

# The absolute maximum and detailed phenomenology of the muon magnetic moment in the 2HDM

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**Adriano Cherchiglia**

*Universidade Federal do ABC - Centro de Ciências Naturais e Humanas, Santo André - Brazil*

**Dominik Stöckinger**

*Institut für Kern- und Teilchenphysik, TU Dresden, 01069 Dresden, Germany*

**Hyejung Stöckinger-Kim**<sup>\*†</sup>

*Institut für Kern- und Teilchenphysik, TU Dresden, 01069 Dresden, Germany*

*E-mail: [hyejung.stoeckinger-kim@tu-dresden.de](mailto:hyejung.stoeckinger-kim@tu-dresden.de)*

We present the muon magnetic moment  $g - 2$  in the flavour-aligned 2HDM evaluated by employing the recent result of full two-loop computation and making comprehensive use of experimental constraints from Higgs and flavour physics and characterize the parameter regions possible to explain the current  $3\sigma$  deviation. We particularly focus on the light CP-odd neutral Higgs boson  $A$  and present the maximum possible Yukawa couplings to leptons and quarks of a light  $A$  allowed by the LHC and  $B$ -physics results, which can enhance  $a_\mu^{2\text{HDM}}$  in this mass region. As a result we find an overall maximum of  $45 \times 10^{10}$  for  $a_\mu^{2\text{HDM}}$  in the parameter region  $20 < M_A < 100$  GeV.

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<sup>\*</sup>Speaker.

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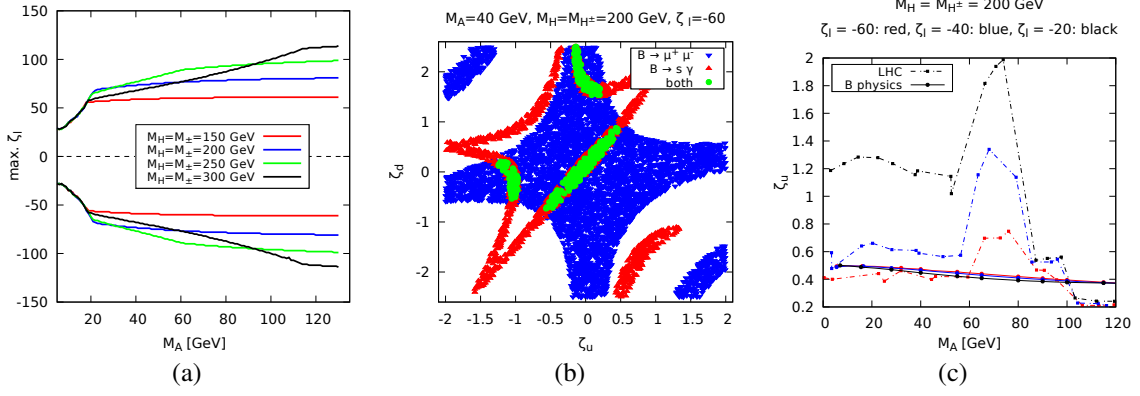


Figure 1

## 1. Introduction

The present proceedings are a review of the detailed numerical analysis of the muon magnetic moment  $g - 2$  in the two-Higgs doublet model (2HDM) in Ref. [1], which is obtained by using the complete two-loop correction results in Ref. [2].

The discrepancy in the muon magnetic moment  $g - 2$  between the experimental measurement [3] and the Standard Model (SM) predictions evaluated from the most recent studies [4–6] amounts to

$$a_\mu^{\text{Exp.}} - a_\mu^{\text{SM}} = (28.1 \pm 6.3^{\text{Exp.}} \pm 3.6^{\text{Th}}) \times 10^{-10}. \quad (1.1)$$

A substantial increase in the accuracy is expected in the further measurements at Fermilab and J-PARC. This persisting  $3\text{--}4\sigma$  deviation motivates new physics (NP) scenarios beyond the SM. Typically the NP contributions to the muon  $g - 2$  is suppressed by heavy NP masses  $\sim (m_\mu^2/M_{\text{NP}}^2)$ . Therefore, a NP scenario with a very high  $M_{\text{NP}}$  scale is inappropriate to explain the discrepancy in Eq. 1.1.

The 2HDM is a minimal extension to the SM and includes four physical Higgs masses  $M_h, M_H, M_A$  and  $M_{H^\pm}$ . The two neutral CP-even Higgs mass eigenstates  $h$  and  $H$  are combined states of the two scalar doublets with mixing angle  $\sin(\beta - \alpha)$ . When  $\sin(\beta - \alpha) = 1$  the SM-limit is reached and hence,  $h$  becomes an SM-like Higgs boson  $h_{\text{SM}}$ . The 2HDM muon  $g - 2$  contribution  $a_\mu^{2\text{HDM}}$  is obtained from the additional Higgs bosons:  $A, H, H^\pm$ .  $Z_2$  symmetry permits four different Yukawa coupling scenarios: the usual type I, II, X and Y. In the more general flavour-aligned 2HDM (A2HDM) [7] the Yukawa couplings are proportional to the Yukawa parameters  $\zeta_{l,u,d}$ .

Here we concentrate on three questions : (a) What are the constraints on the 2HDM parameters relevant for  $a_\mu$ ? (b) What are the parameter regions to explain the current deviation in  $a_\mu$ ? (c) What is the overall maximum possible value of  $a_\mu$  in the 2HDM?

## 2. The 2HDM contributions and constraints on the parameters

As the one-loop contributions are suppressed by higher order of muon mass  $\sim \mathcal{O}(m_\mu^4)$  through the Yukawa couplings the leading contributions to  $a_\mu^{2\text{HDM}}$  come from the Barr-Zee type two-loop

diagrams, where the muon line is coupled with one gauge boson and one Higgs boson with either fermions or bosons in the Barr-Zee loop. The leading fermion loop corrections are from the Barr-Zee  $\tau$ - or  $t$ -loop corrections. The following semi-numerical expressions for the leading fermionic two-loop and bosonic two-loop contributions are useful approximations to estimate the contributions for light  $M_A$ :

$$a_\mu^{\tau\text{-loop, 2HDM}} \simeq \left( \frac{\zeta_l}{100} \right)^2 \left\{ \frac{8 + 4\hat{x}_{M_A}^2 + 2\ln(\hat{x}_{M_A})}{\hat{x}_{M_A}^2} \right\}, \quad (2.1)$$

$$a_\mu^{t\text{-loop, 2HDM}} \simeq \left( \frac{-\zeta_l \zeta_u}{100} \right) \left\{ 54 - 14\ln(\hat{x}_{M_A}) - 15\ln(\hat{x}_{M_H}) \right\}, \quad (2.2)$$

$$|a_\mu^{B, 2HDM}| \simeq \rho |C_{HH^+H^-}/\text{GeV}| |\zeta_l| \times 10^{-15}, \quad (2.3)$$

where  $\rho = 6, 3, 2, 1$  for  $M_H = M_{H^\pm} = 150, 200, 250, 300 \text{ GeV}$  respectively.

The  $\tau$ -loop correction is enhanced by  $\zeta_l^2$  and the  $t$ -loop correction by  $\zeta_l \zeta_u$ . Thus the 2HDM fermion loop contribution  $a_\mu^{F, 2HDM}$  depends on the Yukawa parameters  $\zeta_l$  and  $\zeta_u$  as well as the Higgs boson masses. The  $t$ -loop correction becomes positive when we set the signs of  $\zeta_l$  and  $\zeta_u$  opposite to each other. In the numerical analysis we set  $\zeta_l$  negative and  $\zeta_u$  positive. Eq. 2.3 shows that the bosonic contributions are enhanced by the triple Higgs coupling constant  $C_{HH^+H^-}$  and are proportional to  $\zeta_l$ . From Eqs. 2.1– 2.3 we find that  $\zeta_l$ ,  $\zeta_u$  and  $M_A$  are the determining parameters for  $a_\mu^{2HDM}$ .

It is necessary to investigate the allowed  $\zeta_l$  and  $\zeta_u$  for given Higgs boson mass points to analyse  $a_\mu^{2HDM}$ .  $\zeta_l$  is constrained by  $\tau$ -decay, leptonic  $Z$ -decay and  $ee \rightarrow \tau\tau A$  searches at LEP. These experiments set upper bounds on  $\zeta_l$ . As the decay rates in the 2HDM are enhanced by  $\zeta_l$ , large  $\zeta_l$  leads to disagreement with experimental observations. Fig. 1a shows the upper bounds on  $\zeta_l$  for different Higgs boson mass values. For  $20 < M_A < 120 \text{ GeV}$  and  $150 < M_H (= M_{H^\pm}) < 300 \text{ GeV}$  we obtain  $|\zeta_l| < 60$ .

$\zeta_u$  gains constraints from  $B$ -decay channels ( $b \rightarrow s\gamma$  and  $B_s \rightarrow \mu\mu$ ) as well as from the LHC Higgs searches ( $gg \rightarrow A \rightarrow \tau\tau$  or  $gg \rightarrow H \rightarrow \tau\tau$ ). Fig. 1b shows the allowed  $\zeta_u$  and  $\zeta_d$  regions by  $B$ -decays. The green space indicates the parameter range allowed by both decay modes. It shows that  $\zeta_u$  is more restricted compared to  $\zeta_d$ .  $\zeta_u$  is also constrained by LHC Higgs searches. Large  $\zeta_u$  produces abundant intermediate Higgs  $H$  and consequently results in excessive  $\tau$  final states. Fig. 1c shows  $\zeta_u$  upper bounds allowed by  $B$ -decays and LHC. Depending on the Higgs boson masses and  $\zeta_l$ , the upper bounds on  $\zeta_u$  are determined by  $B$ -physics or by LHC results. The overall combined upper bound of  $\zeta_u$  lies between 0.3 and 0.6.

The LHC upper limit on  $\zeta_u$  is also related to the triple Higgs coupling constant  $C_{HAA}$ . Large  $C_{HAA}$  which is strongly correlated with  $C_{HH^+H^-}$  enhances the decay process  $H \rightarrow AA$ . Thus the final  $\tau$  states are regulated by either  $\zeta_u$  or  $C_{HH^+H^-}$ . Fig. 2a shows the proportional relation between  $C_{HH^+H^-}$  and the possible maximum of  $\zeta_u$ . It also shows the upper limit of  $C_{HH^+H^-}$ , which is constrained by theoretical and electro-weak constraints. The upper limit of  $C_{HH^+H^-}$  determines the maximum of the bosonic contributions  $a_\mu^{B, 2HDM}$  along with  $\zeta_l$ .

### 3. The overall maximum of the muon $g - 2$ and conclusion

Figs. 2b and 2c show the possible range of  $a_\mu^{2HDM}$  for different  $\zeta_l$  and  $M_H = M_{H^\pm}$ . The yellow

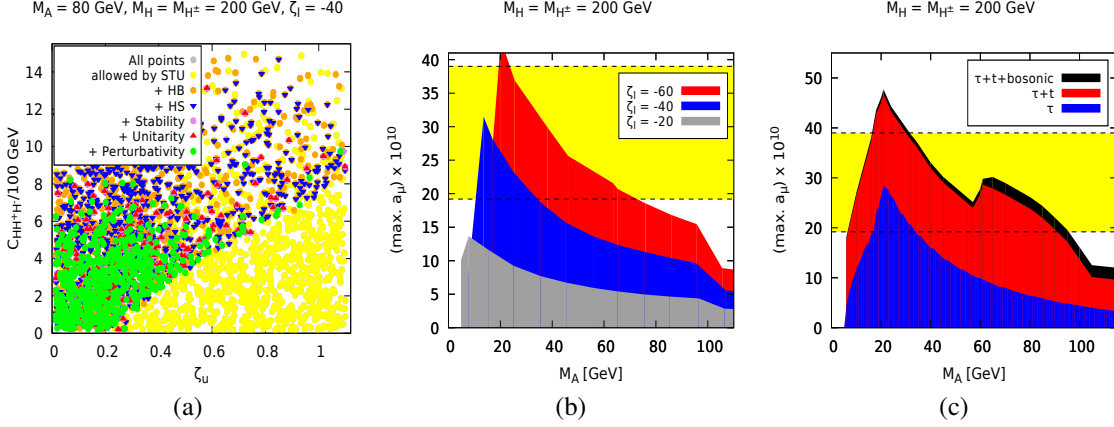


Figure 2

band indicates the current discrepancy in the muon  $g - 2$  in Eq. 1.1. The plot in Fig. 2b shows  $a_\mu^{2\text{HDM}}$  for different  $\zeta_l$ . For fixed  $M_A$  and  $\zeta_l$  the maximum of  $\zeta_u$  obtained in Fig. 1c is adopted. We need  $|\zeta_l| > 30$  to explain the discrepancy as we cannot find any  $M_A$  points to lie in the yellow band for  $\zeta_l = -20$  (the gray region). Fig. 2c shows the overall maximum of  $a_\mu^{2\text{HDM}}$  in the 2HDM. The allowed maxima of  $\zeta_l$  and  $\zeta_u$  for given Higgs masses are used to evaluate the possible maximum of  $a_\mu^{2\text{HDM}}$ . The blue space is only from the  $\tau$ -loop, the red space from adding the  $t$ -loop. The black space indicates the bosonic corrections. We observe that the maximum of  $a_\mu^{2\text{HDM}}$  reaches up to  $\sim 45 \times 10^{-10}$  around  $M_A = 20 \text{ GeV}$  and that it is possible to explain the discrepancy at low mass scales  $20 < M_A < 100 \text{ GeV}$  in the 2HDM in contrast to the Minimal Supersymmetric SM (MSSM), where the typical scales are  $M_{\text{NP}} \sim 500 \text{ GeV}$  or  $M_{\text{NP}} \sim 1 \text{ TeV}$  for the scenario with  $\tan \beta \rightarrow \infty$  [8]. This result further motivates searches of low scale pseudoscalar Higgs bosons at the LHC.

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