

## Recent charm results from Belle

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**Longke Li\***

**On behalf of the Belle Collaboration**

*University of Cincinnati,  
Cincinnati, Ohio 45221, U.S.*

*E-mail: [lilk@ucmail.uc.edu](mailto:lilk@ucmail.uc.edu)*

Recent charm results from Belle experiment are presented in this proceedings, including (1) measurement of mixing parameter  $y_{CP} = (0.96 \pm 0.91 \pm 0.62^{+0.17}_{-0.00})\%$  in  $CP$ -odd decay for the first time, (2) the first Dalitz-plot analysis of  $D^0 \rightarrow K^- \pi^+ \eta$ , (3) measurement of branching fractions of  $\Lambda_c^+ \rightarrow \eta \Lambda^0 \pi^+$  and  $\eta \Sigma^0 \pi^+$  and intermediate processes  $\Lambda_c^+ \rightarrow [\Lambda(1670) \rightarrow \eta \Lambda^0] \pi^+$  and  $\Lambda_c^+ \rightarrow \eta \Sigma(1385)^+$  relative to  $\Lambda_c^+ \rightarrow p K^- \pi^+$ :  $0.293 \pm 0.003 \pm 0.014$ ,  $0.120 \pm 0.006 \pm 0.006$ ,  $(5.54 \pm 0.29 \pm 0.73) \times 10^{-2}$ , and  $0.192 \pm 0.006 \pm 0.016$ , respectively, and (4) first determination of the spin and parity of a charmed-strange baryon  $\Xi_c(2970)^+$  which is consistent with the HQSS prediction for  $J^P(s_l) = 1/2^+(0)$ .

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\*Speaker

## 1. Introduction to Belle at KEKB

KEKB [1] is an asymmetric-energy  $e^+e^-$  collider operating at and near  $\Upsilon(4S)$  mass peak. As the only detector installed in KEKB, Belle detector has a good performance on momentum and vertex resolution,  $K/\pi$  separation etc. A detailed description of the Belle detector can be found elsewhere [2]. It has been ten years since the final full data set ( $\sim 1 \text{ ab}^{-1}$ ) was accumulated, however, fruitful results on physics are lasting to be produced. Here we select some recent charm results from Belle to present in this proceedings.

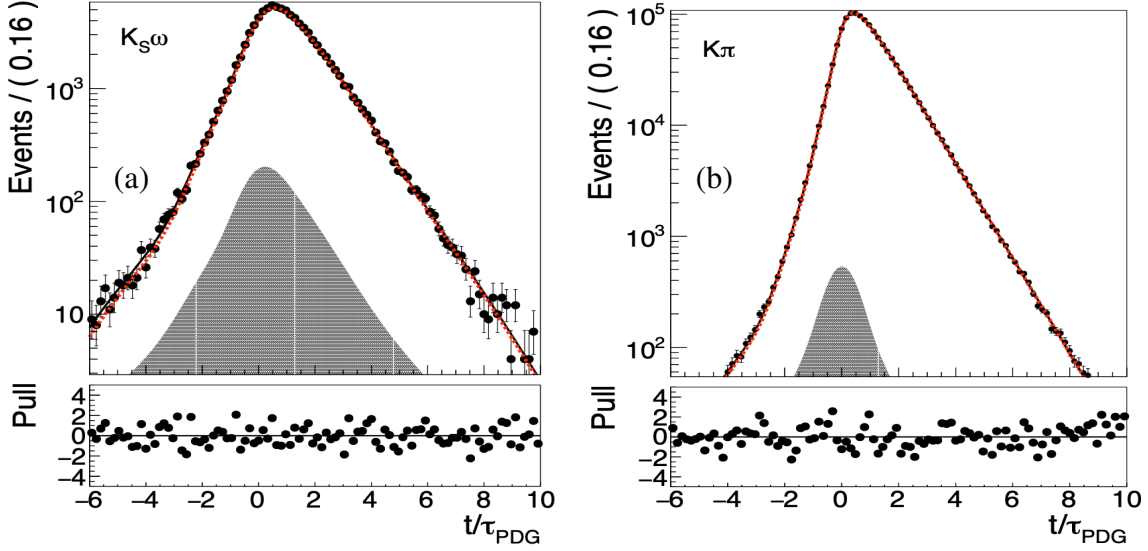
## 2. Charm-mixing parameter $y_{CP}$ in $D^0 \rightarrow K_S^0 \omega$

The mixing parameter  $y_{CP}$  is measured in  $D^0$  decays to the  $CP$ -odd final state  $K_S^0 \omega$  for the first time [3]. Considering mixing parameters  $|x|$  and  $|y| \ll 1$ , the decay-time dependence of  $D^0$  to a  $CP$  eigenstate is approximately exponential,  $d\Gamma/dt \propto e^{-\Gamma(1+\eta_f y_{CP})t}$  where  $\eta_f = +1$  ( $-1$ ) for  $CP$ -even (-odd) decays. Along with the decay rate in flavored eigenstate decays  $d\Gamma/dt \propto e^{-\Gamma t}$ , the  $y_{CP}$  is determined by the decay proper-time value with the formula  $y_{CP} = 1 - \frac{\tau(D^0 \rightarrow K^- \pi^+)}{\tau(D^0 \rightarrow K_S^0 \omega)}$ , where  $D^0 \rightarrow K^- \pi^+$  is the chosen normalization mode with flavor eigenstate final state.

Based on the full Belle data sample of  $976 \text{ fb}^{-1}$ , we obtain 91 thousands of  $D^0 \rightarrow K_S^0 \omega$  and 1.4 millions of reference mode  $D^0 \rightarrow K^- \pi^+$  in  $M - \Delta M$  signal region, where  $M$  is the invariant mass of reconstructed  $D^0$  and  $\Delta M$  is the mass difference of reconstructed  $D^{*+}$  and  $D^0$ . Using unbinned maximum-likelihood fits for lifetime on these two samples with high purities, the proper decay-time of  $D^0$  is determined as  $\tau_{K_S^0 \omega} = (410.47 \pm 3.73) \text{ fs}$  and  $\tau_{K\pi} = (406.53 \pm 0.57) \text{ fs}$ , as shown in Fig. 1. Thus, we calculate  $y_{CP} = (0.96 \pm 0.91 \pm 0.62_{-0.00}^{+0.17})\%$ , where the first uncertainty is statistical, the second is systematic due to event selection and background, and the last is due to possible presence of  $CP$ -even decays in the data sample. This  $y_{CP}$  result is consistent with the world average value. In the future, comparing more precise measurements of  $y_{CP}$  with that of  $y$  may test the SM precisely or reveal new physics effects in the charm system.

## 3. Dalitz-plot analysis of $D^0 \rightarrow K^- \pi^+ \eta$ decays

The understanding of hadronic charmed-meson decay is theoretically challenging due to the significant non-perturbative contributions, and input from experimental measurements thus plays an important role. A Dalitz-plot analysis of  $D^0 \rightarrow K^- \pi^+ \eta$  is performed for the first time at Belle based on  $953 \text{ fb}^{-1}$  of data [4]. Using a  $M$ - $Q$  two-dimensional fit where  $M$  is the invariant-mass of reconstructed  $D^0$  meson,  $M = M(K^+ \pi^- \eta)$ , and  $Q$  is the released energy of  $D^{*+}$  decay,  $Q = M(K^- \pi^+ \eta \pi_s) - M - m_{\pi_s}$ , a signal yield of  $105 197 \pm 990$  is obtained in the signal region of  $1.85 \text{ GeV}/c^2 < M < 1.88 \text{ GeV}/c^2$  and  $5.35 \text{ MeV}/c^2 < Q < 6.35 \text{ MeV}/c^2$  with a high purity ( $94.6 \pm 0.9\%$ ). The Dalitz plot is well described by a combination of the six resonant decay channels  $\bar{K}^*(892)^0 \eta$ ,  $K^- a_0(980)^+$ ,  $K^- a_2(1320)^+$ ,  $\bar{K}^*(1410)^0 \eta$ ,  $K^*(1680)^- \pi^+$  and  $K_2^*(1980)^- \pi^+$ , together with  $K\pi$  and  $K\eta$  S-wave components, as shown in Fig. 2. The dominant contributions to the decay amplitude arise from  $\bar{K}^*(892)^0$ ,  $a_0(980)^+$  and the  $K\pi$  S-wave component. The  $K\eta$  S-wave component, including  $K_0^*(1430)^-$ , is observed with a statistical significance of more than



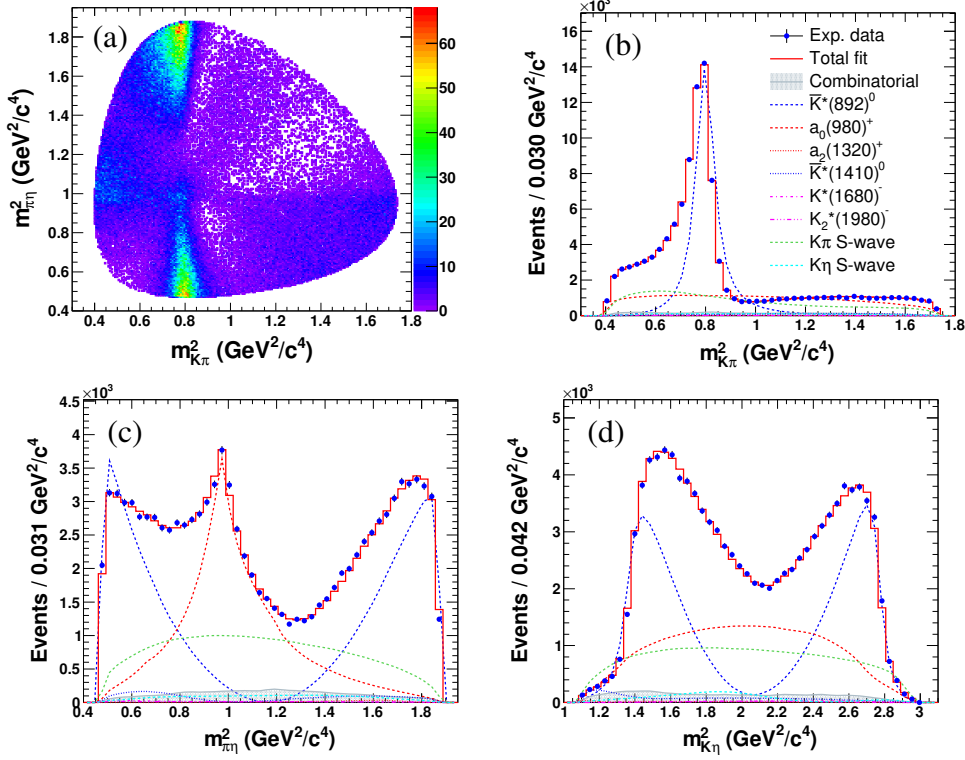
**Figure 1:** The fit of  $D^0$  proper lifetime: (a)  $D^0 \rightarrow K_S^0 \omega$  and (b)  $D^0 \rightarrow K^- \pi^+$ . The dashed red curves are the signal contribution, and the shaded surfaces beneath are the background estimated from  $M - \Delta M$  sidebands.

$30\sigma$ , and the decays  $K^*(1680)^- \rightarrow K^- \eta$  and  $K_2^*(1980)^- \rightarrow K^- \eta$  are observed for the first time and have statistical significances of  $16\sigma$  and  $17\sigma$ , respectively.

We extract the signal yield from the  $D^0$  invariant mass distribution in  $1.78 \text{ GeV}/c^2 < M < 1.94 \text{ GeV}/c^2$  and  $|Q - 5.85| < 1.0 \text{ MeV}/c^2$ , and obtain for the first time the branching ratio  $\frac{\mathcal{B}(D^0 \rightarrow K^- \pi^+ \eta)}{\mathcal{B}(D^0 \rightarrow K^- \pi^+)} = 0.500 \pm 0.002(\text{stat}) \pm 0.020(\text{syst}) \pm 0.003(\mathcal{B}_{\text{PDG}})$ , which corresponds to  $\mathcal{B}(D^0 \rightarrow K^- \pi^+ \eta) = (1.973 \pm 0.009(\text{stat}) \pm 0.079(\text{syst}) \pm 0.018(\mathcal{B}_{\text{PDG}}))\%$ . Then utilizing the world average branching fractions of intermediate resonant decays, the relative branching ratio  $\frac{\mathcal{B}(K^*(1680)^- \rightarrow K^- \eta)}{\mathcal{B}(K^*(1680)^- \rightarrow K^- \pi^0)}$  is determined to be  $0.11 \pm 0.02(\text{stat})_{-0.04}^{+0.06}(\text{syst}) \pm 0.04(\mathcal{B}_{\text{PDG}})$ . This is not consistent with the theoretical prediction under an assumption of a pure  $1^3D_1$  state [5]. We also determine the product of branching fraction  $\mathcal{B}(D^0 \rightarrow [K_2^*(1980)^- \rightarrow K^- \eta] \pi^+) = (2.2_{-1.9}^{+1.7}) \times 10^{-4}$ . For  $a_0(980)^+$ , we confirm the  $\pi\eta'$  contribution in the three-channel Flatté model with a statistical significance of  $10.1\sigma$ . We have also determined the branching fraction  $\mathcal{B}(D^0 \rightarrow \bar{K}^*(892)^0 \eta) = (1.41_{-0.12}^{+0.13})\%$ , which is consistent with, and more precise than, the current world average of  $(1.02 \pm 0.30)\%$ . It deviates from the various theoretical predictions of  $(0.51\text{-}0.92)\%$  [6] with a significance of more than  $3\sigma$ .

#### 4. Measurement of Branching Fractions of $\Lambda_c^+ \rightarrow \eta \Lambda \pi^+$ , $\eta \Sigma^0 \pi^+$ , $\Lambda(1670) \pi^+$ , and $\eta \Sigma(1385)^+$

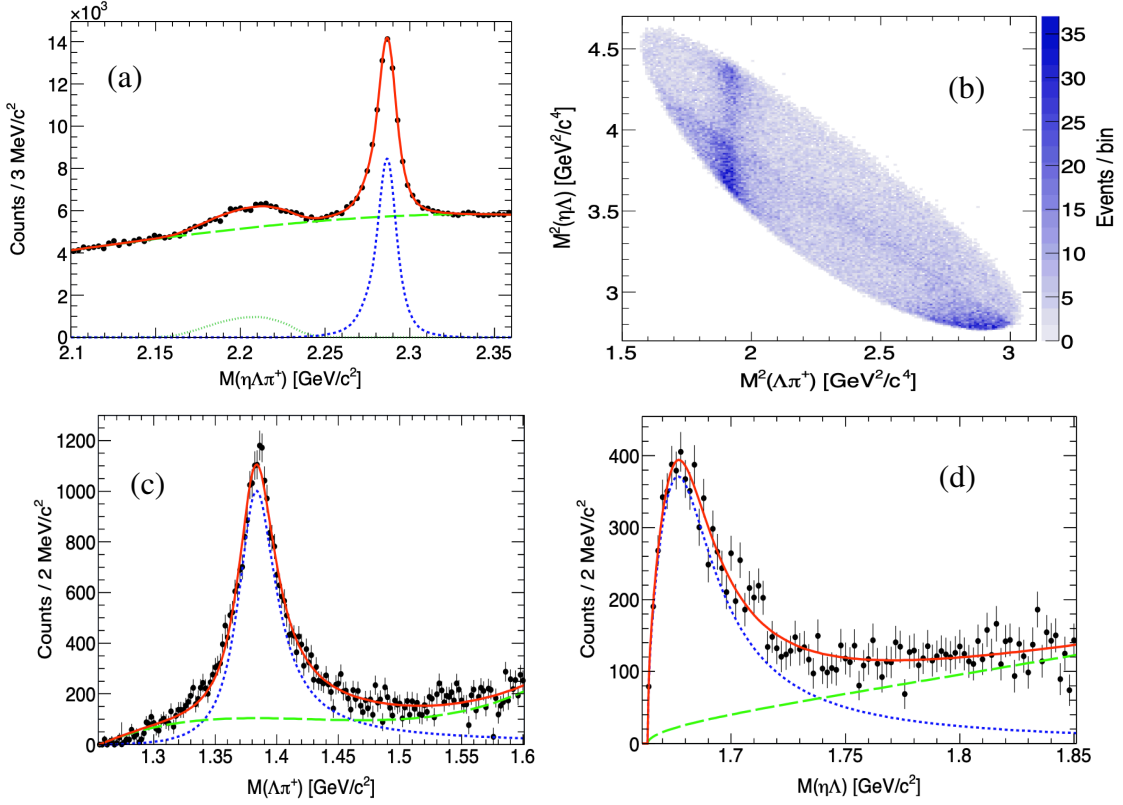
The branching fractions of weakly decaying charmed baryons provide a way to study both strong and weak interactions. The  $\Lambda_c^+ \rightarrow \eta \Lambda \pi^+$  decay mode is especially interesting since it has been suggested that it is an ideal decay mode to study the  $\Lambda(1670)$  and  $a_0(980)$  because, for any combination of two particles in the final state, the isospin is fixed. Based on a  $980 \text{ fb}^{-1}$  data sample, the branching fractions of  $\Lambda_c^+ \rightarrow \eta \Lambda \pi^+$ ,  $\eta \Sigma^0 \pi^+$ ,  $\Lambda(1670) \pi^+$ , and  $\eta \Sigma(1385)^+$  are measured [7]. The  $M(\eta \Lambda \pi^+)$  spectrum is shown in Fig. 3 (a). The  $\Lambda_c^+ \rightarrow \eta \Sigma^0 \pi^+$  is observed indirectly as a feed-down component and it has efficiency-corrected yield  $N_{\text{cor}} = (3.05 \pm 0.16) \times 10^5$ . Considering



**Figure 2:** The Dalitz plot of  $D^0 \rightarrow K^- \pi^+ \eta$  in (a)  $M$ - $Q$  signal region  $1.85 \text{ GeV}/c^2 < M < 1.88 \text{ GeV}/c^2$  and  $5.35 \text{ MeV}/c^2 < Q < 6.35 \text{ MeV}/c^2$ , and projections on (b)  $m_{K\pi}^2$ , (c)  $m_{\pi\eta}^2$  and (d)  $m_{K\eta}^2$ . In projections the fitted contributions of individual components are shown, along with contribution of combinatorial background (grey-filled) from sideband region.

$\Lambda_c^+ \rightarrow \eta \Lambda \pi^+$  and  $\Lambda_c^+ \rightarrow p K^- \pi^+$  have sufficiently large statistic, the yields in individual bins of Dalitz plots are determined:  $N_{cor}(\eta \Lambda \pi^+) = (7.41 \pm 0.07) \times 10^5$  and  $N_{cor}(p K^- \pi^+) = (1.005 \pm 0.001) \times 10^7$ . Finally, the branching ratios of  $\Lambda_c^+ \rightarrow \eta \Lambda \pi^+$  and  $\Lambda_c^+ \rightarrow \eta \Sigma^0 \pi^+$  relative to  $\Lambda_c^+ \rightarrow p K^- \pi^+$  are  $0.293 \pm 0.003 \pm 0.014$  and  $0.120 \pm 0.006 \pm 0.006$ , where the uncertainties are statistical and systematic, respectively.

On the Dalitz plot of  $\Lambda_c^+ \rightarrow \eta \Lambda \pi^+$  shown in Fig. 3 (b), bands corresponding to  $\Lambda_c^+ \rightarrow \Lambda(1670) \pi^+ / \eta \Sigma(1385)^+$  resonant sub-channels are seen clearly, along with  $\Lambda_c^+ \rightarrow \Lambda a_0(980)^+$ . For every  $2 \text{ MeV}/c^2$  bin of  $M(\eta \Lambda)$  and  $M(\Lambda \pi^+)$  distributions, the  $\Lambda_c^+$  yield is obtained by fitting  $M(\eta \Lambda \pi^+)$ . Then, a relativistic Breit-Wigner with momentum-dependent width is used to describe the S-wave  $\Lambda(1670)$  and the P-wave  $\Sigma(1385)$ , as shown in Fig. 3 (c, d). Then, we determine the relative branching ratio  $\frac{\mathcal{B}(\Lambda_c^+ \rightarrow [\Lambda(1670) \rightarrow \eta \Lambda] \pi^+)}{\mathcal{B}(\Lambda_c^+ \rightarrow p K^- \pi^+)} = (5.54 \pm 0.29 \pm 0.73)\%$  and  $\frac{\mathcal{B}(\Lambda_c^+ \rightarrow \eta \Sigma(1385)^+)}{\mathcal{B}(\Lambda_c^+ \rightarrow p K^- \pi^+)} = 0.192 \pm 0.006 \pm 0.016$ . Finally after using the world averaged  $\mathcal{B}(\Lambda_c^+ \rightarrow p K^- \pi^+)$ , we have  $\mathcal{B}(\Lambda_c^+ \rightarrow [\Lambda(1670) \rightarrow \eta \Lambda] \pi^+) = (3.48 \pm 0.19 \pm 0.46 \pm 0.18) \times 10^{-3}$  and  $\mathcal{B}(\Lambda_c^+ \rightarrow \eta \Sigma(1385)^+) = (1.21 \pm 0.04 \pm 0.10 \pm 0.06)\%$ , where the first two uncertainties are statistical and systematic uncertainties, and the third uncertainty is from  $\mathcal{B}(\Lambda_c^+ \rightarrow p K^- \pi^+)$ .



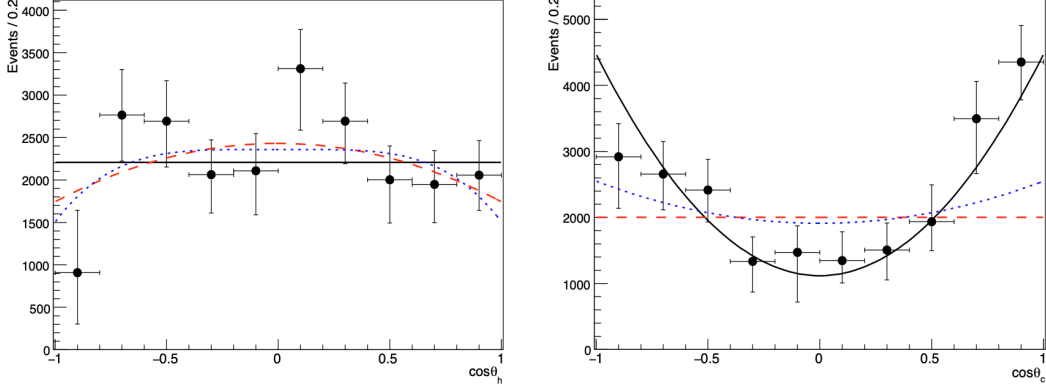
**Figure 3:** Top figures are (a) the invariant mass of  $\eta\Lambda\pi^+$  and (b) its Dalitz plot in signal region. Bottom figures are fits to the  $\Lambda_c^+$  yield in the (c)  $M(\eta\Lambda)$  and (d)  $M(\Lambda\pi^+)$  spectra, where the curves indicate the total fit result (solid red), the signal modeled with a relativistic Breit-Wigner function (dashed blue), and the background (long-dashed green).

## 5. First determination of the Spin and Parity of $\Xi_c(2970)^+$

The unclear theoretical situation motivates an experimental determination of spin and parity of a charmed-strange baryon  $\Xi_c(2970)$ , which provides important information to test predictions and help decipher its nature. Using a  $980 \text{ fb}^{-1}$  data sample, the spin and parity of a charmed-strange baryon  $\Xi_c(2970)^+$  is measured [8] by (1) studies of the helicity angle distributions,  $\theta_h$  of  $\Xi_c(2970)^0$  and  $\theta_c$  of  $\Xi_c(2645)^0$  in  $\Xi_c(2970)^+ \rightarrow \Xi_c(2645)^0\pi^+ \rightarrow \Xi_c^+\pi^-\pi^+$ , and (2) a measurement of the  $\Xi_c(2970)^+$  decay branching ratio  $R = \mathcal{B}(\Xi_c(2970)^+ \rightarrow \Xi_c(2645)^0\pi^+)/\mathcal{B}(\Xi_c(2970)^+ \rightarrow \Xi_c^0\pi^+)$ .

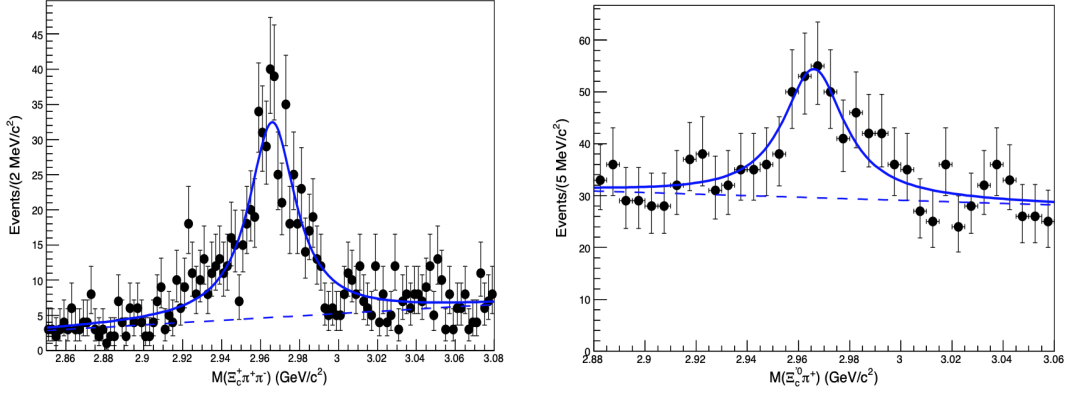
The angular distribution are obtained by dividing the data into 10 equal bins for  $\cos\theta_h$  and  $\cos\theta_c$ , each within intervals of 0.2. The yield of  $\Xi_c(2970)^+ \rightarrow \Xi_c(2645)^0\pi^+$  for each bin is obtained by fitting the invariant-mass distribution of  $M(\Xi_c^+\pi^-\pi^+)$  for the  $\Xi_c(2645)^0$  signal region (within  $5 \text{ MeV}/c^2$  of  $\Xi_c(2645)^0$  nominal mass) and sidebands (interval from 15 to 25  $\text{MeV}/c^2$  away from  $\Xi_c(2645)^0$  nominal mass). The background-subtracted and efficiency-corrected yield distribution in Fig. 4 is fitted with expected decay-angle distributions  $W_J$  for different spin hypotheses. The best fit is for  $J = 1/2$ , while others are excluded with small significance, which shows inconclusive result. For helicity angle  $\theta_c$ , with an assumption that the lowest partial wave dominates, the expected angular correlation  $W(\theta_c)$  is used to describe the distribution. Finally the  $J^P = 1/2^+$  hypothesis is

better than  $3/2^-$  or  $5/2^+$  ones at the level of  $5.1\sigma$  or  $4.0\sigma$ .



**Figure 4:** The yields on the cosine of helicity angle of  $\Xi_c(2970)^0$  (left,  $J = 1/2$  for solid black;  $J = 3/2$  for dashed red;  $J = 5/2$  for dotted blue) and on cosine of helicity angle of  $\Xi_c(2645)^0$  (right,  $J^P = 1/2^+$  for solid black;  $J = 3/2^-$  for dashed red;  $J = 5/2^+$  for dotted blue) in  $\Xi_c(2970)^+ \rightarrow \Xi_c(2645)^0 \pi^+$  decay.

The parity of  $\Xi_c(2970)^+$  is established [8] from the ratio between  $\mathcal{B}(\Xi_c(2970)^+ \rightarrow \Xi_c(2645)^0 \pi^+)$  and  $\mathcal{B}(\Xi_c(2970)^+ \rightarrow \Xi_c^0 \pi^+)$  by  $R = \frac{N^*}{\epsilon^* N(\Xi_c^+)/\epsilon^+} / \frac{N'}{\sum_i \epsilon'_i N(\Xi_c^0)_i / \epsilon_i^0}$ , where  $\Xi_c^0$  uses two modes,  $\Xi^- \pi^+$  and  $\Omega^- K^+$ . The yields  $N^{*,'}$  are obtained by fitting the invariant-mass distributions in Fig. 5. Finally we have  $R = 1.67 \pm 0.29(stat)_{-0.09}^{+0.15}(syst) \pm 0.25(IS)$ , where the last uncertainty is due to possible isospin-symmetry-breaking effects (15%). Heavy-quark spin symmetry (HQSS) predicts  $R = 1.06$  (0.26) for a  $1/2^+$  state with the spin of the light-quark degrees of freedom  $s_l = 0$  (1) [9]. Our result favors a positive-parity assignment with  $s_l = 0$ . We note that HQSS predictions could be larger than the quoted value by a factor of  $\sim 2$  with higher-order terms in  $(1/m_c)$  [10], so our result is consistent with the HQSS prediction for  $J^P(s_l) = 1/2^+(0)$ .



**Figure 5:**  $\Xi_c^+ \pi^- \pi^+$  invariant-mass distribution for  $\Xi_c(2970)^+ \rightarrow \Xi_c(2645)^0 \pi^+ \rightarrow \Xi_c^+ \pi^- \pi^+$ , and  $\Xi_c^0 \pi^+$  invariant-mass distribution for  $\Xi_c(2970)^+ \rightarrow \Xi_c^0 \pi^+ \rightarrow \Xi_c^0 \gamma \pi^+$ . The fit result (solid blue curve) is presented along with the background (dashed blue curve)

## 6. Summary

Belle experiment has achieved the fruitful productions of flavor physics to date. Some selected recent charm results are presented, including charm mixing parameter  $y_{CP}$  in  $CP$ -odd decay

$D^0 \rightarrow K_S^0 \omega$ , hadronic decays  $D^0 \rightarrow K^- \pi^+ \eta$  and  $\Lambda_c^+ \rightarrow \eta \Lambda \pi^+ / \eta \Sigma^0 \pi^+$ , first determination of the spin and parity of  $\Xi_c(2970)^+$ . More charming charm results from Belle will come out in near future. As a summary, I would like to say, "Belle is not only keeping alive but still keeping energetic, together with its upgraded experiment Belle II who is under a rapid growth."

## References

- [1] S. Kurokawa and E. Kikutani, *Nucl. Instrum. Methods Phys. Res. Sect. A* **499**, 1 (2003), and other papers included in this Volume.
- [2] A. Abashian *et al.* (Belle Collaboration), *Nucl. Instrum. Methods Phys. Res. Sect. A* **479**, 117 (2002).
- [3] M. Nayak *et al.* (Belle Collaboration), *Phys. Rev. D* **102**, 071102(R) (2020).
- [4] Y. Q. Chen *et al.* (Belle Collaboration), *Phys. Rev. D* **102**, 012002 (2020).
- [5] T. Barnes, N. Black, and P. R. Page, *Phys. Rev. D* **68**, 054014 (2003); C. Q. Pang, J. Z. Wang, X. Liu, *et al.* *Eur. Phys. J. C* (2017) **77**: 861.
- [6] H. Y. Cheng and C. W. Chiang, *Phys. Rev. D* **81**, 074021 (2010); H. N. Li, C. D. Lü, and F. S. Yu, *Phys. Rev. D* **86**, 036012 (2012); Q. Qin, H. N. Li, C. D. Lü, and F. S. Yu, *Phys. Rev. D* **89**, 054006 (2014).
- [7] J. Y. Lee *et al.* (Belle Collaboration), [arXiv:2008.11575](https://arxiv.org/abs/2008.11575).
- [8] T. J. Moon *et al.* (Belle Collaboration), [arXiv:2007.14700](https://arxiv.org/abs/2007.14700)
- [9] Hai-Yang Cheng and Chun-Khiang Chua, *Phys. Rev. D* **75**, 014006 (2007).
- [10] Adam F. Falk and Thomas Mehen, *Phys. Rev. D* **53**, 231 (1996).