

## Data-driven Estimation of Invisible Energy below EeV

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The calorimetric energy of a cosmic-ray shower is measured by optical telescopes from the emission of isotropic fluorescence light or from the collimated Cherenkov light through the number of charged secondary particles. To reconstruct the energy of the primary cosmic ray the calorimetric energy needs to be further corrected for the energy that is not deposited in the atmosphere. This invisible energy is a substantial source of systematic uncertainties in the energy spectrum of cosmic rays measured by optical telescopes below 1 EeV. Usually, estimations of the invisible energy below 1 EeV relied on Monte Carlo simulations despite the fact that models of hadronic interactions have problems in describing the measured air-shower data. We apply a data-driven method to derive the invisible energy for air showers using the publicly available data of the KASCADE and IceTop experiments. The universal relation between the invisible energy and the number of muons measured by the detectors was utilized. In this way, we determine the invisible energy from measured data between PeV and EeV energies and compare with invisible-energy models adopted at the Pierre Auger and Telescope Array observatories.

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## 1. Introduction

VHECR (Very-high energy cosmic rays) are charged particles in the energy range  $10^{15-18}$  eV. When the VHECR energy is measured using fluorescence telescopes [1–4], the measured calorimetric energy must be corrected for the energy that is not deposited in the atmosphere. This so-called invisible energy is carried by muons and neutrinos, and is a substantial source of systematic uncertainties in the energy spectrum measured by optical telescopes below 1 EeV (in case of Telescope Array experiment  $\sim 10\%$  [3], in case of Auger experiment  $\sim 8\%$  [4]).

The invisible energy of VHECR can be estimated from simulations for a given mass composition of VHECR despite the fact that hadronic interaction (HI) models have problems to describe the measured air-shower data and, therefore, the mass composition of VHECR is burdened by high systematic uncertainties. The problems to describe air-shower data of VHECR (especially the muon component of shower) were found [5] in KASCADE-Grande data for HI models tuned to the LHC data [5]. The inconsistency of description of measured muons using MC simulations is higher at ultra-high energies (above 1 EeV) [6–8], suggesting also a deeper predicted scale of the depth of shower maximum [9].

At the ultra-high energies, a data-driven method was applied to the hybrid data of fluorescence and ground detectors of the Pierre Auger Observatory above  $10^{18.6}$  eV and extrapolated down to  $10^{17}$  eV [10], where also a phenomenological description of the data-driven method can be found. The invisible energy was found to be even larger than the MC simulations predict for iron nuclei.

In this work, we apply a data-driven method to derive the invisible energy from the publicly available VHECR data of the KASCADE and IceTop experiments [11, 12]. The universal relation between the invisible energy and the number of muons measured by the shielded KASCADE detectors was derived and adopted. We also use IceTop data to estimate the energy evolution of invisible energy. In this way, we determine the invisible energy from measured data between PeV and EeV energies and compare with models of invisible energy adopted by Telescope Array [3] and Pierre Auger Observatory [4].

## 2. KASCADE Data and Simulations

The KASCADE experiment [13] measured VHECR since 1996 and finished its measurement in 2003. The detected showers were reconstructed using signals in shielded (signals dominantly from muons above 230 MeV) and unshielded scintillation detectors (signals from charged particles). The collected data of this experiment were recently released together with simulations at the reconstruction level including the detector effects [11] accessible from [14].

Both simulated and measured data contain information on the reconstructed number of muons on ground with energy threshold 230 MeV ( $N_{\mu}^{\text{Rec}}$ ), the zenith angle ( $\Theta_{\text{Rec}}$ ), the lateral shape parameter ( $s^{\text{Rec}}$ ), and the shower energy ( $E_{\text{Rec}}$ ). The KASCADE simulations contain additionally to the reconstructed quantities also the true information on the number of muons above 100 MeV ( $N_{\mu}^{\text{MC}}$ ), the number of electrons ( $N_{\text{el}}^{\text{Rec}}$ ), the true zenith angle ( $\Theta^{\text{MC}}$ ), primary energy ( $E_{\text{MC}}$ ) and the type of primary particle initiating the generated shower. However these KASCADE simulations do not include information on the calorimetric or invisible energy. Therefore, we produced an additional library of showers simulated in program CORSIKA [15] with the same settings as the

publicly available KASCADE simulations to obtain the information on the invisible energy ( $E_{\text{Inv}}$ ) and to finally relate it with the number of generated muons.

## 2.1 KASCADE Data

We used NABOO 2.0 version [11] of released data for runs 4685-7417 containing 252,658,250 reconstructed showers from period 08.05.1998 – 20.12.2003 with zenith angle  $\Theta_{\text{Rec}} = 0^\circ\text{-}60^\circ$ , azimuth angle  $0^\circ\text{-}360^\circ$ , lateral shape parameter  $s^{\text{Rec}} = 0.1\text{-}1.48$ , core positions in the square of size 91 m centred in the middle of the KASCADE experiment with  $\log_{10} N_{\text{el}}^{\text{Rec}}$  and  $\log_{10} N_{\mu}^{\text{Rec}}$  both higher than 2. This pre-selection of data guarantees a constant quality of the measured data.

To the preselected data set, we applied cuts on the reconstructed numbers of particles  $\log_{10} N_{\text{el}}^{\text{CUT}} = 4.4$  and  $\log_{10} N_{\mu}^{\text{CUT}} = 4.0$ . We applied also additional cuts recommended by the KASCADE group to maintain high quality of the reconstructed data [16]:  $s_{\text{low}}^{\text{CUT}} = 0.6$ ,  $s_{\text{high}}^{\text{CUT}} = 1.3$  to cut finally showers with  $\log_{10} N_{\text{el}}^{\text{Rec}} < \log_{10} N_{\text{el}}^{\text{CUT}}$ ,  $\log_{10} N_{\mu}^{\text{Rec}} < \log_{10} N_{\mu}^{\text{CUT}}$ , and  $s^{\text{Rec}} < s_{\text{low}}^{\text{CUT}}$  and  $s^{\text{Rec}} > s_{\text{high}}^{\text{CUT}}$ .

For our analysis, we use only showers with  $\Theta_{\text{Rec}} \leq 25^\circ$  since the formula for estimation of the shower energy using  $\log_{10} N_{\text{el}}^{\text{Rec}}$  and  $\log_{10} N_{\mu}^{\text{Rec}}$  was derived for  $\Theta^{\text{MC}} \leq 25^\circ$  [11]. Finally, 16,302,464 measured showers were used to calculate the invisible energy from the measured number of muons.

## 2.2 KASCADE Simulations

The publicly available simulations are described in [17]. The energy of primary particles followed an energy spectrum with spectral index  $\gamma_{\text{MC}} = 2$  from  $10^{14}$  eV to  $10^{18}$  eV; with high-energy extension to  $3.16 \cdot 10^{18}$  eV. For the purpose of our analysis, we reweighted the simulated showers to correspond to the energy spectrum of measured data with spectral index 2.7. In our analysis, we use showers simulated with EPOS-LHC [18], QGSJet II-04 [19] and Sibyll 2.3 [20] to estimate reconstruction biases on  $N_{\mu}^{\text{Rec}}$  and  $E_{\text{Rec}}$  for p, He, C and Fe primaries. The energy cut-off for electrons, photons and neutral pions was set to 3 MeV and for muons and hadrons to 100 MeV.

The same cuts as the cuts applied to the set of measured data were applied to these simulations. We checked that these cuts keep full reconstruction efficiency of all primary particles above the shower energy  $10^{15.3}$  eV.

Finally, we have obtained about 30,000 selected showers of 500,000 showers at disposal for given model of hadronic interactions and primary particle within  $\Theta_{\text{MC}} = 25^\circ$ .

### 2.2.1 Unfolding Number of muons and Shower Energy

We derived from the KASCADE simulations the parametrization of the average bias on the reconstructed number of muons and on the reconstructed energy for showers with  $\Theta_{\text{MC}} \leq 25^\circ$ .

The average relative bias on the number of muons above 100 MeV,  $\eta_{\mu} = (N_{\mu}^{\text{Rec}} - N_{\mu}^{\text{MC}}) / N_{\mu}^{\text{MC}}$ , was parameterized for each primary particle and each model of hadronic interactions with a polynomial of the 4<sup>th</sup> order as a function of the reconstructed energy for each of the 4 zenith-angle ranges dividing the zenith-angle range  $0^\circ\text{-}25^\circ$  equidistantly in  $\cos^2(\Theta_{\text{MC}})$ .

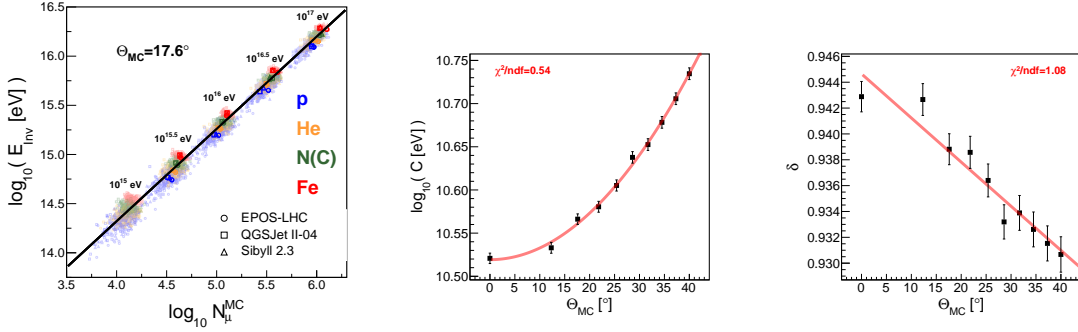
In case of the parameterization of the average relative bias depending on the reconstructed energy,  $\eta_E = (E_{\text{Rec}} - E_{\text{MC}}) / E_{\text{MC}}$ , a polynomial of the 3<sup>rd</sup> order was used for  $E_{\text{Rec}} \geq 10^{15.3}$  eV. The dependence of polynomial coefficients on  $\cos^2(\Theta_{\text{MC}})$  for  $\eta_{\mu}(E_{\text{Rec}})$  and  $\eta_E(E_{\text{Rec}})$  was assumed to be cubic.

For given HI model, the reconstructed quantities were corrected for the average bias on event-by-event basis for a mass composition with primary fractions  $f_i$ ,  $\sum_i f_i = 1$  for  $i = \text{p, He, C, Fe}$  as  $N_\mu = N_\mu^{\text{Rec}} / \sum_i (f_i \cdot \eta_\mu(E_{\text{Rec}}))$ , and  $E_{\text{Tot}} = E_{\text{Rec}} / \sum_i (f_i \cdot \eta_E(E_{\text{Rec}}))$  according to the Global Spline Fit (GSF) model [21] for primary fractions of p, He, CNO group and Fe group, respectively. The maximal values of the mean residuals after the application of the bias corrections for individual primaries and given HI model are a substantial source of systematic uncertainty in the final results (see Section 2.5).

### 2.3 Additional CORSIKA Simulations

We produced 60,000 showers using CORSIKA 7.6400 for three HI models, EPOS-LHC, QGSJet II-04 and Sibyll 2.3, and low-energy model FLUKA 2011.2x for 4 primary particles: p, He, N and Fe. Ten fixed values of the zenith angle were distributed uniformly in  $\cos^2 \Theta_{\text{MC}}$  ( $\Theta_{\text{MC}}=0^\circ$ ,  $12.3^\circ$ ,  $17.6^\circ$ ,  $21.8^\circ$ ,  $25.4^\circ$ ,  $28.6^\circ$ ,  $31.7^\circ$ ,  $34.5^\circ$ ,  $37.3^\circ$  and  $40^\circ$ ) for each of 5 fixed primary energies ( $E_{\text{MC}}=10^{15}$  eV,  $3.2 \cdot 10^{15}$  eV,  $10^{16}$  eV,  $3.2 \cdot 10^{16.5}$  eV and  $10^{17}$  eV). For each HI model, primary particle, energy and zenith angle, 100 showers were generated.

The calorimetric energy ( $E_{\text{Cal}}$ ) was calculated for each simulated shower as the sum of energy deposited by charged particles at each depth of shower until the ground level. A correction for a part of the calorimetric energy below the ground was accounted for. The invisible energy was then obtained as  $E_{\text{Inv}} = E_{\text{MC}} - E_{\text{Cal}}$ . The number of muons ( $N_\mu^{\text{MC}}$ ) was obtained as a sum of all muons (above 100 MeV) reaching the ground level as in the case of  $N_\mu^{\text{MC}}$  in KASCADE simulations. The difference of  $\langle N_\mu^{\text{MC}} \rangle$  between KASCADE simulations and additional CORSIKA simulations was found to be within 0.5%.



**Figure 1:** Left: Relation between the invisible energy ( $E_{\text{Inv}}$ ) and the number of muons above 100 MeV ( $N_\mu^{\text{MC}}$ ). The individual showers of additional CORSIKA simulations generated for 5 fixed energies and the zenith angle  $\Theta_{\text{MC}} = 17.6^\circ$  were used for the fit (black line). Middle and right: Dependence of fitted parameters  $C$  (middle) and  $\delta$  (right) on the zenith angle. These dependencies were assumed (red curves) to be quadratic and linear, respectively.

### 2.4 Data-driven Method

The additional CORSIKA simulations were used to calibrate  $E_{\text{Inv}}$  with  $N_\mu^{\text{MC}}$  for each of ten fixed zenith angles (see an example on the left panel of Fig. 1 according to  $E_{\text{Inv}} = C \cdot (N_\mu^{\text{MC}})^\delta$ ). The general dependencies for showers of all three HI models, all four primaries and all five energy

bins were fitted with the least square method. The obtained parameters  $C$  and  $\delta$  are depicted on the middle and right panel of Fig. 1, respectively, for different  $\Theta_{MC}$ . The zenith angle dependencies of parameters  $C$  and  $\delta$  were fitted with quadratic and linear functions, respectively, using the least square method. These dependencies come mainly from the attenuation of  $N_{\mu}^{MC}$ . The difference of  $E_{Inv}$  between  $\Theta_{MC}=0^{\circ}$  and  $\Theta_{MC}=25^{\circ}$  was found to be within  $\sim 2\%$ .

In the following, the relation between  $E_{Inv}$  and  $N_{\mu}^{MC}$  was considered universal with respect to the HI model and the mass composition of primary particles. The maximal residuals of fitted  $E_{Inv}$  ( $\Delta E_{Inv}/E_{Inv}$ ) contribute significantly to the total systematic uncertainty of the results (see Section 2.5 and the right panel of Fig. 2 for more details).

For showers of ultra-high energies detected by hybrid detectors of the Pierre Auger Observatory [10],  $E_{Cal}$  was measured directly by fluorescence telescopes with very low systematic uncertainties at the level of 14%.  $E_{Inv}$  was measured independently using ground detectors and then related to the  $E_{Cal}$  for the same showers. An estimate of the  $E_{Inv}$  applicable to the optical measurements was provided in the form of  $E_{Inv}/E_{Tot} = E_{Inv}/E_{Tot}(\log_{10}(E_{Cal} [eV]))$ .

In case of the KASCADE experiment, the shower energy ( $E_{Rec}$ ) is estimated from the measured number of muons and electrons on ground [11]. It is based on the comparison with signals of showers generated by given energy for HI model QGSJet II-02 and Fluka 2002\_4. Such energy calibration is substantially biased wrt. the mass composition and HI models (up to 50-10% for energies  $10^{15.5-18.0}$  eV). Therefore, we present our results for a combination of the 4 primaries (p, He, C and Fe) developing with the shower energy according to the GSF for primary fractions of p, He, CNO group and Fe group, respectively. We applied a rescaling of the energy scale in GSF by 0.88 to account for the energy rescaling applied in [21] for KASCADE-Grande that we consider to have the same energy scale as the KASCADE experiment (energy calibrations using the same MC simulations).

For each shower reconstructed with zenith angle  $\Theta_{Rec}$ ,  $N_{\mu}^{Rec}$  and  $E_{Rec}$ , the unfolded number of muons on ground ( $N_{\mu}^{Unf}$ ) and the unfolded shower energy ( $E_{Tot}$ ) are obtained for primary fractions predicted by the GSF model at the energy  $E_{Rec}/0.88$ . The invisible energy,  $E_{Inv}$  ( $N_{\mu}^{Unf}$ ), is calculated for  $C(\Theta_{Rec})$  and  $\delta(\Theta_{Rec})$  for the corresponding zenith angle. We derive  $E_{Cal}$  as  $E_{Cal} = E_{Tot} - E_{Inv}$ .

## 2.5 Systematic Uncertainties

We consider several sources of systematic uncertainty in our method contributing to the total systematic uncertainty at a level of 20% of  $E_{Inv}/E_{Tot}$  (see the right panel of Fig. 2). The individual contributions to the systematic uncertainties of  $E_{Inv}$  and  $E_{Tot}$  were summed in quadrature and propagated to the total systematic uncertainty of  $E_{Inv}/E_{Tot}$ .

The main contribution to the systematic uncertainty of  $E_{Inv}$  comes from the quasi-universal calibration (left panel of Fig. 1) of  $E_{Inv}$  with  $N_{\mu}^{MC}$ . The residual dependence ( $\Delta E_{Inv}/E_{Inv}$ ) on HI model and mass composition decreases from  $\sim \pm 20\%$  at  $10^{15.5}$  eV to  $\sim \pm 15\%$  at  $10^{17}$  eV mainly due to decreasing shower-to-shower fluctuations with increasing energy of showers. The decreasing trend of this uncertainty was extrapolated beyond the energy  $10^{17}$  eV where a reasonable amount of data is present, but not of simulations to be confirmed.

The systematic uncertainty of  $E_{Inv}$  stemming from the imperfection of the parameterization of the  $N_{\mu}$  bias  $\eta_{\mu}$  was estimated to increase from  $\Delta E_{Inv}/E_{Inv} \sim \pm 2\%$  to  $\sim \pm 4\%$ . The systematic

uncertainty of  $E_{\text{Tot}}$  due to the bias correction  $\eta_E$  increases from  $\Delta E_{\text{Tot}}/E_{\text{Tot}} \sim \pm 4\%$  at  $10^{15.5}$  eV to  $\sim \pm 15\%$  and  $10^{17.5}$  eV. The increase of these uncertainties with energy is a consequence of the decrease of statistics in KASCADE simulations and therefore from the reduced reliability of the bias descriptions.

The relative difference in  $N_\mu^{\text{MC}}$  between KASCADE simulations and the additional CORSIKA simulations was found to be around 0.5%. Such a difference is expected to come from different versions of CORSIKA and FLUKA. The remaining relative differences for individual primaries were found to be at a level of 5% (stemming predominantly from low statistics of simulations), which is a value included conservatively as the systematic uncertainty of  $E_{\text{Inv}}$  ( $E_{\text{Inv}} \propto N_\mu^{\text{MC}}$ ).

The systematic uncertainty stemming from the mass composition adopting the GSF model was estimated as the largest change of the results when the proton and helium primary fractions were increased/decreased by 10%, and nitrogen and iron fractions were decreased/increased by 10% to obtain the lightest and the heaviest composition, respectively, from the four components adopting the uncertainty of primary fractions of 10%. The uncertainties of the mass composition derived with the GSF method were estimated to influence our results by few % as a result of different relative weights of the bias corrections for each of the four primaries.

### 3. IceTop Data

The invisible energy can also be estimated indirectly from the measurement of muon densities. This method is based on the relation  $E_{\text{Inv}} = \epsilon_\pi^{\text{C}} \times N_\mu$  which comes from the Heitler–Matthews' model and was validated using detailed MC simulations [10].  $N_\mu$  is the number of muons in the extensive air shower reaching ground level, and  $\epsilon_\pi^{\text{C}}$  is the pion critical energy. If the corresponding MC simulations of the detector response are also available, the invisible energy can be obtained using [4]

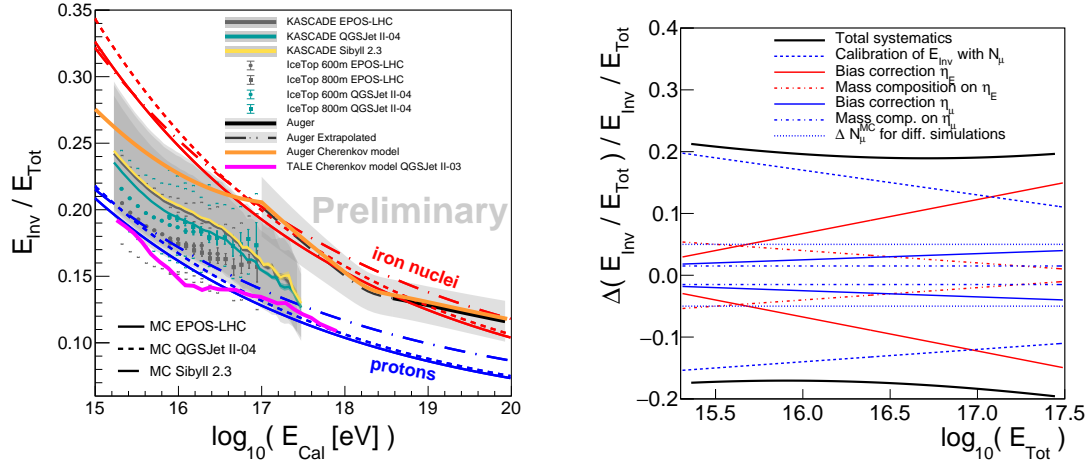
$$E_{\text{Inv}} = E_{\text{Inv,p}} \left( \frac{E_{\text{Inv,Fe}}}{E_{\text{Inv,p}}} \right)^z, \quad z = \frac{\ln(N_\mu^{\text{det}}) - \ln(N_{\mu,p}^{\text{det}})}{\ln(N_{\mu,Fe}^{\text{det}}) - \ln(N_{\mu,p}^{\text{det}})},$$

where  $E_{\text{inv,p}}$  and  $E_{\text{inv,Fe}}$  are the invisible energies estimated by the chosen high–energy interaction model, here QGSJet II-04 and EPOS-LHC, for protons and iron nuclei, respectively. The quantity  $z$  can be estimated e.g. from the IceTop data [12] for two different shower-core distances (600m and 800m) as was done in [22].

### 4. Comparison of Results with Invisible-energy Models

On the left panel of Fig. 2, the mean fractions of the invisible energy to the shower energy from KASCADE (curves) and IceTop (markers) data are plotted for various HI models as a function of the logarithm of the calorimetric energy. For comparison, we plot the MC predictions for protons (blue) and iron nuclei (red) obtained with CONEX 6.40 [23, 24] simulations for zenith angles within  $25^\circ$  and energies between  $10^{15}$  eV and  $10^{20}$  eV. The Auger measurement (black solid line) and its extrapolation (black dashed-and-dotted curve) are depicted as well. This extrapolation down to  $10^{17}$  eV assumed the mass evolution according to the Auger measurements and no evolution of the muon discrepancy between data and simulations with energy. Finally, we plot the invisible-energy models adopted at the Pierre Auger (orange curves) and Telescope Array (purple curve)

observatories. The energy spectrum measured by TALE optical telescopes between  $\sim 2$  PeV and  $\sim 2$  EeV [3] used prediction for energy evolution of the mass composition that matched the observed data on the depth of shower maximum, so called TXF composition model. Such comparison relies on the absolute scale of depth of shower maximum for given HI model, which is a subject of large systematic uncertainties (see e.g. [9]). Although not specified by TALE, we estimated the TXF composition for the TALE model in Fig. 2 from the quoted results in [25] using QGSJet II-03.



**Figure 2:** Left: Ratio of the invisible energy to the total shower energy as a function of the logarithm of calorimetric energy derived from KASCADE (systematics in gray bands) and IceTop data (systematics in squared brackets) at two different shower-core distances. The Auger measurements and extrapolation are shown by black lines [10]. The models adopted at the Pierre Auger [4] and Telescope Array [3] observatories is depicted by cyan and purple lines, respectively. Right: Individual contributions to the total systematic uncertainty of the ratio of the invisible energy to the total shower energy for KASCADE data.

In the range of  $\log_{10}(E_{\text{Cal}} [\text{eV}]) = 17.0 - 17.4$ , the measurement using KASCADE data is below the extrapolation of Auger measurements, although still within the quoted systematic uncertainties (gray bands). This difference might be a consequence of an energy evolution of the discrepancy between data and simulations, by different energy scales adopted by the experiments, or by other source of systematics. Applying energy rescaling from the GSF model to compare Auger extrapolation with KASCADE and IceTop data and the same energy scale, we have not found a significant improvement of the discrepancy.

In general, our results using publicly available data of IceTop and KASCADE experiments suggest somewhat better accordance with the invisible-energy model below EeV energy adopted at the Pierre Auger Observatory. The ultimate goal of this study is to provide new model of the energy evolution of invisible energy fraction that could be easily rescaled by any experiment to its energy scale.

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