

## Study of Branching fraction and CP asymmetry of charm mesons at Belle

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*CP* violation in charm meson decays is expected to be small within the Standard Model (SM) framework, and an observation of a large *CP* asymmetry could indicate new physics. We report measurement of branching fractions and direct *CP* asymmetries  $A_{CP}$  in  $D^0 \rightarrow \pi^+\pi^-\eta$ ,  $K^+K^-\eta$ ,  $\phi\eta$  and  $D^0 \rightarrow K_S^0 K_S^0 \pi^+\pi^-$  decays. For the latter the T-odd asymmetry  $a_{CP}^T$  sensitive to *CP* violation in the decay, is also measured. This report also covers the search for *CP* violation in  $D \rightarrow Kh\pi^0$  ( $h = \pi, K$ ) decays. The results are based on the full data collected with the Belle detector at the KEKB asymmetric-energy  $e^+e^-$  collider.

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## 1. Introduction

Equal amounts of matter and antimatter existed in the early Universe [1]. For such an initial state to evolve into our current matter-dominated universe [2, 3] violation of  $CP$  (charge-conjugation and parity) symmetry [4] is required. The amount of  $CP$  violation ( $CPV$ ) present in the Standard Model (SM) fails to account for the observed imbalance between matter and antimatter [3, 5]. Thus, it is important to search for new sources of  $CPV$ . In the SM framework,  $CPV$  is expected to be very small ( $O(10^{-3})$  or smaller) in the charm meson decays [6]. Any significant deviation from SM expectation will probe new physics effects beyond the SM. Singly Cabibbo suppressed (SCS) decays are expected to be especially sensitive to physics beyond the SM, as their amplitudes receive contributions from QCD “penguin” operators and also chromomagnetic dipole operators [6]. The SCS decays  $D^0 \rightarrow K^+ K^-$  and  $D^0 \rightarrow \pi^+ \pi^-$  [7] are the only decay modes in which  $CPV$  has been observed in the charm sector. The  $CP$  asymmetry measured,

$$A_{CP} \equiv \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow \bar{f})}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow \bar{f})}, \quad (1)$$

is small, at the level of 0.1%.

All the results reported in this document are obtained using full data collected by Belle detector running at KEKB asymmetric-energy  $e^+e^-$  collider operating at and near  $\Upsilon(4S)$  mass peak. Belle experiment [8] ran a successful physics program with very good performance on particle identification, momentum resolution and vertexing. The Belle experiment collected a total of  $1 \text{ ab}^{-1}$  of data, which includes  $1.3 \times 10^9$   $c\bar{c}$  events. In this proceeding, we report the recent charm results from the Belle experiment including; a) Measurement of the branching fraction ( $\mathcal{B}$ ) and search for  $CPV$  in the SCS decay  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$  [9]; b) the measurement of branching fraction and search for  $CPV$  in  $D^0 \rightarrow \pi^+ \pi^- \eta$ ,  $D^0 \rightarrow K^+ K^- \eta$ ,  $D^0 \rightarrow \phi \eta$  [10]; and c) the measurement of branching fractions for  $D \rightarrow Kh\pi\pi^0$  ( $h = \pi, K$ ) decays [11].

## 2. Measurement of the branching fraction and search for $CPV$ in the SCS decay

$$D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$$

In  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$  analysis, we search for  $CPV$  in two complementary ways. We first measure the asymmetry  $A_{CP}$ ; a nonzero value may result from interference between contributing decay amplitudes. The  $CP$ -violating interference term is proportional to  $\sin(\phi) \sin(\delta)$  [12–14] where  $\phi$  and  $\delta$  are the weak and strong phase differences, respectively, between the amplitudes. Thus, to observe  $A_{CP} \neq 0$ ,  $\delta$  must be nonzero. To avoid the need for  $\delta \neq 0$ , we also search for  $CPV$  by measuring the asymmetry in the triple-product  $C_T = \vec{p}_{K_S^0} \cdot (\vec{p}_{\pi^+} \times \vec{p}_{\pi^-})$ , where  $\vec{p}_{K_S^0}$ ,  $\vec{p}_{\pi^+}$ , and  $\vec{p}_{\pi^-}$  are the three-momenta of the  $K_S^0$ ,  $\pi^+$ , and  $\pi^-$  daughters, respectively, and defined in the  $D^0$  rest frame. From the two  $K_S^0$  in final state we choose the  $K_S^0$  with the higher momentum for this calculation. The asymmetry is defined as

$$A_T \equiv \frac{N(C_T > 0) - N(C_T < 0)}{N(C_T > 0) + N(C_T < 0)}, \quad (2)$$

where  $N(C_T > 0)$  and  $N(C_T < 0)$  correspond to the yields of  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$  decays having  $C_T > 0$  and  $C_T < 0$ , respectively. For  $\bar{D}^0$  decays, we define the CP conjugate quantity

$$\bar{A}_T \equiv \frac{\bar{N}(-\bar{C}_T > 0) - \bar{N}(-\bar{C}_T < 0)}{\bar{N}(-\bar{C}_T > 0) + \bar{N}(-\bar{C}_T < 0)}. \quad (3)$$

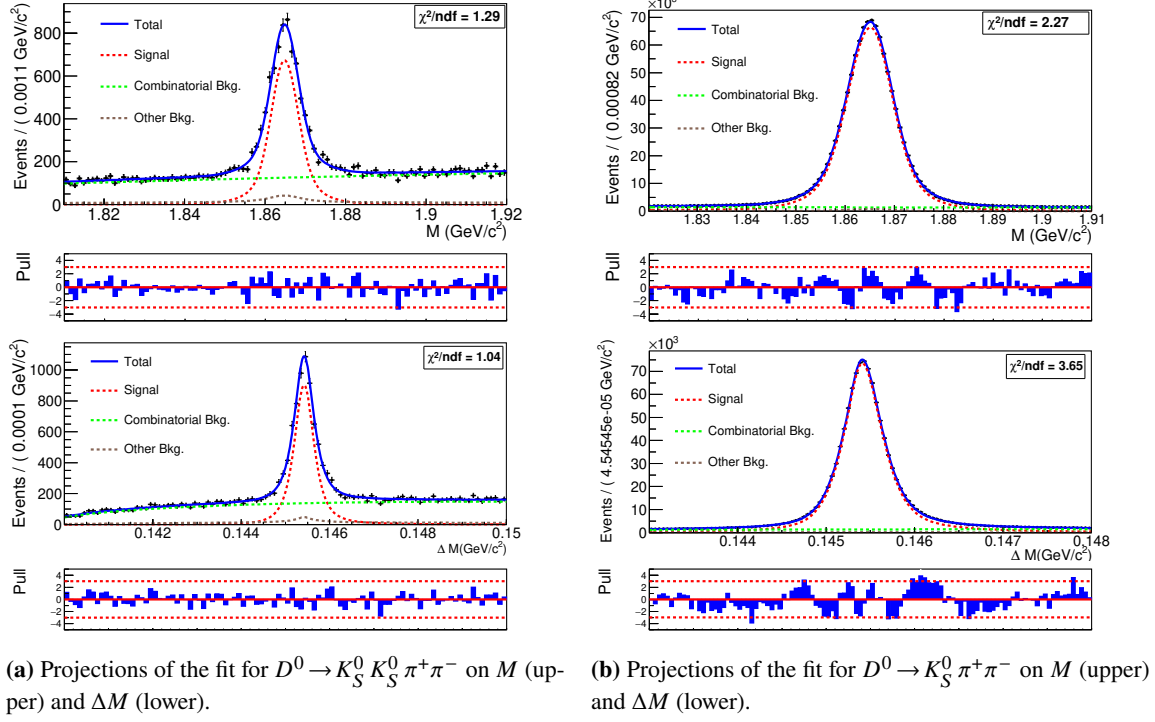
The difference is a CP violating observable

$$a_{CP}^T \equiv \frac{A_T - \bar{A}_T}{2} \quad (4)$$

proportional to  $\sin(\phi) \cos(\delta)$ , and, unlike  $A_{CP}$ ,  $\delta = 0$  results in the largest CP asymmetry. The observable  $a_{CP}^T$  is also advantageous to measure experimentally, as any production- or detection-related asymmetry cancels out.

To measure the branching fraction and search for CP violation, we use  $922 \text{ fb}^{-1}$  of Belle data. We reconstruct the decay chain  $D^{*+} \rightarrow D^0 \pi_s^+$ ,  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$  where the charge of slow pion ( $\pi_s$ ) is used to tag the flavor of D meson. We measure the branching fraction relative to Cabibbo favored  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$  decays observed in the same data set. For  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$ , we determine the signal yield via a two-dimensional unbinned extended maximum-likelihood fit to the variables  $M$  and  $\Delta M \equiv M(K_S^0 K_S^0 \pi^+ \pi^- \pi_s^+) - M$ . The fitted ranges are  $1.810 \text{ GeV}/c^2 < M < 1.920 \text{ GeV}/c^2$  and  $0.140 \text{ GeV}/c^2 < \Delta M < 0.150 \text{ GeV}/c^2$ . The fit yields  $6095 \pm 98$  signal events. Projections of the fit are shown in Fig. (1a). We determine  $N_{K_S^0 \pi^+ \pi^-}$  from a two-dimensional binned fit (rather than unbinned, as the statistics are large) to the  $M$  and  $\Delta M$  distributions. The fitted ranges are  $1.820 \text{ GeV}/c^2 < M < 1.910 \text{ GeV}/c^2$  and  $0.143 \text{ GeV}/c^2 < \Delta M < 0.148 \text{ GeV}/c^2$  [15]. The fit yields  $1\,069\,870 \pm 1831$   $D^0 \rightarrow K_S^0 \pi^+ \pi^-$  decays. Projections of the fit are shown in Fig. (1b).

We measure the CP asymmetry  $A_{CP}$  from the difference in signal yields for  $D^0$  and  $\bar{D}^0$  decays  $A_{CP}^{\text{det}} = \frac{N(D^0 \rightarrow f) - N(\bar{D}^0 \rightarrow \bar{f})}{N(D^0 \rightarrow f) + N(\bar{D}^0 \rightarrow \bar{f})}$ . The observable  $A_{CP}^{\text{det}}$  includes asymmetries in production and reconstruction,  $A_{CP}^{\text{det}} = A_{CP} + A_{\text{FB}} + A_{\epsilon}^{\pi_s}$  where  $A_{\text{FB}}$  is the ‘‘forward-backward’’ production asymmetry [16] between  $D^{*+}$  and  $D^{*-}$  due to  $\gamma^* - Z^0$  interference in  $e^+ e^- \rightarrow c \bar{c}$ ; and  $A_{\epsilon}^{\pi_s}$  is the asymmetry in reconstruction efficiencies for  $\pi_s^\pm$  tracks. We correct for  $A_{\epsilon}^{\pi_s}$  in  $K_S^0 K_S^0 \pi^+ \pi^-$  events by separately weighting  $D^0$  and  $\bar{D}^0$  decays. After correcting for  $A_{\epsilon}^{\pi_s}$ , we obtain  $A_{CP}^{\text{cor}} = A_{CP} + A_{\text{FB}}$ . The asymmetry  $A_{\text{FB}}$  is an odd function of  $\cos \theta^*$ , and  $A_{CP}$  is constant, where  $\theta^*$  is the polar angle between the  $D^{*\pm}$  momentum and the  $+z$  axis in the CM frame. We thus extract  $A_{CP}$  and  $A_{\text{FB}}$  via  $A_{CP} = \frac{A_{CP}^{\text{cor}}(\cos \theta^*) + A_{CP}^{\text{cor}}(-\cos \theta^*)}{2}$ ,  $A_{\text{FB}} = \frac{A_{CP}^{\text{cor}}(\cos \theta^*) - A_{CP}^{\text{cor}}(-\cos \theta^*)}{2}$ . We calculate  $A_{CP}^{\text{cor}}$  in four bins of  $\cos \theta^*$ :  $(-1.0, -0.4)$ ,  $(-0.4, 0)$ ,  $(0, 0.4)$  and  $(0.4, 1.0)$ . We determine  $A_{CP}^{\text{cor}}$  for each bin by simultaneously fitting for  $D^0$  and  $\bar{D}^0$  signal yields for weighted events in that bin. The results for  $A_{CP}^{\text{cor}}$  are combined to obtain  $A_{CP}$  and  $A_{\text{FB}}$ . Fitting the  $A_{CP}$  values in bins of  $\cos \theta^*$  to a constant, we obtain  $A_{CP} = [-2.51 \pm 1.44 \text{ (stat)}_{-0.52}^{+0.35} \text{ (syst)}] \%$ , where the first uncertainty is statistical and second is systematic [9]. To measure  $a_{CP}^T$ , we divide the data into four subsamples:  $D^0$  decays with  $C_T > 0$  (yield= $N_1$ ) and  $C_T < 0$  (yield= $N_2$ ); and  $\bar{D}^0$  decays with  $-\bar{C}_T > 0$  ( $N_3$ ) and  $-\bar{C}_T < 0$  ( $N_4$ ). Thus,  $A_T = (N_1 - N_2)/(N_1 + N_2)$ ,  $\bar{A}_T = (N_3 - N_4)/(N_3 + N_4)$ , and  $a_{CP}^T = (A_T - \bar{A}_T)/2$ . We fit the four subsamples simultaneously and take the fitted parameters to be  $N_1$ ,  $N_3$ ,  $A_T$ , and  $a_{CP}^T$ . The fit gives  $a_{CP}^T = [-1.95 \pm 1.42 \text{ (stat)}_{-0.12}^{+0.14} \text{ (syst)}] \%$ , where the first uncertainty is statistical and



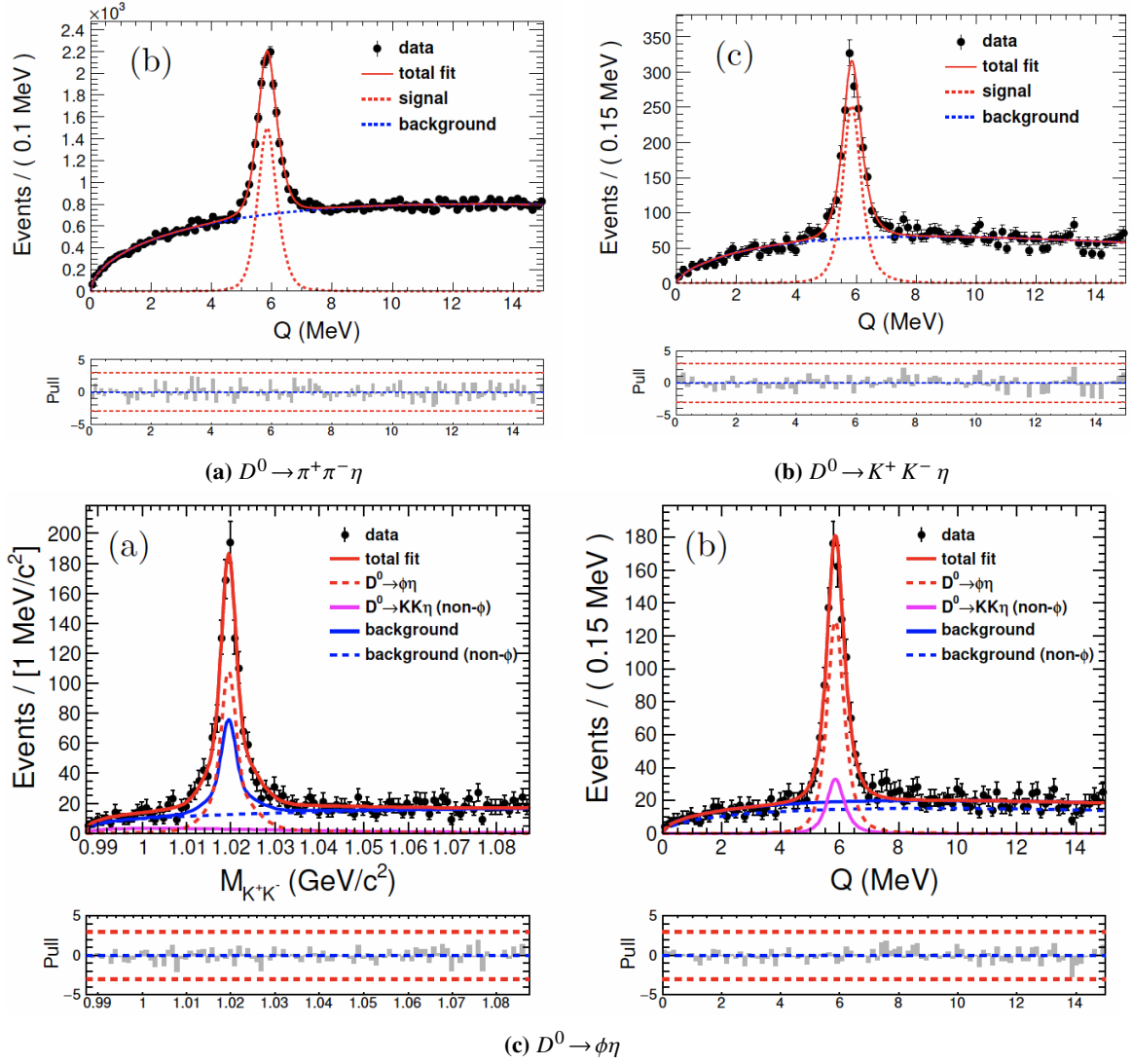
**Figure 1:** Fit projections in  $M$  and  $\Delta M$  for  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$  on left and  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$  on right. The corresponding pull [= (data – fit result)/(data uncertainty)] distributions are shown below each projection. The dashed red lines correspond to  $\pm 3\sigma$  values.

second is systematic [9]. We report the first  $CP$  violation search for  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$  decays using  $A_{CP}$  and  $a_{CP}^T$ . Both  $A_{CP}$  and  $a_{CP}^T$  measurements are consistent with zero  $CP$  violation.

We report the world's most precise branching fraction measurement for  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$  decays. The branching fraction, measured relative to that for  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ , is:  $\mathcal{B}(D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-) / \mathcal{B}(D^0 \rightarrow K_S^0 \pi^+ \pi^-) = [1.72 \pm 0.03 \text{ (stat)} \pm 0.04 \text{ (syst)}] \times 10^{-2}$ . Inserting the world average value  $\mathcal{B}(D^0 \rightarrow K_S^0 \pi^+ \pi^-) = (2.80 \pm 0.18)\%$  [17] gives  $\mathcal{B}(D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-) = [4.82 \pm 0.08 \text{ (stat)}_{-0.11}^{+0.10} \text{ (syst)} \pm 0.31 \text{ (norm)}] \times 10^{-4}$  where the last uncertainty is due to  $\mathcal{B}(D^0 \rightarrow K_S^0 \pi^+ \pi^-)$ .

### 3. Measurement of branching fractions and search for $CP$ violation in $D^0 \rightarrow \pi^+ \pi^- \eta$ , $D^0 \rightarrow K^+ K^- \eta$ , $D^0 \rightarrow \phi \eta$ decays

This paper [10] reports the branching fraction of Cabibbo suppressed  $D^0 \rightarrow \pi^+ \pi^- \eta$ ,  $D^0 \rightarrow K^+ K^- \eta$  and  $D^0 \rightarrow \phi \eta$  decays relative to the normalization mode  $D^0 \rightarrow K^- \pi^+ \eta$  using 988  $\text{fb}^{-1}$  of Belle data set. The signal yield is determined via a one-dimensional unbinned extended maximum-likelihood fit to the variable  $Q$ , where  $Q = M[K^+ K^- \eta \pi_s^+] - M[K^+ K^- \eta] - M[\pi_s^+]$  for  $D^0 \rightarrow \pi^+ \pi^- \eta$ ,  $D^0 \rightarrow K^+ K^- \eta$  and a two-dimensional fit in variables  $M[K^+ K^-]$ ,  $Q$  for  $D^0 \rightarrow \phi \eta$  decays. Fig. 2 shows the fit projections for the three modes. The measured branching fractions are  $\mathcal{B}(D^0 \rightarrow \pi^+ \pi^- \eta) = [1.22 \pm 0.02 \text{ (stat)} \pm 0.02 \text{ (syst)} \pm 0.03 \text{ (syst)}] \times 10^{-3}$ ,  $\mathcal{B}(D^0 \rightarrow K^+ K^- \eta) = [1.80_{-0.06}^{+0.07} \pm 0.04 \pm 0.05] \times 10^{-4}$  and  $\mathcal{B}(D^0 \rightarrow \phi \eta) = [1.84 \pm 0.09 \pm 0.06 \pm 0.05] \times 10^{-4}$ . The analysis report the search for  $CPV$  using  $A_{CP}$  similar to  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$  but with 8 bins in



**Figure 2:** Fig. (a), (b) show the 1d fit projections for  $D^0 \rightarrow \pi^+ \pi^- \eta$  and  $D^0 \rightarrow K^+ K^- \eta$ . Fig. (c) show the 2d fit projections on  $M[K^+ K^-]$ ,  $Q$  for  $D^0 \rightarrow \phi \eta$  decays.

$\cos(\theta^*)$ . The measured  $A_{CP}$  values are  $A_{CP}(D^0 \rightarrow \pi^+ \pi^- \eta) = [+0.90 \pm 1.20 \text{ (stat)} \pm 0.40 \text{ (syst)}]\%$ ,  $A_{CP}(D^0 \rightarrow K^+ K^- \eta) = [-1.40 \pm 3.30 \pm 1.0]\%$  and  $A_{CP}(D^0 \rightarrow \phi \eta) = [-1.90 \pm 4.40 \pm 0.60]\%$ . The result for  $D^0 \rightarrow \pi^+ \pi^- \eta$  is a significant improvement over the previous measurement and the other two are first  $CPV$  search for those decays. All results are consistent with zero  $CPV$ .

#### 4. Measurement of branching fractions for Cabbibo-Suppressed $D^+ \rightarrow K^+ K^- \pi^+ \pi^0$ , $D_{(s)}^+ \rightarrow K^+ \pi^- \pi^+ \pi^0$ decays

This analysis[11] measures the branching fraction of  $D^+ \rightarrow K^+ K^- \pi^+ \pi^0$ ,  $D_{(s)}^+ \rightarrow K^+ \pi^- \pi^+ \pi^0$  decays observed in the  $988 \text{ fb}^{-1}$  of Belle data set relative to the normalization modes  $D^+ \rightarrow K^- \pi^+ \pi^+ \pi^0$ ,  $D_s^+ \rightarrow K^+ K^- \pi^+ \pi^0$ . We extract the signal yield with a one-dimensional unbinned

extended maximum-likelihood fit to  $M[D_{(s)}^+]$ . The fit yields 50k  $D^+ \rightarrow K^+ K^- \pi^+ \pi^0$ , 3.6k for doubly CS  $D^+ \rightarrow K^+ \pi^- \pi^+ \pi^0$  and 26k for CS  $D_s^+ \rightarrow K^+ \pi^- \pi^+ \pi^0$  which is also the first observation for this decay. The measured branching fractions are:  $\mathcal{B}(D^+ \rightarrow K^+ K^- \pi^+ \pi^0) = [7.08 \pm 0.07 \pm 0.16 \pm 0.20] \times 10^{-3}$ ,  $\mathcal{B}(D^+ \rightarrow K^+ \pi^- \pi^+ \pi^0) = [1.05 \pm 0.05 \pm 0.02 \pm 0.03] \times 10^{-3}$  and  $\mathcal{B}(D_s^+ \rightarrow K^+ \pi^- \pi^+ \pi^0) = [9.44 \pm 0.25 \pm 0.28 \pm 0.32] \times 10^{-3}$ .

## 5. Summary

We reported precision measurements of branching fraction and  $CPV$  using  $A_{CP}$  and  $a_{CP}^T$  in Cabibbo suppressed charm meson decays obtained using the Belle detector. All the branching fractions and  $CPV$  measurements are either world's most precise results or first observation. All  $CPV$  results are consistent with zero  $CPV$  asymmetry.

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