

## Measurements of CKM angles at Belle

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In this review recent studies on  $CP$  violation and related hadronic  $B$  decays by the Belle experiment, in particular measurements of CKM angles  $\phi_1$  and  $\phi_2$  are reported.

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## 1. Introduction

In the standard model (SM) of electroweak interaction, charge-parity ( $CP$ ) violation arises from an irreducible complex phase in the Cabibbo-Kobayashi-Maskawa (CKM) quark-mixing matrix [1]. The Belle and BaBar experiments have established  $CP$  violating effects in the  $B$  meson system. Both experiments use their measurements of the mixing-induced  $CP$  violation in  $b \rightarrow c\bar{c}s$  transitions to precisely determine the parameter  $\sin(2\phi_1)$ , where  $\phi_1$  is defined as  $\arg[-V_{cd}V_{cb}^*/V_{td}V_{tb}^*]$ , with  $V_{ij}$  is the CKM matrix element of quarks  $i, j$ . In this proceeding an overview of recent measurements of the CKM angles  $\phi_1$  and  $\phi_2$  ( $\arg[-V_{td}V_{tb}^*/V_{ud}V_{ub}^*]$ ) is presented. Unless stated otherwise, all measurements presented here are based on Belle's final dataset of  $772 \times 10^6 B\bar{B}$  pairs.

## 2. First observation of $CP$ violation in $\bar{B}^0 \rightarrow D_{CP}^{(*)}h^0$ decays with Belle + BaBar data

The decay  $\bar{B}^0 \rightarrow D^{(*)}h^0$ , where  $h^0$  is a light, unflavored neutral meson ( $h^0 \in \pi^0, \eta, \omega$ ), is dominated by a  $b \rightarrow c\bar{u}d$  color-suppressed tree diagram in the SM. The final state  $D^{(*)}h^0$  is a  $CP$  eigenstate if the neutral  $D$  meson decays to a  $CP$  eigenstate as well (*i.e.*,  $D_{CP}^0 \rightarrow K_S^0\pi^0$ ,  $D_{CP}^0 \rightarrow K_S^0\omega$  ( $CP = -1$ ) or  $D_{CP}^0 \rightarrow K^+K^-$  ( $CP = +1$ ) and  $D_{CP}^{*0} \rightarrow D_{CP}^0\pi^0$ ). Therefore, a time-dependent  $CP$  asymmetry measurement is applicable in the same way as used in the  $b \rightarrow c\bar{c}s$  decays, but with a small correction from the  $b \rightarrow u\bar{c}d$  process. This  $b \rightarrow u\bar{c}d$  amplitude is suppressed by  $V_{ub}V_{cd}^*/V_{cb}V_{ud}^* \approx 0.02$  relative to the leading amplitude. Neglecting the suppressed amplitude, the time evolution of  $\bar{B}^0 \rightarrow D_{CP}^{(*)}h^0$  decays is governed by  $\phi_1$ [2].

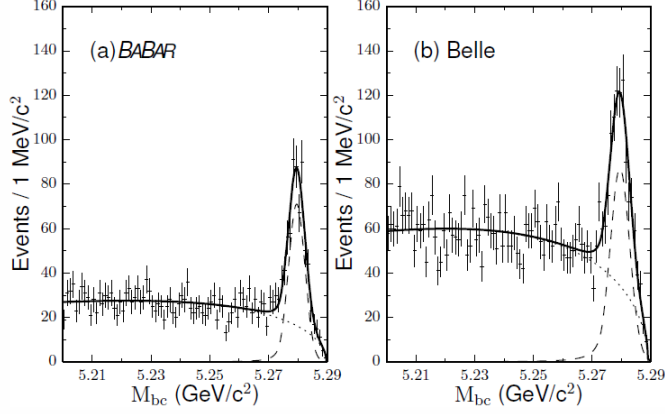
Due to the limited available statistics, previous measurements performed separately by the BaBar and Belle collaborations were not able to establish  $CP$  violation in these or related decays [3]. This motivated a joint analysis using the combined full dataset of Belle and BaBar experiments [4]. Using a fit to the beam-energy constrained mass  $M_{bc} = \sqrt{E_{\text{beam}}^2 - p_B^2}$ , where  $E_{\text{beam}}$  is the beam energy and  $p_B$  is the reconstructed  $B$  meson momentum in the center-of-mass system, we extract  $508 \pm 31$  signal events in the BaBar data of 431 million  $B\bar{B}$  events and  $757 \pm 44$  signal events in the Belle data of 772 million  $B\bar{B}$  events, as shown in Fig. 1. The dominant source of background originates from  $e^+e^- \rightarrow p\bar{q}$  ( $q \in u, d, s, c$ ) continuum events. To suppress this background, we use a multivariate analyzer based on a neural network. The neural network uses the so-called event shape variables to discriminate continuum events, which tend to be jetlike, from spherical  $B\bar{B}$  events.

The time-dependent  $CP$  violation measurement is performed using established Belle and BaBar techniques for the vertex reconstruction, the flavor-tagging, and the modeling of  $\Delta t$  resolution effects, where  $\Delta t$  is the proper time interval between the decays of the two  $B$  mesons produced in an  $\Upsilon(4S)$  decay. Combined analysis is performed by maximizing a joint log-likelihood function

$$\ln \mathcal{L} = \sum_i \ln \mathcal{P}_i^{\text{Belle}} + \mathcal{P}_i^{\text{BaBar}}. \quad (2.1)$$

The experiment-dependent probability density function (PDF)  $\mathcal{P}^{\text{Exp}}$  is defined as

$$\mathcal{P}^{\text{Exp}} = \sum_k f_k \int \left[ P_k(\Delta t') R_k^{\text{Exp}}(\Delta t - \Delta t') \right] d\Delta t', \quad (2.2)$$



**Figure 1:**  $M_{bc}$  distributions (data points with error bars) and fit projections (solid lines) of  $\bar{B}^0 \rightarrow D_{CP}^{(*)}h^0$  decays for (a) BaBar and (b) Belle. The dashed (dotted) lines represent projections of the signal (background) fit components.

where the index  $k$  represents the signal and background PDF components. The symbol  $P_k$  denotes the PDF describing the proper time interval of the particular physical process and  $R_k^{\text{Exp}}$  refers to the corresponding resolution function. The fractions  $f_k$  are evaluated on an event-by-event basis as a function of  $M_{bc}$ . While the background model is determined from the  $M_{bc}$  sideband and hence is experiment-dependent, the signal model is expressed as

$$P_{\text{sig}}(\Delta t, q) = \frac{1}{4\tau_{B^0}} e^{\frac{-|\Delta t|}{\tau_{B^0}}} [1 + q(S \sin(\Delta m \Delta t) - A \cos(\Delta m \Delta t))], \quad (2.3)$$

where the  $B^0$  meson lifetime is represented by  $\tau_{B^0}$ ,  $B^0 - \bar{B}^0$  mixing frequency by  $\Delta m$  and  $q$  is event- and experiment-dependent tagging quality parameter. In the SM, the coefficients,  $S = -\eta_f \sin(2\phi_1)$  and  $A = 0$ , where  $\eta_f$  is the  $CP$  eigenvalue of the final state.  $S$  and  $A$  quantify mixing-induced and direct  $CP$  violation, respectively. The combined fit gives

$$-\eta_f S = +0.66 \pm 0.10 \text{ (stat.)} \pm 0.06 \text{ (syst.)}, \quad A = -0.02 \pm 0.07 \text{ (stat.)} \pm 0.03 \text{ (syst.)}. \quad (2.4)$$

These results correspond to the first observation of  $CP$  violation in  $\bar{B}^0 \rightarrow D_{CP}^{(*)}h^0$  decays with a significance of 5.4 standard deviations and are in agreement with the value of  $\phi_1$  measured from  $b \rightarrow c\bar{c}s$  transitions.

### 3. Measurement of $\phi_1$ in $B^0 \rightarrow \bar{D}^{(*)0}h^0$ with time-dependent binned Dalitz plot analysis

In this analysis, we present a model-independent measurement of the angle  $\phi_1$  in  $b \rightarrow c\bar{u}d$  transitions governing  $B^0 \rightarrow \bar{D}^{(*)0}h^0$  decays, with subsequent decay  $\bar{D}^0 \rightarrow K_S^0 \pi^+ \pi^-$  is not a  $CP$  eigenstate [5]. From a fit to  $M_{bc}$  and  $\Delta E = E_B - E_{\text{beam}}$ , where  $E_B$  is the reconstructed  $B$  mesons energy in the center-of-mass system, we extract total  $962 \pm 41$  signal events, of which  $464 \pm 26$  events are from  $B^0 \rightarrow \bar{D}^0 \pi^0$  mode (Fig. 2), with a signal fraction  $(72.1 \pm 4.1)\%$  and  $182 \pm 18$  events from  $B^0 \rightarrow \bar{D}^0 \omega$  with a fraction of  $(58.4 \pm 5.7)\%$ . The signal fraction of other decay modes ranges between 44% and 70%.

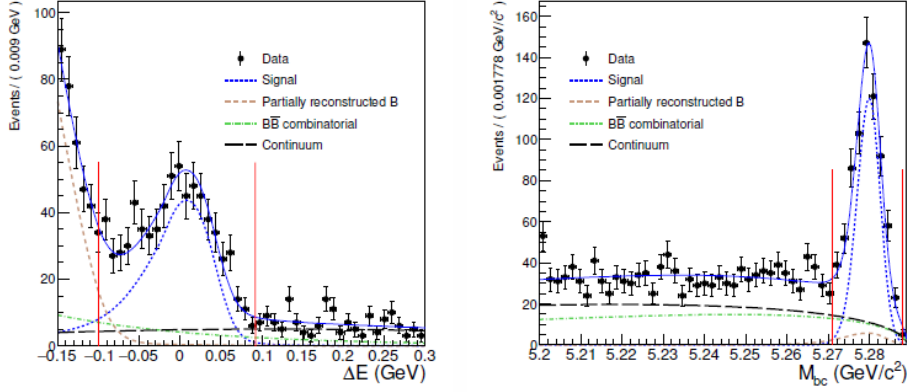


Figure 2:  $M_{bc}$  and  $\Delta E$  distributions of  $B^0 \rightarrow \bar{D}^0 \pi^0$  decays.

Our measurement of  $\phi_1$  is based on the binned Dalitz distribution approach. This idea was proposed in Ref. [6] to measure the angle  $\phi_3$ . Events are divided into 16 bins on the Dalitz plot plane and the number of events in bin  $i$  ( $i = -8, \dots, -1, +1, \dots, +8$ ) is modeled as

$$P_i(\Delta t, \phi_1) = h e^{-\frac{|\Delta t|}{\tau_B}} \left[ 1 + q \frac{K_i - K_{-i}}{K_i + K_{-i}} \cos(\Delta m \Delta t) + 2q \xi_{h^0} (-1)^L \frac{\sqrt{K_i K_{-i}}}{K_i + K_{-i}} \sin(\Delta m \Delta t) (S_i \cos(2\phi_1) + C_i \sin(2\phi_1)) \right], \quad (3.1)$$

where  $h$  is the normalization constant,  $\xi_{h^0}$  is the  $CP$  eigenvalue of  $h^0$  meson,  $L$  is the relative angular momentum in the  $D^{(*)0} h^0$  system,  $K_i$  is the integrated squared amplitude, and  $S_i$  and  $C_i$  represent the weighted averages of the sine and cosine of the phase difference between  $\bar{D}^0$  and  $D^0$  decay amplitudes over the  $i$ th Dalitz plot bin. The parameters  $K_i$  can be measured with a set of flavor-tagged neutral  $D$  mesons such as  $D^{*+} \rightarrow D^0 \pi^+$  or  $B^+ \rightarrow \bar{D}^0 \pi^+$  decays, by measuring signal yield in each Dalitz plot bin. The measurement of the phase parameters  $S_i$  and  $C_i$  is more complicated and can be done with coherent decays of  $D^0 \bar{D}^0$  pairs [7]. We obtain

$$\begin{aligned} \sin(2\phi_1) &= 0.43 \pm 0.27 \text{ (stat.)} \pm 0.08 \text{ (syst.)} \\ \cos(2\phi_1) &= 1.06 \pm 0.33 \text{ (stat.)}^{+0.21}_{-0.15} \text{ (syst.)} \\ \phi_1 &= 11.7^\circ \pm 7.8^\circ \text{ (stat.)} \pm 2.1^\circ \text{ (syst.)}. \end{aligned} \quad (3.2)$$

The value  $\sin(2\phi_1) = 0.691 \pm 0.017$  measured in  $b \rightarrow c\bar{c}s$  transitions determines the absolute value of  $\cos(2\phi_1)$ , leading two possible solutions in the  $0^\circ \leq \phi_1 \leq 180^\circ$  range. Our measurement is inconsistent with the negative solution, corresponding to the value  $\phi_1 = 68.1^\circ$  at the level of 5.1 standard deviations, but in agreement with the positive solution, corresponding to the value  $\phi_1 = 21.9^\circ$  at 1.3 standard deviations.

#### 4. First observation of the decay $B^0 \rightarrow \psi(2S)\pi^0$

Although decays mediated via  $b \rightarrow c\bar{c}s$  transitions allow us to access the  $\phi_1$  at first order (tree), its value is prone to distortion from suppressed higher-order loop-induced (penguin) amplitudes containing different weak phases. The related  $b \rightarrow c\bar{c}d$  induced decays can be used to quantify the

shift in  $\phi_1$  caused by these loop contributions and may provide useful information about the penguin pollution [8]. Since the dominant  $b \rightarrow c\bar{c}d$  tree amplitude is also suppressed,  $B^0 \rightarrow J/\psi\pi^0$  is the only mode measured so far, providing  $\sin(2\phi_1) = 0.65 \pm 0.21$  (stat.)  $\pm 0.05$  (syst.) by Belle [9], which is consistent with  $\sin(2\phi_1)$  from  $b \rightarrow c\bar{c}s$ . The possible next mode,  $B^0 \rightarrow \psi(2S)\pi^0$  was not observed previously.

The decay mode  $B^0 \rightarrow \psi(2S)\pi^0$  is reconstructed with  $\psi(2S) \rightarrow \ell^+\ell^-$  ( $\ell = e, \mu$ ) or  $\psi(2S) \rightarrow J/\psi(\rightarrow \ell^+\ell^-)\pi^+\pi^-$  [10]. The major background contribution originates from  $b \rightarrow c\bar{c}q$  decays other than the signal. The background arises from  $e^+e^- \rightarrow q\bar{q}$  ( $q = u, d, s, c$ ) continuum events is not so problematic and is suppressed by applying a loose requirement on the ratio of second- to zeroth-order Fox-Wolfram moments. The signal is extracted from a fit to  $M'_{bc}$  and  $\Delta E$ , where  $M'_{bc}$  is the modified beam-constrained mass to take into account the worse energy resolution of  $\pi^0$  than rest of the particles. The fit gives  $85 \pm 12$  signal events with a significance of 7.2 standard deviations. The branching fraction is measured to be

$$\mathcal{B}(B^0 \rightarrow \psi(2S)\pi^0) = [1.17 \pm 0.17 \text{ (stat.)} \pm 0.08 \text{ (syst.)}] \times 10^{-5}. \quad (4.1)$$

This measurement constitutes the first observation of this decay and it will contribute to the future time-dependent  $CP$  asymmetry measurement of the  $b \rightarrow c\bar{c}d$  process.

## 5. Study of $B^0 \rightarrow \rho^+\rho^-$ decays

In order to access  $\phi_2$ , charmless decay modes that are mediated via  $b \rightarrow u\bar{u}d$  transitions are necessary. Examples are the decays  $B \rightarrow \pi\pi, \rho\pi, \rho\rho$ . At tree level, one expects  $A = 0$  and  $S = \sin(2\phi_2)$ . Possible penguin contributions can give rise of direct  $CP$  violation,  $A \neq 0$  and also pollute the measurement of  $\phi_2$ ,  $S = \sqrt{1-A^2}\sin(2\phi_2^{\text{eff}})$ , where the observed  $\phi_2^{\text{eff}} = \phi_2 - \Delta\phi_2$  is shifted by  $\Delta\phi_2$  due to different weak and strong phases from additional non-leading contributions. This inconvenience can be overcome by estimating  $\Delta\phi_2$  using either an isospin analysis [11] or  $SU(3)$  flavor symmetry [12]. In this analysis, we present a measurement of the branching fraction and the longitudinal polarization fraction of  $B^0 \rightarrow \rho^+\rho^-$  decays, as well as the time-dependent  $CP$  violating parameters [13].

In addition to combinatorial background, the presence of multiple background components with the same four-pion final state as  $B^0 \rightarrow \rho^+\rho^-$  make this decay quite difficult to isolate and interferences between the various four-pion modes need to be considered. A multi-dimensional maximum likelihood fit is performed. The fit uses the variables  $\Delta E$ ,  $M_{bc}$ , the masses and helicity angles (angle between one of the daughter of  $\rho^\pm$  meson and the  $B$  flight direction in the corresponding rest frame of the  $\rho^\pm$ .) of the two reconstructed  $\rho^\pm$  mesons to separate longitudinally polarized states from transversely polarized states, a fisher discriminant to separate the jet-like continuum events from the spherical  $B\bar{B}$  decays and the  $\Delta t$  distribution for the two flavors of  $B_{\text{tag}}$ . We obtain the branching fraction

$$\mathcal{B}(B^0 \rightarrow \rho^+\rho^-) = [28.3 \pm 1.5 \text{ (stat.)} \pm 1.5 \text{ (syst.)}] \times 10^{-6}, \quad (5.1)$$

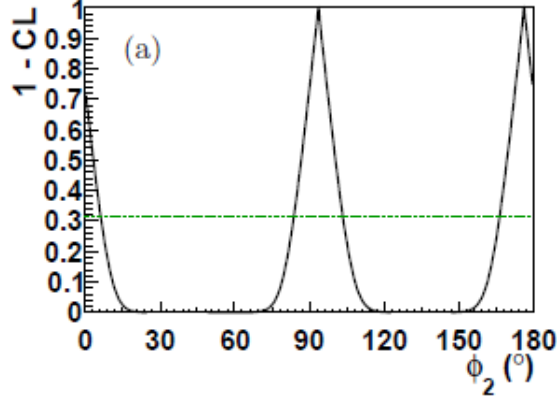
the fraction of longitudinal polarization

$$f_L = 0.988 \pm 0.012 \text{ (stat.)} \pm 0.023 \text{ (syst.)}, \quad (5.2)$$

and the  $CP$  violating parameters

$$S = -0.13 \pm 0.15 \text{ (stat.)} \pm 0.05 \text{ (syst.)}, \quad A = 0.00 \pm 0.10 \text{ (stat.)} \pm 0.06 \text{ (syst.)}. \quad (5.3)$$

These results together with the other Belle measurements [14] are used to perform an isospin analysis to constrain the CKM angle  $\phi_2$  and obtain two solutions with  $\phi_2 = (93.7 \pm 10.6)^\circ$  being most compatible with other SM based fits to the data. The size of the penguin pollution is consistent with zero:  $\Delta\phi_2 = (0.0 \pm 9.6)^\circ$ . Figure 3 shows the  $\phi_2$  can from the isospin analysis.



**Figure 3:** Probability scan of  $\phi_2$  in the  $B \rightarrow \rho\rho$  system. The horizontal line shows the 68% confidence level.

## 6. Summary

The first observation of  $CP$  violation in  $\bar{B}^0 \rightarrow D_{CP}^{(*)}h^0$  decays from a combined analysis of Belle and BaBar dataset is presented. The result is consistent with the value of  $\sin(2\phi_1)$  measured in the  $b \rightarrow c\bar{c}s$  process. Using a similar process,  $B^0 \rightarrow \bar{D}^{(*)0}h^0$  with  $\bar{D}^0 \rightarrow K_S^0\pi^+\pi^-$ , a model-independent time-dependent Dalitz plot analysis is performed and excludes the second  $\phi_1$  solution by 5.1 standard deviations. Observation of  $B^0 \rightarrow \psi(2S)\pi^0$  is presented, which will contribute to the  $\phi_1$  measurement in future. And finally  $\phi_2$  measurement from  $B \rightarrow \rho\rho$  decays is presented.

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