

W-boson angular coefficients at LHC at high precision

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We present state-of-the-art high-precision theory predictions for the dominant angular coefficients parametrizing the spin-correlations in the production and decay of a W-boson produced at transverse momentum larger than 30 GeV. The computation at NNLO QCD and NLO EW accuracy are combined to obtain differential distributions in the W-boson transverse momentum and rapidity. The found results show up to 10 % corrections in certain regions of phase space, while the scale bands are significantly reduced as compared to NLO QCD.

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1. Introduction

The W-boson mass is one of the fundamental parameters of the Standard Model, which, through its connection to the other electroweak parameters and thus to the electroweak symmetry breaking, is an important key to detecting beyond Standard Model physics. One such process from which the mass can be measured is the W-boson production at non-zero transverse momentum (W+jet process). The mass parameter is however not measured directly, due to the inherent difficulty of measuring the neutrino, but rather through template fits from theory predictions.

In order to reduce both the theoretical and experimental systematic uncertainties, prior to the W-boson mass template fits, a theory-data comparison is made to the similar Z+jet process [1]. Eventual discrepancies between theory and data in the Z+jet process is then translated to the W+jet process. In order to do this efficiently, and to reduce statistical fluctuations in the theory computations, the five-dimensional phase space of the V+jet process can be translated into a three-dimensional one, together with eight angular coefficient functions, describing the decay of the vector boson. Despite the similarities, the two processes are still not the same: different parton luminosities contribute, the scales are different, and the EW corrections differ. As illustration, we show the comparison of the A_4 coefficient, differentially in the vector boson p_T at NLO QCD and at NLO EW¹ precision in Fig. 1. It is thus necessary to predict both of the processes and the corresponding angular coefficients with the current state-of-the-art accuracy. The Z+jet process has been presented at NNLO QCD [2] and NLO EW [3]. In the current work, we present a combination of NNLO QCD and NLO EW corrections to the W-boson related process [4] for the 13 TeV LHC.

2. Theory and computational setup

The differential cross section in terms of the eight angular coefficients is

$$\begin{aligned} \frac{d\sigma}{dp_{T,W} dy_W dm_{\ell\nu} d\Omega} = & \frac{3}{16\pi} \frac{d\sigma^{U+L}}{dp_{T,W} dy_W dm_{\ell\nu}} \left((1 + \cos^2 \theta) + A_0 \frac{1}{2} (1 - 3 \cos^2 \theta) \right. \\ & + A_1 \sin 2\theta \cos \phi + A_2 \frac{1}{2} \sin^2 \theta \cos 2\phi + A_3 \sin \theta \cos \phi + A_4 \cos \theta \\ & \left. + A_5 \sin^2 \theta \sin 2\phi + A_6 \sin 2\theta \sin \phi + A_7 \sin \theta \sin \phi \right), \end{aligned} \quad (1)$$

in which the (charged) lepton angles θ, ϕ are suitably evaluated in the Collins-Soper frame [5], and σ^{U+L} refers to the unpolarized normalizing cross section.

This work considers a combination of higher-order corrections, separately at NNLO QCD ($\mathcal{O}(\alpha_s^3 \alpha^2)$), computed using the STRIPPER framework [6–9] within the narrow-width approximation² and NLO EW ($\mathcal{O}(\alpha_s \alpha^3)$), using MADGRAPH5_AMC@NLO [10, 11]. The mixed QCD+EW correction at the combined order however is ambiguously defined, as the angular coefficients are defined as ratios of observables,

$$A_j^{\text{def}} = \frac{\sigma_{\text{num}}}{\sigma_{\text{den}}}. \quad (2)$$

¹For the EW K-factor, the LO results are computed with a one-loop ρ -parameter for a fair comparison to the NLO EW results.

²The off-shell effects at NLO QCD have been cross-checked to be negligible.

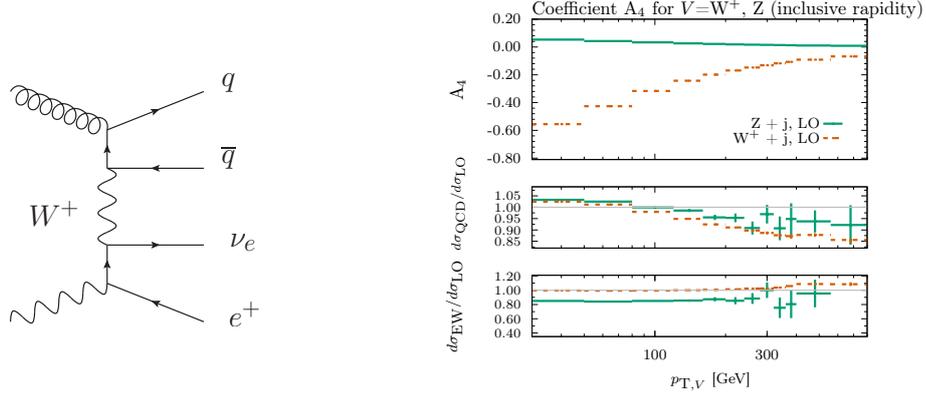


Figure 1: Left: Exemplary Feynman diagram of photon-induced contributions featuring double-soft singularities at the current perturbative order. **Right:** The A_4 coefficient for the Z -jet process and W^+ +jet (upper panel), the corresponding NLO QCD K -factors (middle panel) and the NLO EW K -factors (lower panel).

In this work, we compare both an unexpanded ratio (denoted as *def*) and an expanded ratio in the strong coupling constant (denoted as *exp*),

$$A_j^{\text{exp}} = A + \alpha_s B + \alpha_s^2 C. \quad (3)$$

The electroweak corrections are then included as K -factors at the level of the coefficients,

$$A_{j,\text{QCD+EW}}^{\text{def/exp}} = K_{\text{EW}} \times A_j^{\text{def/exp}} \quad (4)$$

in order to remedy a soft divergence present in the calculations at this order³, portrayed in the left of Fig. 1.

In the electroweak sector, the complex- G_μ and the complex-mass-scheme used, and final-state photons are recombined with the charged leptons. As the central scales, we choose the transverse energy of the W -boson and as customary perform a 7-point variation on the numerator and denominator, and a 31-point variation on the ratio.

3. Results

We show the A_0 and A_3 coefficients, inclusive in the W -boson rapidity, in Fig. 2 for W^- production⁴. The factor ~ 2 decrease in the scale uncertainty at NNLO QCD as compared to the NLO QCD result is visible for both of these (and all the other) coefficients. In the lower panels, we make a comparison between the expanded and unexpanded versions of the coefficients, where we note that while the central values show negligible difference, the scale bands are a factor ~ 2 smaller for the expanded versions.

Regarding the rapidity-dependence of the coefficients, in Fig. 3 are shown the A_4 coefficient in two rapidity bins. Similarly, A_1 and A_3 are found to have significant rapidity-dependence, while the A_0 and A_2 coefficients remain rapidity-independent.

³The double-soft IR singularity is not canceled at the separate $O(\alpha_s \alpha^3)$ order, as this requires mixed QCD+EW loop diagrams to be included.

⁴The corresponding results for the plus signature behave similarly for all coefficients except the parity-odd A_3 and A_4 , in which cases the distributions change sign.

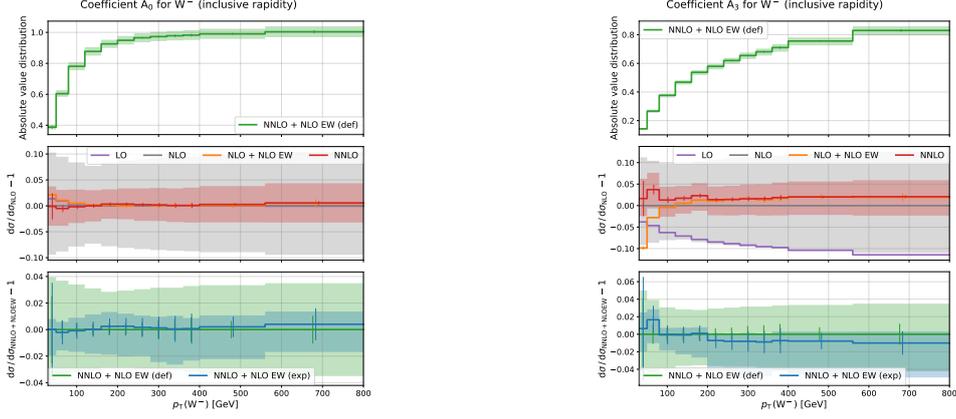


Figure 2: The A_0 (left) and A_3 (right) coefficients, inclusive in the W-boson rapidity.

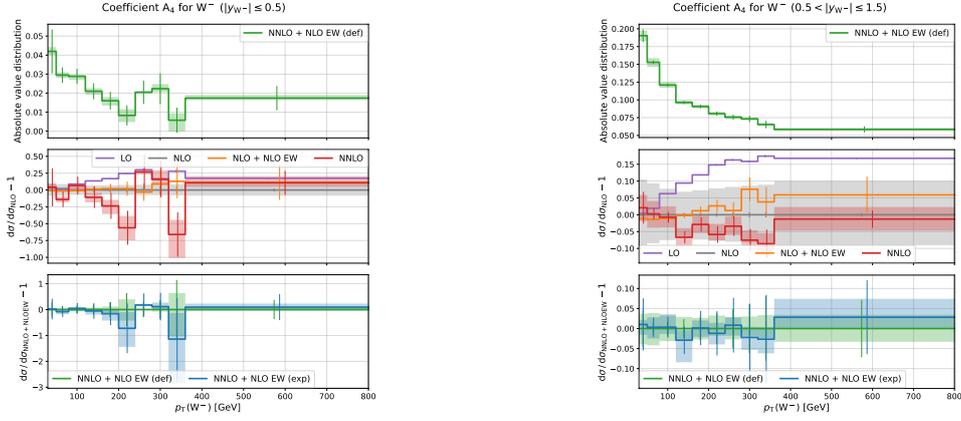


Figure 3: The A_4 coefficient in the central-rapidity region (left) and in the mid-rapidity region (right).

The decomposition into angular coefficients as in Eq. (1) is strictly only valid when the boson decay is a 2-body decay, which is broken when electroweak corrections are considered. This effect was examined in the work by performing a reweighted event generation for LO events, reweighted with NLO EW accurate coefficients. We found this non-completeness electroweak effect to be negligible.

4. Conclusion

We found moderate corrections at NNLO QCD and NLO EW for the angular coefficients, while the scale uncertainties were found to significantly decrease. This motivates well these high-precision predictions to be the starting point for an experimental determination of these coefficients, and alongside it, a more accurate W-boson mass measurement.

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