the LHCb discovery of CP violation in charm decays*, *JHEP* **12** (2019) 104 [[1909.11242](#)].
- [9] R. Bause, H. Gisbert, M. Golz and G. Hiller, *Exploiting CP-asymmetries in rare charm decays*, *Phys. Rev. D* **101** (2020) 115006 [[2004.01206](#)].
- [10] H.-Y. Cheng and C.-W. Chiang, *CP violation in quasi-two-body  $D \rightarrow VP$  decays and three-body  $D$  decays mediated by vector resonances*, *Phys. Rev. D* **104** (2021) 073003 [[2104.13548](#)].
- [11] I. Bediaga, T. Frederico and P. Magalhaes, *Enhanced charm CP asymmetries from final state interactions*, [2203.04056](#).
- [12] LHCb COLLABORATION collaboration, *Measurement of the time-integrated CP asymmetry in  $D^0 \rightarrow K^- K^+$  decays, submitted to PRL* (2022) LHCb-PAPER-2022-024, CERN-EP-2022-163, [[2209.03179](#)].
- [13] LHCb COLLABORATION collaboration, *Measurement of CP asymmetry in  $D^0 \rightarrow K^- K^+$  decays*, *Phys. Lett. B* **767** (2017) 177 LHCb-PAPER-2016-035 CERN-EP-2016-259, [[1610.09476](#)].
- [14] LHCb COLLABORATION collaboration, *Measurement of CP asymmetry in  $D^0 \rightarrow K^- K^+$  and  $D^0 \rightarrow \pi^- \pi^+$  decays*, *JHEP* **07** (2014) 041 CERN-PH-EP-2014-082 LHCb-PAPER-2014-013, [[1405.2797](#)].
- [15] LHCb COLLABORATION collaboration, *Search for time-dependent CP violation in  $D^0 \rightarrow K^+ K^-$  and  $D^0 \rightarrow \pi^+ \pi^-$  decays*, *Phys. Rev. D* **104** (2021) 072010 LHCb-PAPER-2020-045, CERN-EP-2021-060, [[2105.09889](#)].

- [16] LHCb COLLABORATION collaboration, *Search for CP violation in  $D^+ \rightarrow K^- K^+ \pi^+$  decays*, *Phys. Rev.* **D84** (2011) 112008 LHCb-PAPER-2011-017 CERN-PH-EP-2011-163, [[1110.3970](#)].
- [17] LHCb COLLABORATION collaboration, *Search for CP violation in  $D^0 \rightarrow \pi^- \pi^+ \pi^0$  decays with the energy test*, *Phys. Lett.* **B740** (2015) 158 CERN-PH-EP-2014-251 LHCb-PAPER-2014-054, [[1410.4170](#)].
- [18] LHCb COLLABORATION collaboration, *Search for CP violation in  $D_{(s)}^+ \rightarrow K^- K^+ K^+$* , *JHEP* **07** (2023) 067 LHCb-PAPER-2022-042, [[2303.04062](#)].
- [19] LHCb COLLABORATION collaboration, *Search for CP violation in  $D^0 \rightarrow \pi^- \pi^+ \pi^0$* , LHCb-PAPER-2023-005.