

# Study of Charmless Hadronic $B$ Decays and Rare $D$ Decays at Belle

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We present the summary of recent studies of  $B^+ \rightarrow K^+ K^- \pi^+$  and  $B^0 \rightarrow \pi^0 \pi^0$  charmless  $B$  decays,  $D^+ \rightarrow \pi^+ \pi^0$  rare  $D$  decay and the first search for  $D^0$  to *invisible final states* using a full data sample ( $\sim 1 \text{ ab}^{-1}$ ) of the Belle experiment at the KEKB asymmetric-energy  $e^+ e^-$  collider.

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## 1. Introduction

Rare  $B$  and  $D$  meson decays provide a powerful probe to search for physics beyond the standard model (SM). Observation of any significant deviation from the SM will be clear evidence for new physics (NP) beyond the SM. Here we present direct  $CP$  asymmetry ( $\mathcal{A}_{CP} = \frac{|\bar{A}_{B \rightarrow \bar{f}}/A_{B \rightarrow f}|^2 - 1}{|\bar{A}_{B \rightarrow \bar{f}}/A_{B \rightarrow f}|^2 + 1}$ , where  $A_{B \rightarrow f}$  and  $\bar{A}_{\bar{B} \rightarrow \bar{f}}$  are instantaneous decay amplitudes) and branching fraction ( $\mathcal{B}$ ) measurements of  $B^+ \rightarrow K^+ K^- \pi^+$  and  $B^0 \rightarrow \pi^0 \pi^0$  charmless hadronic  $B$  decays; a search for  $CP$  violation in  $D^+ \rightarrow \pi^+ \pi^0$  rare  $D$  decay; and the first search for  $D^0$  to *invisible final states* at the Belle experiment. The results are based on the full data sample collected by the Belle detector at KEKB.

## 2. Measurement of Branching Fraction and Direct $CP$ Asymmetry in

### $B^+ \rightarrow K^+ K^- \pi^+$ Decay

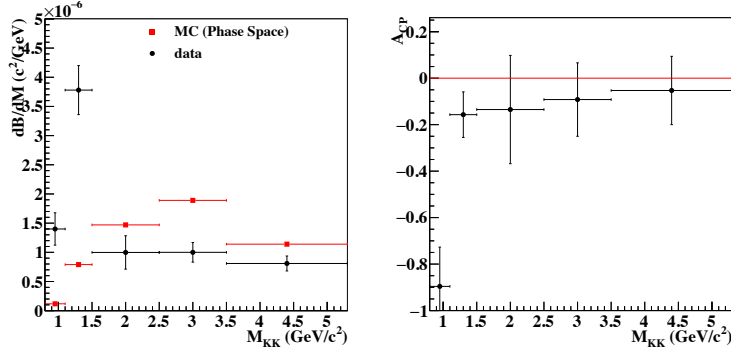
The decays of  $B^+ \rightarrow K^+ K^- \pi^+$  are dominated by the Cabibbo-suppressed  $b \rightarrow u$  tree and  $b \rightarrow d$  loop transitions. Interference between tree and loop processes with similar amplitudes can cause large  $CP$  asymmetries. *BABAR* measured the  $\mathcal{B}$  of  $B^+ \rightarrow K^+ K^- \pi^+$  decay as  $[5.0 \pm 0.5(stat) \pm 0.5(syst)] \times 10^{-6}$  and  $\mathcal{A}_{CP}$  which is consistent with zero [1]. *BABAR* also reported a broad peaking structure near  $1.5 \text{ GeV}/c^2$  in the  $K^+ K^-$  invariant mass distribution. Later, LHCb observed a nonzero inclusive  $CP$  asymmetry of  $-0.123 \pm 0.017(stat) \pm 0.012(syst) \pm 0.007$  (where the third uncertainty is due to  $CP$  asymmetry of the  $B^+ \rightarrow J/\psi K^\pm$ ) and a large unquantified local  $CP$  asymmetry in the same  $K^+ K^-$  invariant mass ( $M_{K^+ K^-}$ ) region [2, 3]. This analysis aims to quantify the  $\mathcal{B}$  and  $CP$  asymmetry as a function of  $M_{K^+ K^-}$  using a data sample that contains  $772 \times 10^6 B\bar{B}$  pairs collected at the  $\Upsilon(4S)$  resonance with the Belle detector.

Two standard kinematic variables are used to identify  $B$  meson candidates: the beam-energy-constrained mass,  $M_{bc} = \sqrt{E_{beam}^2/c^4 - |p_B/c|^2}$  and the energy difference,  $\Delta E = E_B - E_{beam}$ , where  $E_{beam}$  is the beam energy and  $E_B$  and  $p_B$  are the energy and momentum of the  $B$  candidate in the center-of-mass reference frame. The primary background is continuum  $e^+ e^- \rightarrow q\bar{q}$  ( $q = u, d, s, c$ ) events. To eliminate this type of events from signal, a neural network [4] is employed by combining variables based on the event topology. A requirement on the neural network output  $\mathcal{C}_{NN} < 0.88$  suppresses 99% of the continuum events while keeping 48% of the signal. The charm veto is applied to reject charm  $B$  decays having the same final-state particles. There are a few charmless  $B$  decays contributing to the  $M_{bc}$  signal region with corresponding  $\Delta E$  peak due to  $K-\pi$  misidentification:  $B^+ \rightarrow K^+ K^- K^+$ ,  $B^+ \rightarrow K^+ \pi^- \pi^+$  and their intermediate resonant modes. Events which remain after removing peaking backgrounds are referred to as ‘rare combinatorial’ background.

A two-dimensional unbinned maximum-likelihood (ML) fit to  $M_{bc}$  and  $\Delta E$  distributions in bins of  $M_{K^+ K^-}$  is performed to determine the signal yield and  $\mathcal{A}_{CP}$ . The measured inclusive branching fraction and direct  $CP$  asymmetry are [5]

$$\mathcal{B}(B^+ \rightarrow K^+ K^- \pi^+) = (5.38 \pm 0.40 \pm 0.35) \times 10^{-6} \quad \text{and} \quad \mathcal{A}_{CP} = -0.170 \pm 0.073 \pm 0.017 .$$

Figure 1 shows quantified differential  $\mathcal{B}$  and  $\mathcal{A}_{CP}$  as a function of  $M_{K^+ K^-}$ . A strong evidence of large  $CP$  asymmetry with  $4.8 \sigma$  significance is found in the region where  $M_{K^+ K^-}$  is smaller than  $1.1 \text{ GeV}/c^2$ , consistent with the *BABAR* and LHCb measurements.



**Figure 1:** Measured differential  $\mathcal{B}$  (left), and direct  $CP$  (right) as a function of  $M_{K^+K^-}$ . Each point is obtained from a two-dimensional fit with systematic uncertainty included. Red squares with error bars on the left figure indicate the expected signal distributions in a three-body phase-space MC sample. Note that the phase-space hypothesis is rescaled to the total observed  $B^+ \rightarrow K^+K^-\pi^+$  signal yield.

### 3. Measurement of Branching Fraction and Direct $CP$ Asymmetry in $B^0 \rightarrow \pi^0\pi^0$ Decay

The CKM angle  $\phi_2$  can be determined by measuring the time-dependent  $CP$  violation in  $B^0 \rightarrow \pi^+\pi^-$  decay. Possible penguin contributions can give rise to direct  $CP$  violation,  $\mathcal{A}_{CP} \neq 0$ , and potentially modify the asymmetry by introducing  $\Delta\phi_2$  term in the mixing-induced  $CP$  violation parameter,  $S_{CP} = \sqrt{1 - A_{CP}^2} \sin[2(\phi_2 - \Delta\phi_2)]$ . To extract  $\Delta\phi_2$  information, an isospin analysis of the entire  $B \rightarrow \pi\pi$  system is needed [6]. The branching fraction and  $\mathcal{A}_{CP}$  for  $B^0 \rightarrow \pi^0\pi^0$  are the least well determined among the  $B \rightarrow \pi\pi$  decays. *BABAR* (with 467 million  $B\bar{B}$  events) and Belle (with 275 million  $B\bar{B}$  events) report the  $\mathcal{B}$  of  $1.8 \times 10^{-6}$  and  $2.3 \times 10^{-6}$ , respectively [7, 8]. On the other hand, the theoretical prediction is below  $1 \times 10^{-6}$  [9, 10]. This analysis measures  $\mathcal{B}$  and  $\mathcal{A}_{CP}$  in  $B^0 \rightarrow \pi^0\pi^0$  based on the full Belle data sample that contains 752 million  $B\bar{B}$  pairs.

The  $b$ -flavor of the other  $B$  meson,  $B_{tag}^0$ , is used to extract the  $\mathcal{A}_{CP}$  and the effect of  $B\bar{B}$  mixing is corrected. To distinguish signal from background, two kinematic variables,  $M_{bc}$  and  $\Delta E$ , are deployed. Event shape variables are combined in the Fisher discriminant ( $T_c$ ) to suppress continuum background. The signal yield and  $\mathcal{A}_{CP}$  are obtained using an unbinned extended maximum-likelihood fit to  $M_{bc}$ ,  $\Delta E$  and  $T_c$ . The fit projection plots of  $\Delta E$ ,  $M_{bc}$ , and  $T_c$  are shown in Figure 2. The fit yields  $217 \pm 32$  signal candidates. The  $\mathcal{B}$  and  $\mathcal{A}_{CP}$  are determined as

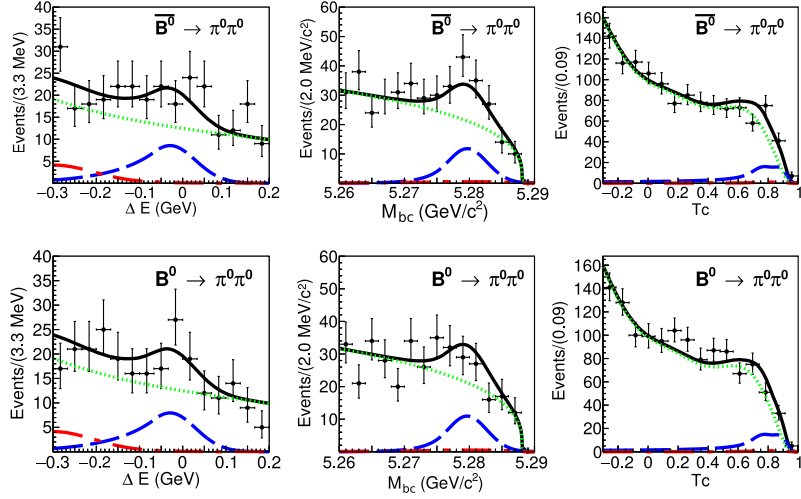
$$\mathcal{B}(B^0 \rightarrow \pi^0\pi^0) = (1.31 \pm 0.19 \pm 0.19) \times 10^{-6} \text{ and } \mathcal{A}_{CP} = -0.14 \pm 0.36 \pm 0.10.$$

The signal significance, including the systematic uncertainty, is 6.4 standard deviations. The measured  $\mathcal{B}$  is consistent with the *BABAR* measurement and supersedes the previous Belle one [8].

All Belle  $B \rightarrow \pi\pi$  measurements [11, 12, 13] are combined to exclude  $\phi_2$  from  $15.5^\circ < \phi_2 < 75.0^\circ$  at 95% confidence level [11].

### 4. Search for $CP$ violation in $D^+ \rightarrow \pi^+\pi^0$

In contrast to strange and bottom sectors, the SM predictions of  $CP$  asymmetry in the charm sector are much smaller. The singly Cabibbo-suppressed  $D^+ \rightarrow \pi^+\pi^0$  decay is an excellent can-



**Figure 2:** Projections of the fit results onto  $\Delta E$  (left),  $M_{bc}$  (middle), and  $T_c$  (right) in the signal-enhanced region:  $5.275 \text{ GeV}/c^2 < M_{bc} < 5.285 \text{ GeV}/c^2$ ,  $-0.15 \text{ GeV} < \Delta E < 0.05 \text{ GeV}$ , and  $T_c > 0.7$ . Data are points with error bars; the full fit results are shown by the solid black curves. Contributions from signal, continuum  $q\bar{q}$ , combined  $\rho \pi$ , and other rare  $B$  decays are shown by the dashed blue, dotted green, and dash-dotted red curves, respectively. The top (bottom) row panels are for events with positive (negative)  $b$ -flavor charge ( $q$ ) of  $B_{tag}^0$ .

didate to search for  $CP$  violation in the charm system. In addition to a search for  $CP$  violation in  $D^+ \rightarrow \pi^+ \pi^0$ , Grossman, Kagan and Zupan suggest verifying a sum rule relating individual asymmetries of the three isospin-related  $D \rightarrow \pi\pi$  decays [14] to probe potential NP. The  $CP$  asymmetry of  $D^+ \rightarrow \pi^+ \pi^0$  decay measured by CLEO ( $\mathcal{A}_{CP}(D^+ \rightarrow \pi^+ \pi^0) = (2.9 \pm 2.9 \pm 0.3)\%$ ) has high statistical uncertainty and therefore limits the precision with which the sum rule can be tested [15].

Here we present the measurement of  $\mathcal{A}_{CP}$  for the  $D^+ \rightarrow \pi^+ \pi^0$  decay based on  $921 \text{ fb}^{-1}$  of Belle data. A sample of  $D^+$  mesons tagged by  $D^{*+} \rightarrow D^+ \pi^0$  decays (*tagged* sample) and another not tagged by  $D^{*+}$  decays (*untagged* sample) are considered for the  $\mathcal{A}_{CP}$  measurement. The decay  $D^+ \rightarrow K_S^0 \pi^+$  is used as a normalization channel ( $\mathcal{A}_{CP}^{K\pi} = (0.363 \pm 0.094 \pm 0.067)\%$  [16]) to correct the pion detection efficiency asymmetry,  $A_{\epsilon}^{\pi^\pm}$ , and the forward-backward asymmetry,  $A_{FB}$ , originating due to interference between the amplitudes mediated by a virtual photon,  $Z^0$  boson, and higher order effects in  $e^+ e^- \rightarrow c\bar{c}$ .

The raw asymmetry is related to  $A_{raw}^{\pi\pi} = \frac{N(D^+ \rightarrow \pi^+ \pi^0) - N(D^- \rightarrow \pi^- \pi^0)}{N(D^+ \rightarrow \pi^+ \pi^0) + N(D^- \rightarrow \pi^- \pi^0)} = A_{CP}^{\pi\pi} + A_{FB} + A_{\epsilon}^{\pi^\pm}$ , where  $N(D^+ \rightarrow \pi^+ \pi^0)$  and  $N(D^- \rightarrow \pi^- \pi^0)$  are the yields for the signal and its  $CP$ -conjugate process, respectively. A simultaneous fit to the invariant mass ( $M_D$ ) is employed to determine the raw asymmetries. For the tagged sample, the raw asymmetries are obtained as  $\mathcal{A}_{raw}^{\pi\pi} = (+0.52 \pm 1.92)\%$  (signal) and  $\mathcal{A}_{raw}^{K\pi} = (0.29 \pm 0.44)\%$  (normalization mode); the corresponding results for untagged sample are  $\mathcal{A}_{raw}^{\pi\pi} = (+3.77 \pm 1.60)\%$  and  $\mathcal{A}_{raw}^{K\pi} = (0.25 \pm 0.17)\%$ .

The difference in the raw asymmetries is represented as  $\Delta\mathcal{A}_{raw} \equiv \mathcal{A}_{raw}^{\pi\pi} - \mathcal{A}_{raw}^{K\pi} = \mathcal{A}_{CP}^{\pi\pi} - \mathcal{A}_{CP}^{K\pi}$ , and is calculated for both tagged and untagged sample:  $\Delta\mathcal{A}_{raw}(\text{tagged}) = (+0.81 \pm 1.97 \pm 0.19)\%$  and  $\Delta\mathcal{A}_{raw}(\text{untagged}) = (+4.02 \pm 1.61 \pm 0.32)\%$ . A combination of the two [17] results in

$\Delta A_{raw} = (+2.67 \pm 1.24 \pm 0.20)\%$ . Finally, we obtain

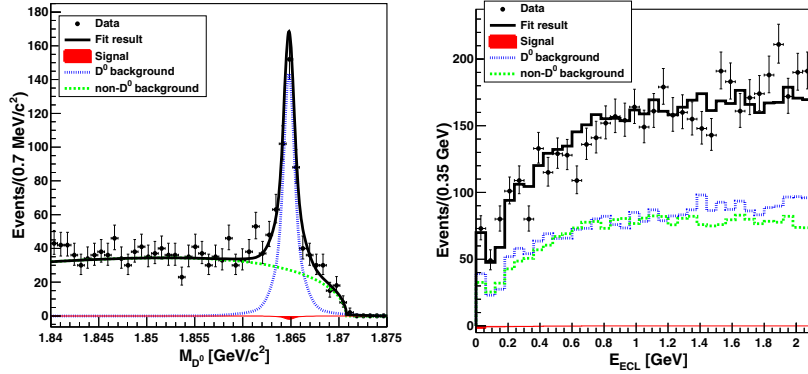
$$\mathcal{A}_{CP}(D^+ \rightarrow \pi^+ \pi^0) = (+2.31 \pm 1.24 \pm 0.23)\%,$$

which is consistent with zero, as expected in the Standard Model [18]. The precision is improved by more than a factor of two over the measurement performed by CLEO.

## 5. Search for $D^0 \rightarrow$ invisible final states

The estimated  $\mathcal{B}$  of helicity-suppressed  $D^0 \rightarrow \nu\bar{\nu}$  decay is  $1.1 \times 10^{-30}$  [19], which is impossible to be reached by current collider experiments. The  $\mathcal{B}$  of  $D^0$  to invisible final states may be enhanced up to  $\mathcal{O}(10^{-15})$  with several dark matter candidates in the non-SM mechanism [20, 21].

We report the first search for the  $D^0$  decays to invisible final states using  $924 \text{ fb}^{-1}$  data collected at and near the  $\Upsilon(4S)$  and  $\Upsilon(5S)$  resonances. To identify  $D^0$  decays containing invisible particles, the charm tagger method is used to select an inclusive  $D^0$  sample [22]. The process  $e^+e^- \rightarrow c\bar{c} \rightarrow D_{tag}^{(*)} X_{frag} \bar{D}_{sig}^{(*)-}$  with  $\bar{D}_{sig}^{(*)-} \rightarrow \bar{D}_{sig}^{(0)} \pi_s^-$  is reconstructed except for  $\bar{D}_{sig}^{(0)}$ . Here,  $D_{tag}^{(*)}$  and  $X_{frag}$  denote a charm particle ( $D^{(*)0}$ ,  $D^{(*)+}$ ,  $D_s^{(*)+}$  or  $\Lambda_c^+$ ) and extra fragmentation particles, respectively. The inclusive  $D^0$  yield is extracted from a one dimensional extended unbinned maximum likelihood fit to the missing mass for the  $D_{tag}^{(*)} X_{frag} \pi_s^-$  system ( $M_{D^0}$ ). Requiring no remaining final state particles associated with  $\bar{D}_{sig}^{(0)}$  selects the invisible  $D^0$  decay candidates. A two-dimensional extended unbinned maximum-likelihood fit to the invariant mass distributions of  $D^0$  and the residual energy in the electromagnetic calorimeter  $E_{ECL}$  is used to extract the  $D^0 \rightarrow$  invisible signal yield. Figure 3 shows the projections of the fit. The fitted signal yield is  $-6.3_{-21.0}^{+22.5}$ , which is consistent with zero. An upper limit on the  $\mathcal{B}$  is determined as  $9.4 \times 10^{-5}$  at the 90% confidence level [23].



**Figure 3:** Fit results of  $D^0$  decays to invisible final states. The left plot shows the  $M_{D^0}$  distribution for  $E_{ECL} < 0.5 \text{ GeV}$  and right plot shows  $E_{ECL}$  for  $M_{D^0} > 1.86 \text{ GeV}/c^2$ . The points with error bars are data, the blue dotted line is  $D^0$  background, the green dashed line is non- $D^0$  background, the red filled area is the signal of  $D^0$  decaying to invisible final states and the solid black line is the total fit result.

## 6. Summary

We have summarized recent studies from Belle on  $B^+ \rightarrow K^+ K^- \pi^+$  and  $B^0 \rightarrow \pi^0 \pi^0$  charmless  $B$  decays,  $D^+ \rightarrow \pi^+ \pi^0$  rare  $D$  decay and the first search for  $D^0$  to invisible final states using the

full Belle data set. The  $\mathcal{B}$  and  $\mathcal{A}_{CP}$  in  $B^+ \rightarrow K^+ K^- \pi^+$  are quantified as a function of  $K^+ K^-$  invariant mass. We confirm the large  $CP$  asymmetry with  $4.8 \sigma$  significance in the low  $M_{K^+ K^-}$  region consistent with the *BABAR* and LHCb measurements. An extensive data set from Belle II and LHCb is needed to understand the origin of the low-mass dynamics. Measurements of the  $\mathcal{B}$  and  $\mathcal{A}_{CP}$  in  $B^0 \rightarrow \pi^0 \pi^0$  have been presented. The results are used to update the  $\phi_2$  constraint from Belle. A search for  $CP$  violation in the  $D^+ \rightarrow \pi^+ \pi^0$  decay crucial to test the isospin sum rule has been discussed. The  $\mathcal{A}_{CP}$  is consistent with the SM expectation (null asymmetry), and the precision is improved by more than a factor of two over the previous measurement. The first search for  $D^0$  decays into invisible final states has been performed, and no significant signal yield is found.

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