

B anomalies linked to the problem of the origin of Yukawa couplings

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We discuss a theory of flavour in which Higgs Yukawa couplings are related to those of the new scalar triplet leptoquark and/or Z' responsible for $R_{K^{(*)}}$, with all couplings arising effectively from mixing with a vector-like fourth family, whose mass may be anywhere from the Planck scale to the electroweak scale for the leptoquarks explanation, but is pinned down to the TeV scale if the Z' exchange plays a role. However, in this particular model, only leptoquark exchange can contribute significantly to $R_{K^{(*)}}$, since Z' exchange is too constrained from B_s mixing and $\tau \rightarrow 3\mu$, although other Higgs Yukawa matrix structures may allow it.

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1. Introduction

The Standard Model (SM) has almost thirty parameters, most of them arising from the unspecified Higgs Yukawa couplings. This motivates theories of flavour beyond the SM. Here we shall consider one simple example where the usual Higgs Yukawa couplings with the three families of chiral fermions are forbidden by some symmetry, which is broken by some new scalar field $\langle\phi\rangle$, allowing the Higgs Yukawa couplings to arise effectively from mixing with a vector-like fourth family [1]. In principle the mass of the vector-like fourth family M_4 (i.e. the flavour scale in this example) may be anywhere from the Planck scale to the electroweak scale, providing that the ratios $\langle\phi\rangle/M_4$ which govern the Yukawa couplings are held fixed.

The LHCb Collaboration [2] and other experiments have reported a number of anomalies in $B \rightarrow K^{(*)}l^+l^-$ decays such as the R_K and R_{K^*} ratios of $\mu^+\mu^-$ to e^+e^- final states, which are observed to be about 80% of their expected values with a 2.5σ deviation from the SM. Such anomalies may be accounted for by a new physics operator of the form [2] $\bar{b}_L\gamma^\mu s_L\bar{\mu}_L\gamma_\mu\mu_L$, with a coefficient Λ^{-2} where $\Lambda \sim 30$ TeV. This hints that there may be new physics arising from the non-universal couplings of leptoquarks and/or Z' in order to generate such an operator. However the introduction of these new particles increases the parameter count still further, and only serves to make the flavour problem of the SM worse.

Motivated by such considerations, it is interesting to speculate that the above empirical hint of flavour non-universality is linked to a possible theory of flavour. In this talk we consider an example of this based on the vector-like fourth family discussed above. To achieve the desired link, one may introduce leptoquarks and/or Z' into the above theory of flavour in such a way that the effective Higgs Yukawa couplings and the effective leptoquark and/or Z' couplings are generated at the same time, from mixing with the vector-like fourth family. In such a model, the couplings of leptoquarks and/or Z' may be related to Yukawa couplings, leading to a very predictive framework.

2. Model of flavour and $R_{K^{(*)}}$ with leptoquarks and Z'

Consider the model in Table 1 with a vector-like fourth family of fermions of mass M_4 [1]. The model also involves a gauged $U(1)'$, which is broken by a singlet ϕ leading to a massive Z' with non-universal couplings [3, 4, 5]. We have also included a scalar leptoquark triplet S_3 of mass M_{S_3} [6, 7]. The model in Table 1, defined in these proceedings for the first time, may be regarded as an amalgamation of the Z' model [5] and the leptoquark model [7], where both models previously included also a vector-like fourth family of fermions. The idea is that the usual three chiral families of quarks and leptons do not have renormalisable couplings to Higgs or leptoquarks or Z' (since they are neutral under $U(1)'$). However, as we shall see, such couplings are generated via mixing with the vector-like fourth family, thereby relating all these couplings to each other.

2.1 The Higgs couplings

We first consider the couplings involving the two Higgs doublets $H_{u,d}$. This was first discussed in [1], where a Z_2 symmetry prevented the usual Yukawa couplings. Here it is the gauged $U(1)'$ which forbids the usual Yukawa couplings since the Higgs carry the new charges while the chiral fermions do not. However Higgs scalar doublets with $U(1)'$ charge -1 can couple a chiral fermion

Field	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$U(1)'$
Q_i	$\mathbf{3}$	$\mathbf{2}$	$1/6$	0
u_i^c	$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	0
d_i^c	$\bar{\mathbf{3}}$	$\mathbf{1}$	$1/3$	0
L_i	$\mathbf{1}$	$\mathbf{2}$	$-1/2$	0
e_i^c	$\mathbf{1}$	$\mathbf{1}$	1	0
ν_i^c	$\mathbf{1}$	$\mathbf{1}$	0	0
Q_4	$\mathbf{3}$	$\mathbf{2}$	$1/6$	1
u_4^c	$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	1
d_4^c	$\bar{\mathbf{3}}$	$\mathbf{1}$	$1/3$	1
L_4	$\mathbf{1}$	$\mathbf{2}$	$-1/2$	1
e_4^c	$\mathbf{1}$	$\mathbf{1}$	1	1
ν_4^c	$\mathbf{1}$	$\mathbf{1}$	0	1
\bar{Q}_4	$\bar{\mathbf{3}}$	$\bar{\mathbf{2}}$	$-1/6$	-1
\bar{u}_4^c	$\mathbf{3}$	$\mathbf{1}$	$2/3$	-1
\bar{d}_4^c	$\mathbf{3}$	$\mathbf{1}$	$-1/3$	-1
\bar{L}_4	$\mathbf{1}$	$\bar{\mathbf{2}}$	$1/2$	-1
\bar{e}_4^c	$\mathbf{1}$	$\mathbf{1}$	-1	-1
$\bar{\nu}_4^c$	$\mathbf{1}$	$\mathbf{1}$	0	-1
H_u	$\mathbf{1}$	$\mathbf{2}$	$1/2$	-1
H_d	$\mathbf{1}$	$\mathbf{2}$	$-1/2$	-1
ϕ	$\mathbf{1}$	$\mathbf{1}$	0	1
S_3	$\bar{\mathbf{3}}$	$\mathbf{3}$	$1/3$	-2

Table 1: The model consists of three chiral fermion families, one vector-like fermion family and two Higgs scalar doublets. The gauged $U(1)'$ is broken by a singlet ϕ leading to a massive Z' . We also include a scalar leptoquark triplet S_3 .

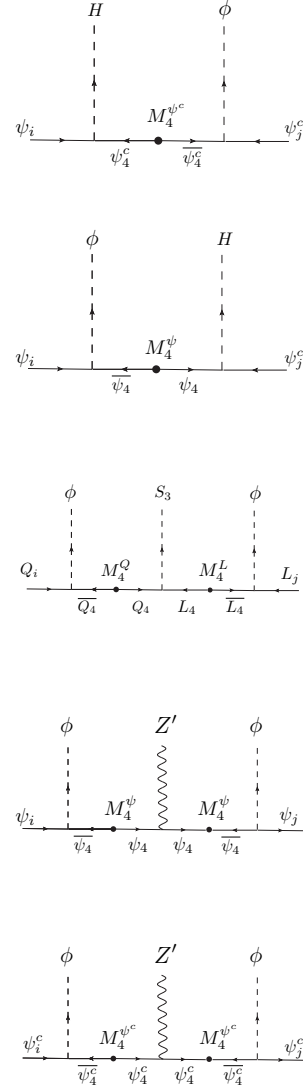


Table 2: Effective Higgs couplings (upper two) (where $H = H_{u,d}$, $\psi_i = Q_i, L_i$ and $\psi_i^c = u_i^c, d_i^c, e_i^c$), leptoquark couplings (middle) and Z' couplings (lower two).

to a vector-like fourth family fermion with $U(1)'$ charge $+1$, controlled by new Yukawa couplings y_{4i} . The $U(1)'$ also allows the scalar singlet ϕ to couple a chiral fermion to a vector-like fourth family fermion, controlled by new Yukawa couplings x_i . These couplings generate the 3×3 effective Yukawa matrices, via the upper diagrams in Table 2, in a particular basis [1]:

$$y_{ij}^{e,u} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & \varepsilon_{22}^{e,u} & \varepsilon_{23}^{e,u} \\ 0 & \varepsilon_{32}^{e,u} & y_{33}^{e,u} + \varepsilon_{33}^{e,u} \end{pmatrix}, \quad y_{ij}^d = \begin{pmatrix} 0 & \varepsilon_{12}^d & \varepsilon_{13}^d \\ 0 & \varepsilon_{22}^d & \varepsilon_{23}^d \\ 0 & \varepsilon_{32}^d & y_{33}^d + \varepsilon_{33}^d \end{pmatrix}, \quad (2.1)$$

where the effective Yukawa couplings ε_{ij} are defined as $\varepsilon_{ij}^e H_d L_i e_j^c$, $\varepsilon_{ij}^u H_u Q_i u_j^c$, $\varepsilon_{ij}^d H_d Q_i d_j^c$, and are

given by the upper left diagrams in Table 2, hence $\varepsilon_{ij}^{e,u,d} \propto 1/M_4^{e,u,d}$. These couplings are suppressed $\varepsilon_{ij} \ll y_{33}$, assuming $M_4^{L,Q} \ll M_4^{e,u,d}$ (see [1] for more details).

To leading order the dominant third family Yukawa couplings are given by the upper right diagrams in Table 2,

$$y_\tau \approx y_{33}^e \approx y_{43}^e \left(\frac{x_3^L \langle \phi \rangle}{M_4^L} \right), \quad y_t \approx y_{33}^u \approx y_{43}^u \left(\frac{x_3^Q \langle \phi \rangle}{M_4^Q} \right), \quad y_b \approx y_{33}^d \approx y_{43}^d \left(\frac{x_3^Q \langle \phi \rangle}{M_4^Q} \right) \quad (2.2)$$

where the effective Yukawa couplings are defined for the two Higgs doublet model as $y_{33}^e H_d L_3 e_3^c$, $y_{33}^u H_u Q_3 u_3^c$ and $y_{33}^d H_d Q_3 d_3^c$. In this basis, only the third family Yukawa couplings originate from such diagrams [1].

Interestingly, the fourth family vector-like neutrinos provide a new contribution to neutrino mass via the type Ib seesaw¹ diagram in Fig. 1 (left) [8]. Below the mass scale of the fourth family of vector-like neutrinos, this leads to a new Weinberg operator for neutrino mass of the form $\frac{1}{M_4^{\nu_c}} H_u \tilde{H}_d L_i L_j$ involving the two different Higgs doublets H_u , \tilde{H}_d , where the charge conjugated doublet $\tilde{H}_d = -i\sigma_2 H_d^*$, and H_d^* is the complex conjugate of H_d . For more details including a phenomenological analysis see [8].

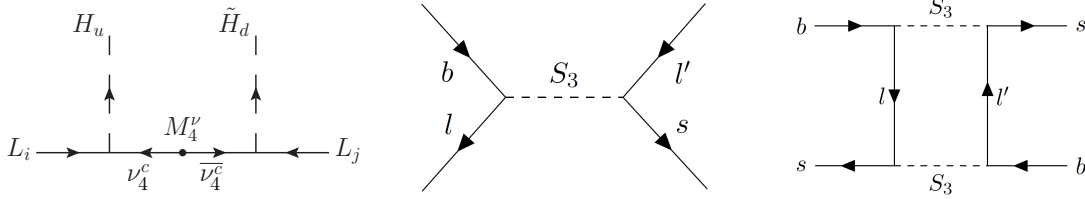


Figure 1: The fourth family vector-like neutrinos allows a new contribution to neutrino mass via a diagram involving two different Higgs doublets H_u , \tilde{H}_d (left), which we refer to as the type Ib seesaw mechanism. The leptoquark S_3 contributes to $R_{K^{(*)}}$ at tree-level (centre), and to B_s mixing at one loop (right).

2.2 The leptoquark couplings

We now consider the couplings involving the scalar leptoquark triplet S_3 as discussed in [7]. The assigned $U(1)'$ charges allow the renormalisable leptoquark coupling, $\lambda_4 S_3 Q_4 L_4$, involving the fourth family, but not the first three families. The middle diagram in Table 2 generates a single effective leptoquark coupling, which involves the third family (only) in the same basis as Eq.2.1 [7]:

$$\lambda_4 \left(\frac{x_3^L \langle \phi \rangle}{M_4^L} \right) \left(\frac{x_3^Q \langle \phi \rangle}{M_4^Q} \right) S_3 Q_3 L_3 \approx \lambda_4 \left(\frac{y_{33}^e}{y_{43}^e} \right) \left(\frac{y_{33}^u}{y_{43}^u} \right) S_3 Q_3 L_3 \approx y_\tau y_t S_3 Q_3 L_3 \quad (2.3)$$

where the first equality in Eq.2.3 has used Eq.2.2, and the second equality sets $y_{4i} \approx \lambda_4 \approx 1$.

Effective leptoquark couplings to first and second family quarks and leptons are generated when the Yukawa matrices in Eq.2.1 are diagonalised and so are suppressed by ε_{ij}/y_{33} . Since down quark mixing is larger than up quark mixing (due to the milder mass hierarchy), we assume

¹We refer to the seesaw mechanism involving two different Higgs doublets H_u , \tilde{H}_d as type Ib to distinguish it from the usual seesaw mechanism involving two identical Higgs doublets H_u which we refer to as type Ia.

$\theta_{23}^d \approx V_{ts}$, while the analogous charged lepton mixing angle θ_{23}^e is similarly small. Hence in the diagonal Yukawa basis we have leptoquark couplings involving the left-handed lepton doublets $L_3 = (\nu_\tau, \tau)_L^T$, $L_2 = (\nu_\mu, \mu)_L^T$, and quark doublets $Q_3 = (t, b)_L^T$, $Q_2 = (c, s)_L^T$, from Eq.2.3, assuming $y_t \approx 1$,

$$y_\tau S_3 Q_3 L_3, \quad y_\tau V_{ts} S_3 Q_2 L_3, \quad y_\tau \theta_{23}^e S_3 Q_3 L_2, \quad y_\tau \theta_{23}^e V_{ts} S_3 Q_2 L_2, \quad \dots \quad (2.4)$$

Thus, after a number of reasonable dynamical assumptions, we have obtained the leptoquark couplings in Eq.2.4 in terms of Yukawa couplings and mixing angles.

The leptoquark couplings in Eq.2.4 have a number of interesting phenomenological implications, mainly due to the the couplings of the electric charge $+4/3$ component of S_3 to the physical left-handed down quark and charged lepton mass eigenstates

$$\lambda_{b\tau} S_3 b_L \tau_L, \quad \lambda_{s\tau} S_3 s_L \tau_L, \quad \lambda_{b\mu} S_3 b_L \mu_L, \quad \lambda_{s\mu} S_3 s_L \mu_L, \quad (2.5)$$

$$\lambda_{b\tau} \approx y_\tau, \quad \lambda_{s\tau} \approx y_\tau V_{ts}, \quad \lambda_{b\mu} \approx y_\tau \theta_{23}^e, \quad \lambda_{s\mu} \approx y_\tau \theta_{23}^e V_{ts}. \quad (2.6)$$

The leptoquark S_3 contributes to $R_{K^{(*)}}$ at tree-level, via the (centre) diagram in Fig.1, where the requirement to explain the anomaly is [7]

$$\frac{\lambda_{b\mu} \lambda_{s\mu}}{M_{S_3}^2} \approx \frac{y_\tau^2 (\theta_{23}^e)^2 V_{ts}}{M_{S_3}^2} \approx \frac{1.1}{(35 \text{ TeV})^2} \rightarrow y_\tau^2 (\theta_{23}^e)^2 \approx 2.2 \times 10^{-2} \left(\frac{M_{S_3}}{1 \text{ TeV}} \right)^2, \quad (2.7)$$

using $V_{ts} \approx 4.0 \times 10^{-2}$, which requires quite a large $y_\tau \approx 1$ (i.e. large $\tan \beta = \langle H_u \rangle / \langle H_d \rangle$) and a large mixing angle $\theta_{23}^e \approx 0.1$, together with a low leptoquark mass $M_{S_3} \approx 1 \text{ TeV}$, close to current LHC limits [7].

On the other hand, B_s mixing only occurs at one loop, via the (right) diagram in Fig.1, dominated by τ exchange, leading to the 2015 bound [7]

$$\frac{(\lambda_{s\tau} \lambda_{b\tau})^2}{16\pi^2 M_{S_3}^2} \approx \frac{y_\tau^4 V_{ts}^2}{16\pi^2 M_{S_3}^2} \leq \frac{1}{(140 \text{ TeV})^2} \rightarrow y_\tau^4 \leq 5.0 \left(\frac{M_{S_3}}{1 \text{ TeV}} \right)^2 \quad (2.8)$$

which is satisfied even for large $y_\tau \approx 1$ with $M_{S_3} \approx 1 \text{ TeV}$. However the stronger 2017 bound with scale of 770 TeV instead of 140 TeV implies a bound of $y_\tau^4 \leq 0.16$ for $M_{S_3} \approx 1 \text{ TeV}$ [7].

2.3 The Z' couplings

We now consider the couplings involving the Z' as discussed in [5]. Although the chiral fermions do not carry $U(1)'$ charges, the lower diagrams in Table 2 generate effective Z' couplings to chiral fermions, via the vector-like fourth family fermions which do carry $U(1)'$ charges (which are trivially anomaly free). The Z' couplings in the basis of Eq.2.1 are dominated by left-handed couplings to the third family [5],²

$$y_t^2 g' Z'_\mu Q_3^\dagger \gamma^\mu Q_3 + y_\tau^2 g' Z'_\mu L_3^\dagger \gamma^\mu L_3, \quad (2.9)$$

²Unlike the leptoquark case, there are also small Z' couplings to the right-handed fermions, in the basis of Eq.2.1, $\varepsilon_{ij}^\mu \varepsilon_{ji}^\mu g' Z'_\mu u_i^{c\dagger} \gamma^\mu u_j^c$, $\varepsilon_{ij}^d \varepsilon_{ji}^d g' Z'_\mu d_i^{c\dagger} \gamma^\mu d_j^c$, $\varepsilon_{ij}^e \varepsilon_{ji}^e g' Z'_\mu e_i^{c\dagger} \gamma^\mu e_j^c$, which are second order in the small Yukawa couplings. Thus, the small value of the Yukawa coupling of the charm quark implies that the c_R coupling to Z' is suppressed by $(m_c/m_t)^2 \sim 10^{-4}$ in this basis. The s_R coupling to Z' is similarly suppressed, so there there is a negligible contribution to $K_0 - \bar{K}_0$ mixing for $M_{Z'} \sim 1 \text{ TeV}$.

The Z' couplings in Eq.2.9 are analogous to the case of the third family leptoquark couplings in Eq.2.3, with no couplings to the first or second family in the basis of Eq.2.1. However, flavour changing couplings involving the quark doublets $Q_3 = (t, b)_L^T$, $Q_2 = (c, s)_L^T$, will be generated when the Yukawa matrices in Eq.2.1 are diagonalised,

$$y_t^2 g' Z'_\mu Q_3^\dagger \gamma^\mu Q_3 \rightarrow V_{ts} Z'_\mu Q_3^\dagger \gamma^\mu Q_2, \quad V_{ts}^2 Z'_\mu Q_2^\dagger \gamma^\mu Q_2, \quad \dots \rightarrow V_{ts} Z'_\mu b_L^\dagger \gamma^\mu s_L, \quad \dots \quad (2.10)$$

Similarly the operator $y_\tau^2 g' Z'_\mu L_3^\dagger \gamma^\mu L_3$ in Eq.2.9 leads to flavour changing couplings involving the lepton doublets $L_3 = (\nu_\tau, \tau)_L^T$, $L_2 = (\nu_\mu, \mu)_L^T$, controlled by a left-handed lepton mixing θ_{23}^e ,

$$\theta_{23}^e y_\tau^2 Z'_\mu L_3^\dagger \gamma^\mu L_2, \quad (\theta_{23}^e)^2 y_\tau^2 Z'_\mu L_2^\dagger \gamma^\mu L_2 \quad \dots \rightarrow \theta_{23}^e y_\tau^2 Z'_\mu \tau_L^\dagger \gamma^\mu \mu_L, \quad (\theta_{23}^e)^2 y_\tau^2 Z'_\mu \mu_L^\dagger \gamma^\mu \mu_L \quad (2.11)$$

where we have taken $y_t \approx g' \approx 1$. The couplings in Eqs.2.10, 2.11 control the Z' exchange diagrams in Fig.2 which contribute to $R_{K^{(*)}}$ (left), to B_s mixing (centre) and to $\tau \rightarrow \mu\mu\mu$ (right).

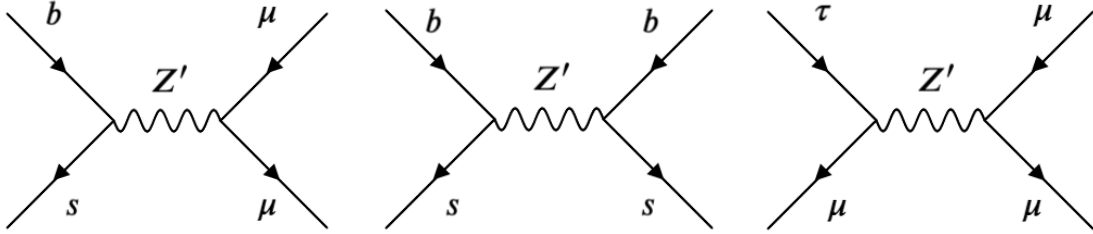


Figure 2: These Z' exchange diagrams contribute to $R_{K^{(*)}}$ (left), to B_s mixing (centre) and to $\tau \rightarrow \mu\mu\mu$ (right). The couplings are defined as $g_{bs} Z'_\mu b_L^\dagger \gamma^\mu s_L$, $g_{\mu\mu} Z'_\mu \mu_L^\dagger \gamma^\mu \mu_L$ and $g_{\tau\mu} Z'_\mu \tau_L^\dagger \gamma^\mu \mu_L$.

The Z' contributes to $R_{K^{(*)}}$ at tree-level, via the (left) diagram in Fig.2, where the requirement to explain the anomaly (ignoring the contribution from the leptoquark) is [5]

$$\frac{g_{\mu\mu} g_{bs}}{M_{Z'}^2} \approx \frac{y_\tau^2 (\theta_{23}^e)^2 V_{ts}}{M_{Z'}^2} \approx \frac{1.1}{(35 \text{ TeV})^2} \rightarrow y_\tau^2 (\theta_{23}^e)^2 \approx 2.2 \times 10^{-2} \left(\frac{M_{Z'}}{1 \text{ TeV}} \right)^2, \quad (2.12)$$

using $V_{ts} \approx 4.0 \times 10^{-2}$, which is analogous to the expression we obtained for the leptoquark in Eq.2.7. As before, this requires quite a large $y_\tau \approx 1$ (i.e. large $\tan\beta = \langle H_u \rangle / \langle H_d \rangle$) and a large mixing angle $\theta_{23}^e \approx 0.1$, together with a low mass $M_{Z'} \approx 1 \text{ TeV}$, close to current LHC limits [4].

Now B_s mixing is mediated by tree-level Z' exchange as in the (centre) diagram in Fig.2, leading to the 2015 bound [4],

$$\frac{g_{bs} g_{bs}}{M_{Z'}^2} \approx \frac{V_{ts}^2}{M_{Z'}^2} \leq \frac{1}{(140 \text{ TeV})^2} \rightarrow M_{Z'} \geq V_{ts} (140 \text{ TeV}) = 5.6 \text{ TeV} \quad (2.13)$$

However the stronger 2017 bound with scale of 770 TeV instead of 140 TeV implies a bound of $M_{Z'} \geq 31 \text{ TeV}$, which seems incompatible with the $R_{K^{(*)}}$ requirement in Eq.2.12.

Moreover $\tau \rightarrow \mu\mu\mu$ is mediated by tree-level Z' exchange as in the (right) diagram in Fig.2, leading to the bound [4],

$$\frac{g_{\tau\mu} g_{\mu\mu}}{M_{Z'}^2} \approx \frac{(\theta_{23}^e)^3 y_\tau^4}{M_{Z'}^2} \leq \frac{1}{(16 \text{ TeV})^2} \rightarrow y_\tau^4 (\theta_{23}^e)^3 \leq 4.0 \times 10^{-3} \left(\frac{M_{Z'}}{1 \text{ TeV}} \right)^2. \quad (2.14)$$

Writing $g_{\tau\mu} = g_{\mu\mu}/\theta_{23}^e$, the bounds on B_s mixing and $\tau \rightarrow \mu\mu\mu$ may be written as:

$$\frac{g_{bs}}{M_{Z'}} \leq \frac{1}{(140 \text{ TeV})}, \quad \frac{g_{\mu\mu}}{M_{Z'}} \leq \frac{(\theta_{23}^e)^{1/2}}{(16 \text{ TeV})} \quad (2.15)$$

which may be combined, leading to a bound³ on the contribution to $R_{K^{(*)}}$,

$$\frac{g_{\mu\mu}}{M_{Z'}} \frac{g_{bs}}{M_{Z'}} \leq \frac{(\theta_{23}^e)^{1/2}}{(140 \text{ TeV})(16 \text{ TeV})} = \frac{(\theta_{23}^e)^{1/2}}{(47 \text{ TeV})^2} \quad (2.16)$$

which is somewhat less than the $\frac{1.1}{(35 \text{ TeV})^2}$ required in Eq.2.12 to explain the anomaly. Moreover, the stronger 2017 bound with scale of 770 TeV instead of 140 TeV implies a bound of $\frac{(\theta_{23}^e)^{1/2}}{(111 \text{ TeV})^2}$, which is significantly less than the $\frac{1.1}{(35 \text{ TeV})^2}$ required to explain the anomaly.

3. Summary and Conclusion

In this talk we have explored the possibility that Higgs Yukawa couplings are related to the couplings of a new scalar triplet leptoquark or Z' , providing a predictive theory of flavour, including flavour changing, and flavour non-universality.

In particular, we have here combined the Z' model [5] and the leptoquark model [7], including also a vector-like fourth family of fermions, as a possible explanation of $R_{K^{(*)}}$. The idea of these models is that the Yukawa couplings are generated by the same physics that generates the Z' and leptoquark couplings, namely mixing with the vector-like fourth family. The combined model proposed here allows Z' and leptoquark contributions to be compared in the same framework.

In the combined model considered here, the leptoquark couplings in Eq.2.5 are given in terms of Yukawa couplings and mixing angles in Eq.2.6. We have seen that such a flavoured leptoquark can just about account for $R_{K^{(*)}}$, while satisfying the bound on B_s mixing, providing that the leptoquark mass is close to its current LHC bound, namely $M_{S_3} \approx 1 \text{ TeV}$, which is a clear prediction of the model, providing a target future LHC runs. However, as seen above, this also requires quite a large $y_\tau \approx 1$ and a large mixing angle $\theta_{23}^e \approx 0.1$, so the leptoquark-only explanation of $R_{K^{(*)}}$ is under some tension.

Unfortunately, the Z' couplings in Eqs. 2.10,2.11, are unable to account for $R_{K^{(*)}}$, while satisfying the bounds from B_s mixing and $\tau \rightarrow \mu\mu\mu$, as can be seen from the bound in Eq.2.16. However it is possible that other (lepton) Yukawa matrix structures may allow Z' exchange to account for $R_{K^{(*)}}$, as previously discussed [5].

There is an important distinction to be drawn between the leptoquark and Z' explanations of $R_{K^{(*)}}$, when linked to a theory of flavour. The leptoquark mass term $M_{S_3}^2 |S_3|^2$ respects $U(1)'$, and hence the leptoquark mass M_{S_3} is independent of the order parameter $\langle\phi\rangle$. As far as the leptoquark mass is concerned, the flavour breaking scale $\langle\phi\rangle$ may be anywhere from the Planck scale to the electroweak scale, providing that the ratios $\langle\phi\rangle/M_4$ which govern the Yukawa couplings are held fixed. By contrast, since the Z' mass is of order $\langle\phi\rangle$, a TeV scale Z' (as would be required to account for $R_{K^{(*)}}$) would require a theory of flavour near the electroweak scale!

³I am grateful to E.Perdomo for pointing out this bound.

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