

## Search for a stable six-quark state in $\Upsilon$ decays at *BABAR*

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Recent investigations have suggested that the six-quark combination  $uuddss$  could be a deeply bound state ( $S$ ) that has eluded detection so far, and a potential dark matter candidate. We report the first search for a stable, doubly strange six-quark state in  $\Upsilon \rightarrow S\bar{\Lambda}\bar{\Lambda}$  decays with the *BABAR* experiment. No signal is observed, and limits on the combined  $\Upsilon(2S, 3S) \rightarrow S\bar{\Lambda}\bar{\Lambda}$  branching fraction set stringent limits on the existence of such exotic particles.

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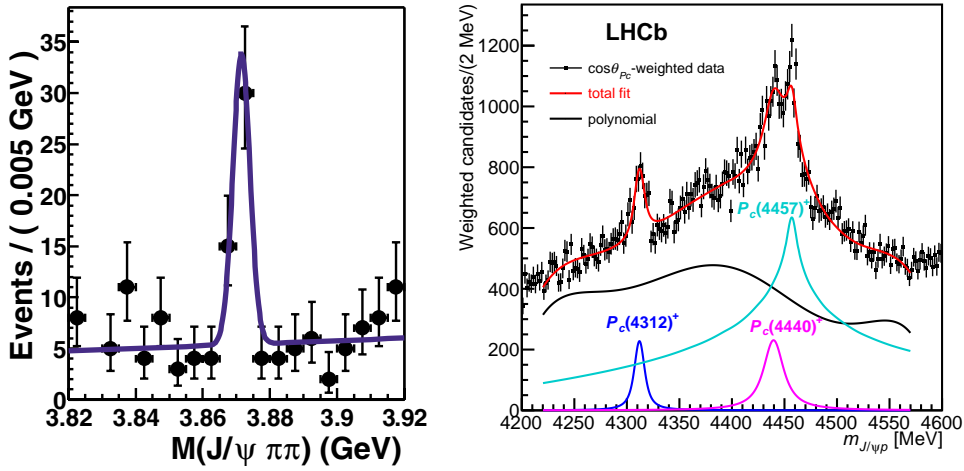
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\*Speaker.

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## 1. Introduction

In the traditional quark model, only mesons ( $q\bar{q}$ ) and baryons ( $qqq$ ) are predicted [1]. Other states such as ( $q\bar{q}q\bar{q}$ ), ( $q\bar{q}qq$ ), or ( $qqqqqq$ ) were not considered since those were not observed. In recent years, however, several experiments found states consistent with tetraquarks ( $q\bar{q}q\bar{q}$ ). For example, the Belle experiment first observed the  $X(3872)$ , a  $J^{PC} = 1^{++}$  state in  $B \rightarrow K\pi^+\pi^-J/\psi(1S)$  [2]. Figure 1 (left) shows the  $J/\psi\pi^+\pi^-$  invariant-mass spectrum, which reveals a prominent peak at 3872 MeV/c<sup>2</sup>. The state has exotic properties that differ from a conventional  $q\bar{q}$  state. The classification as a tetraquark state is the most likely option. The BES III experiment first observed the  $Z_c(3900)^+$  state [3] and Belle first observed the  $Z_c(4430)^+$  state, which have properties that are incompatible with a  $q\bar{q}$  assignment. These states are consistent with being tetraquark states as well. By now, the LHCb experiment observed three pentaquark states, the  $P_c(4312)$ , the  $P_c(4440)$  and the  $P_c(4457)$  [5]. They are visible in the  $J/\psi p$  invariant-mass spectrum displayed in Fig. 1 (right). Therefore, it is rather likely that also six-quark states may exist.



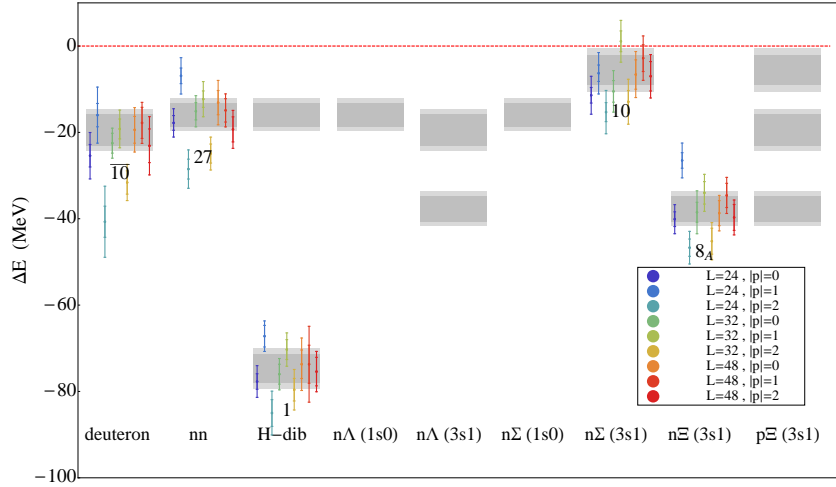
**Figure 1:** Left: The  $J/\psi\pi^+\pi^-$  invariant-mass spectrum observed by Belle showing the  $X(3872)$  exotic state. Right: The  $J/\psi p$  invariant-mass spectrum from LHCb showing three pentaquark states, the  $P_c(4412)^+$ ,  $P_c(4440)$  and  $P_c(4457)$  states [5].

In 1977, Jaffe proposed the H-dibaryon, a  $|udsuds\rangle$ , S-wave and flavor singlet state that is a loosely bound  $\Lambda\Lambda$  state [7]. The bag model predicted its mass to be  $m_H = 2150$  MeV/c<sup>2</sup>. If  $m_H < 2m_\Lambda$  the state is stable with respect to strong decays. Therefore, the H is expected to decay weakly, with a lifetime of  $10^{-10}$  s. Numerous searches for an H-dibaryon, however, did not find any signal.

In 2017, Farrar proposed a  $|uuddss\rangle$  six-quark state S that is different from the loosely bound H-dibaryon state at 2150 MeV predicted by Jaffe. The scalar state has charge zero, baryon number two, strangeness minus two, and should be produced in decays such as  $\Upsilon \rightarrow gluons \rightarrow S\bar{\Lambda}\bar{\Lambda}$  [9]. It is a very compact state with a radius of 0.1 – 0.4 fm. Recent Lattice QCD calculations indicate that it is a tightly bound  $\Lambda\Lambda$  state with a mass  $m_S < m_\Lambda + m_p + m_e = 2.0545$  GeV/c<sup>2</sup>. If  $m_S < 1.878$  GeV/c<sup>2</sup>, S is absolutely stable. It is a flavor singlet that is allowed by QCD with small couplings to mesons. Figure 2 shows the binding energy of various di-baryon systems calculated in lattice gauge theories [10]. Note that the singlet state is the most stable di-baryon state. The

$S$ -nucleon interactions are suppressed due to the tiny wave function overlap. Thus, neutron stars do not decay to  $S$ . Also, the decay  $nn \rightarrow S\pi^0$  is not observed, Searches of past experiments rule out  $m_S > 2 \text{ GeV}/c^2$ . However, the mass region below  $2 \text{ GeV}/c^2$  have not been explored.

The six-quark  $S$  state could be the astronomical dark matter (DM). If dark matter consists of a nearly equal number of  $u$ ,  $d$ ,  $s$  quarks, the formation rate is driven by a quark-gluon plasma transition to the hadronic phase. So DM models in this category include hexaquarks. Please note that hexaquark DM with a mass of  $1860\text{-}1880 \text{ MeV}/c^2$  can reproduce the ratio of DM to ordinary matter densities  $\Omega_{DM}/\Omega_b$  within 15%. In this scenario, the total baryon asymmetry in the universe would be at a level close to the observed value after including the dark-matter contribution. Please also note that a low-mass hexaquark is hard to distinguish kinematically from a neutron.



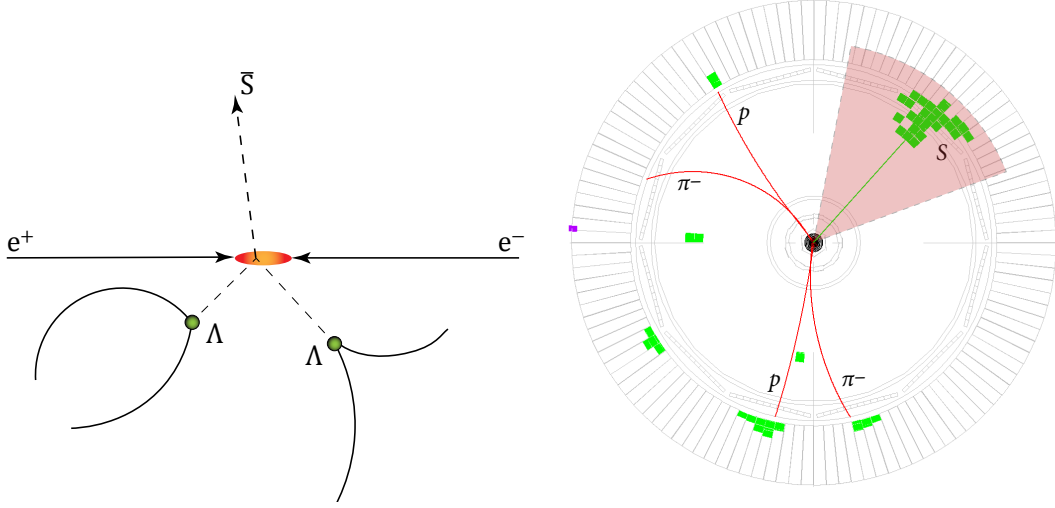
**Figure 2:** Binding energies of two-baryon systems calculated in lattice QCD. The grey-shaded regions denote statistical uncertainties while the colored error bars show statistical and systematic errors combined. The different colors show results for three lattice dimensions and different momenta [10].

## 2. Search Strategy

The *BABAR* experiment has searched for the hexaquark  $S$  in the process  $\Upsilon(2S, 3S) \rightarrow gluons \rightarrow S\bar{\Lambda}\bar{\Lambda}$  or  $\bar{S}\Lambda\Lambda$  performing a blind analysis of  $90 \times 10^6$   $\Upsilon(2S)$  decays and  $100 \times 10^6$   $\Upsilon(3S)$  decays. The  $\Upsilon(4S)$  data set of  $424.2 \text{ fb}^{-1}$  is used to evaluate the off-peak background since according to simulations the contribution of  $B$  meson decays to the final mass spectrum is negligible. The  $\bar{\Lambda}\bar{\Lambda}$  ( $\Lambda\Lambda$ ) system is fully reconstructed in the  $\bar{p}\pi^+\bar{p}\pi^+$  ( $p\pi^-p\pi^-$ ) decays. The  $\Lambda \rightarrow p\pi^-$  decay has a branching fraction of  $\mathcal{B}(\Lambda \rightarrow p\pi^-) = 0.64$ . With the fully reconstructed  $\bar{\Lambda}s$  the recoil mass  $m_{rec}^2 = (p_\Upsilon - p_{\bar{\Lambda}} - p_{\bar{\Lambda}})^2$  is calculated. Figure 3 (left) shows the topology of the process  $e^+e^- \rightarrow \Upsilon(2S, 3S) \rightarrow gluons \rightarrow S\bar{\Lambda}\bar{\Lambda}$ . The  $S$  lies in the recoil of the  $\bar{\Lambda}\bar{\Lambda}$  system.

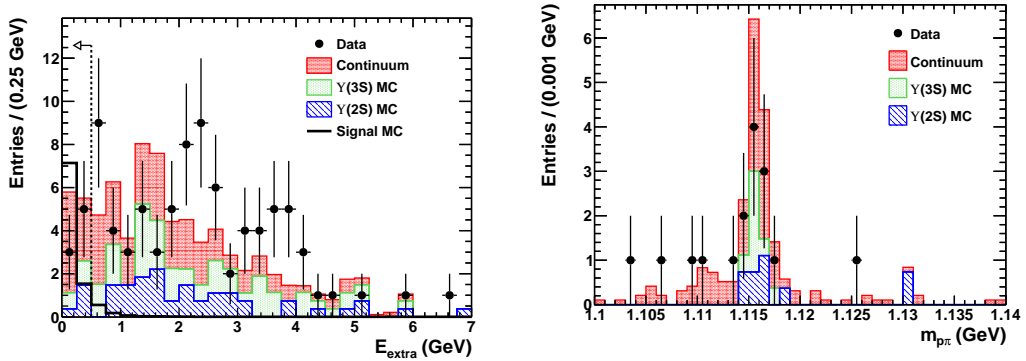
We select events that have four charged tracks. One additional track is allowed that does not come from the interaction region having a distance of closest approach  $DOCA > 5 \text{ cm}$ . This accounts for particles that are produced in secondary interactions with the detector material. We

apply loose particle identification criteria to select  $p$  or  $\bar{p}$ . We reconstruct  $\bar{\Lambda}\bar{\Lambda}$  or  $\Lambda\Lambda$  using the  $\bar{p}\pi^+$  or  $p\pi^-$  decay. For each  $\bar{\Lambda}(\Lambda)$  we require a flight distance significance of  $|\vec{r}_\Lambda|/\sigma_{r_\Lambda} > 5$  where  $r_\Lambda$  is the flight distance vector. The  $\bar{\Lambda}(\Lambda)$  have to point back to interaction region,  $\vec{r}_\Lambda \cdot \vec{p}_\Lambda / (|\vec{r}_\Lambda| |\vec{p}_\Lambda|) > 0.9$ . To extract the signal we examine the extra neutral energy  $E_{extra}$ , which is the energy of all neutral clusters in electromagnetic calorimeter except for a cone around the  $S$ . Figure 3 (right) shows an event display of a simulated signal event. The pink cone shows the region that is not included in the determination of  $E_{extra}$ . For signal we require  $E_{extra} < 500$  MeV. We use the sample  $E_{extra} > 500$  MeV for validation.



**Figure 3:** Left: Topology of the process  $e^+e^- \rightarrow Y(2S, 3S) \rightarrow \text{gluons} \rightarrow S\bar{\Lambda}\Lambda$ . Right: Event display of a simulated signal event. Clusters lying in the pink cone are not included in the  $E_{extra}$  calculation.

Figure 4 (left) shows the  $E_{extra}$  distribution after preselection. We see 92 events of which 8 events satisfy  $E_{extra} < 500$  MeV. The  $p\pi$  invariant mass shows a true  $\Lambda$  signal as depicted in Fig. 4 (right). After performing a kinematic fit of each  $\Lambda$  candidate by constraining the mass to the nominal  $\Lambda$  mass and requiring a common point in the beam spot leaves four candidates.



**Figure 4:** Left: The distribution of extra energy in the calorimeter  $E_{extra}$  after preselection. Right: The  $p\pi$  invariant mass of all candidates that satisfy  $E_{extra} < 500$  MeV/ $c^2$ .

**Table 1:** Systematic uncertainties.

Source	Systematic error
$S$ angular distribution modeling	5 – 8%
$S$ particle type modeling	8 – 11%
$\Lambda$ reconstruction	4% per $\Lambda$
Monte Carlo statistics	2%
$\Lambda$ branching fraction	1.6%
proton particle identification	1% per $p$
Number of $\Upsilon(2S, 3S)$	0.6%

### 3. Efficiency and Backgrounds

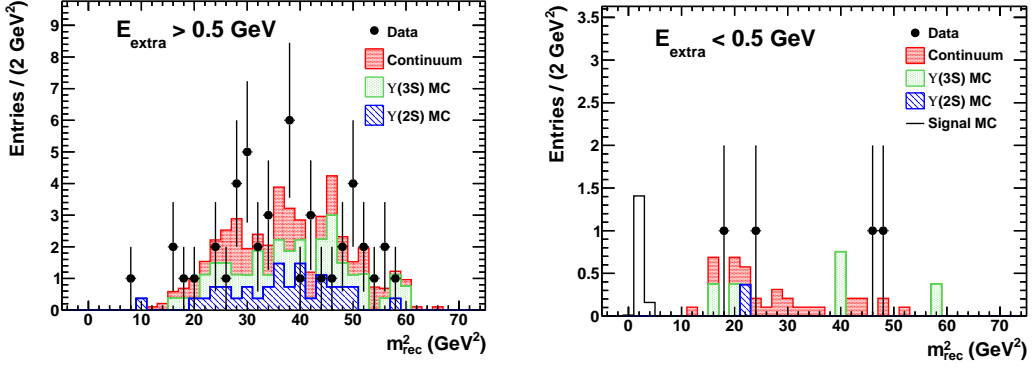
For simulation of the signal we use dedicated signal Monte Carlo samples that were generated both with the decay amplitude provided by Farrar [11] and with phase space. We model the hexaquark  $S$  as a neutron or as a neutrino that has no interaction with the detector material. The efficiency including  $\mathcal{B}(\lambda \rightarrow p\pi^-)^2$  varies from 7.2% at threshold to 8.2% near 2 GeV/c<sup>2</sup> and is mainly driven by the geometric acceptance. The resolution of the recoil mass is 100 MeV/c<sup>2</sup>. The background originates from  $q\bar{q}$  continuum with  $q = u, d, s, c$  or from  $\Upsilon(2S)$  and  $\Upsilon(3S)$  decays. We use  $\Upsilon(4S)$  decays for  $q\bar{q}$  continuum determination since the signal contribution is negligible. We scale the  $\Upsilon(2S)$  and  $\Upsilon(3S)$  Monte Carlo samples so that the Monte Carlo and  $q\bar{q}$  continuum matches the  $E_{extra}$  sideband. A residual background consists of  $\bar{\Lambda}\bar{\Lambda}(\Lambda\Lambda)X$  events in which the  $\bar{\Lambda}(\Lambda)$  decays to  $\bar{n}(n)\pi^0$ . This background may pass or fail the  $E_{extra}$  selection.

### 4. Systematic Uncertainties

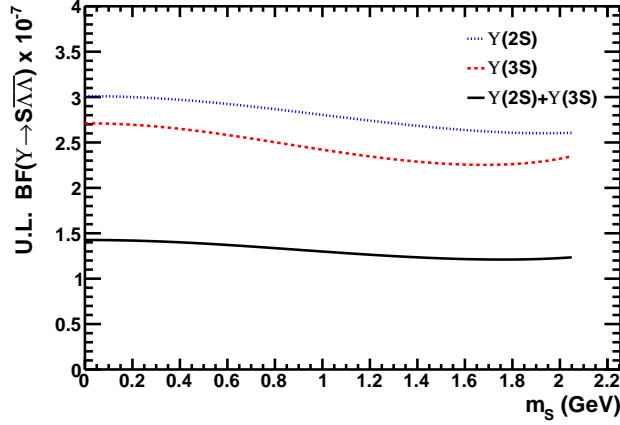
Table 1 summarizes the different types of systematic uncertainties. The largest effects come from modeling the hexaquark production amplitude and the angular distribution. The total systematic error ranges from 12.8% to 16.1%.

### 5. Validation and Results

Figure 5 (left) shows the distribution of the recoil mass  $m_{rec}$  squared for the validation sample for which  $E_{extra} > 500$  MeV/c<sup>2</sup>. In the  $E_{extra}$  sideband we observe zero background events in the  $m_{rec}$  signal region. Figure 5 (right) shows  $m_{rec}$  squared for  $E_{extra} < 500$  MeV/c<sup>2</sup> in which we see no events in the signal region. The four candidates populate the high mass region. To illustrate how a signal would look like, we performed a simulation of  $S$  with a mass of 1.6 GeV/c<sup>2</sup> and a branching fraction of  $\mathcal{B}(\Upsilon(nS) \rightarrow S\bar{\Lambda}\bar{\Lambda}) = 10^{-7}$ . We see no evidence for hexaquarks in the decays  $\Upsilon(2S, 3S) \rightarrow S\bar{\Lambda}\bar{\Lambda}$ . We use the profile likelihood method to set branching fraction upper limits at 90% confidence level in the mass range 0.0-2.05 GeV including systematic errors. Figure 6 shows the branching fraction upper limits at 90% confidence level as a function of the  $S$  mass. The upper limit on the branching fraction at 90% confidence level is  $\mathcal{B}(\Upsilon \rightarrow S\bar{\Lambda}\bar{\Lambda}) < 1.4 \times 10^{-7}$  at low masses falling off to  $\mathcal{B}(\Upsilon \rightarrow S\bar{\Lambda}\bar{\Lambda}) < 1.2 \times 10^{-7}$  at high masses.



**Figure 5:** Left: Distribution of the recoil mass for all candidate with  $E_{extra} > 500 \text{ MeV}/c^2$ . Right: Distribution of the recoil mass for signal candidate with  $E_{extra} < 500 \text{ MeV}/c^2$ .



**Figure 6:** Branching fraction upper limits at 90% confidence level as a function of  $m_S$  for  $\Upsilon(2S) \rightarrow S\bar{\Lambda}\bar{\Lambda}$  (blue dotted curve), for  $\Upsilon(3S) \rightarrow S\bar{\Lambda}\bar{\Lambda}$  (red dashed curve) and for both samples combined (black solid line).

## 6. Conclusion

A tightly bound  $S = |uudds\rangle$  state may be more stable than previously predicted. If  $m_S < m_\Lambda + m_p + m_e = 2.0545 \text{ GeV}/c^2$ , it may be stable even on cosmological time scales. If it exists, it is a good candidate for dark matter. It is not excluded by searches for the  $H$ -dibaryon. BABAR has searched for the hexaquark  $S$  in  $\Upsilon(2S)$  and  $\Upsilon(3S)$  decays in the recoil against  $\bar{\Lambda}\bar{\Lambda}$  using a data sample of 200 million  $\Upsilon(2S)$  and  $\Upsilon(3S)$  events. No evidence is found in  $\Upsilon(nS)$  decays for a stable hexaquark state. We see no background events in the signal region and set a stringent branching fraction upper limit of  $\mathcal{B}(\Upsilon \rightarrow S\bar{\Lambda}\bar{\Lambda}) < (1.2 - 1.4) \times 10^{-7}$  at 90% confidence level for  $m_S < 2.05 \text{ GeV}$ .

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