

The X-ray outburst of the Galactic Centre magnetar as monitored by *Chandra* and *XMM-Newton*

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In 2013 April a new magnetar, SGR 1745–2900, was discovered as it entered an outburst, at an angular separation of only 2.4 arcsec from the supermassive black hole at the centre of the Milky Way, Sagittarius A*. The new source was detected both in the radio and X-ray bands, with a peak X-ray luminosity $L_X \sim 5 \times 10^{35}$ erg s⁻¹, and it has a spin-down magnetic field of $\sim 2 \times 10^{14}$ G. Here we report on the long-term *Chandra* (25 observations) and *XMM–Newton* (eight observations) X-ray monitoring campaign of SGR 1745–2900 from the onset of the outburst in 2013 April 2013 until 2014 September. This unprecedented data set allows us to refine the timing properties of the source, as well as to study the outburst spectral evolution as a function of time and rotational phase. Our timing analysis confirms the increase in the spin period derivative by a factor of ~ 2 around 2013 June, and reveals that a further increase occurred between 2013 October 30 and 2014 February 21. We find that the period derivative changed from 6.6×10^{-12} to 3.3×10^{-11} s s⁻¹ in 1.5 yr. On the other hand, this magnetar shows a slow flux decay compared to other magnetars and a rather inefficient surface cooling. In particular, starquake-induced crustal cooling models alone have difficulty in explaining the high luminosity of the source for the first ~ 200 d of its outburst, and additional heating of the star surface from currents flowing in a twisted magnetic bundle is probably playing an important role in the outburst evolution.

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1. Introduction

In the past decade, extensive study of magnetars in outburst has led to a number of unexpected discoveries which have changed our understanding of these objects ([1], [2]). The detection of typical magnetar-like bursts and a powerful enhancement of the persistent emission unveiled the existence of three low magnetic field ($B < 4 \times 10^{13}$ G) magnetars ([3], [4], [5], [6]). Recently, an absorption line at a phase-variable energy was discovered in the X-ray spectrum of SGR 0418+5729. This, if interpreted in terms of a proton cyclotron feature, provides a direct estimate of the magnetic field strength close to the neutron star surface ([7]).

In 2013 April a new magnetar, SGR 1745–2900, was discovered as it entered an outburst at only 2.4 arcsec from the supermassive black hole at the Centre of the Milky Way, Sgr A* ([8], [9], [10]). SGR 1745–2900 has a spin-down magnetic field of $\sim 2 \times 10^{14}$ G and holds the record as the closest neutron star to a black hole detected to date. The angular separation of 2.4 ± 0.3 arcsec from Sgr A* corresponds to a minimum physical separation of 0.09 ± 0.02 pc (at a 95% confidence level) for an assumed distance of 8.3 kpc. The source has been observed daily with *Swift*/XRT until 2014 October, and its 2–10 keV flux has decayed steadily during this time interval ([11]).

Here we report on the X-ray long-term monitoring campaign of SGR 1745–2900 covering the first 1.5 yr of the outburst decay. In Section 2 we describe the *Chandra* and *XMM–Newton* observations and the data analysis. In Section 3 we discuss our results; conclusions follow in Section 4.

2. Observations and data analysis

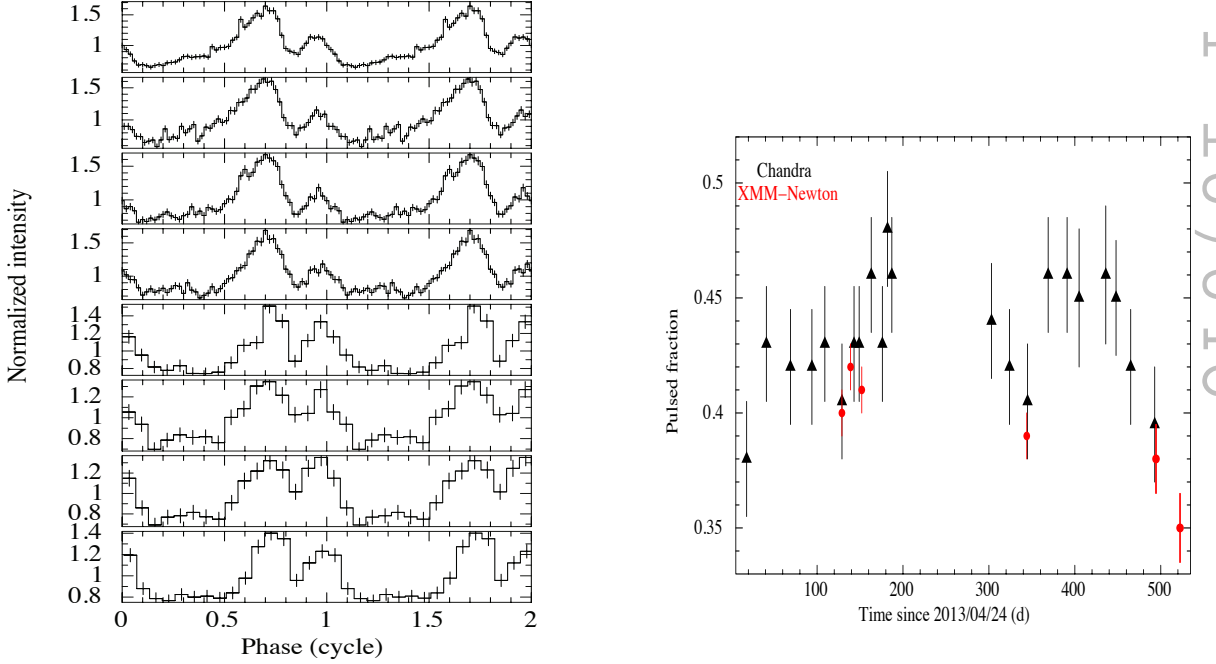
Chandra observed SGR 1745–2900 twenty-six times between 2013 April 29 and 2014 August 30. The first observation was performed with the HRC to have the best spatial accuracy to localize the source in the crowded region of the Galactic Centre ([10]). The remaining observations were performed with the ACIS in faint timed-exposure imaging mode with a 1/8 sub-array (time resolution of 0.4 s), and in three cases with the HETG. The source was positioned on the back-illuminated S3 chip. Eight observations were carried out by *XMM–Newton*/EPIC, with the pn CCD camera operated in full-frame window mode (time resolution of 73.4 ms) in all cases.

2.1 Timing analysis

We derive a phase coherent solution (solution A, see Table 1) that is able to model the pulse phase evolution before a 115 d observations gap starting at MJD 56600, and which is compatible with the solution given by [12] for the partly overlapping interval MJD 56457 – 56519. After the observation gap, solution A is no longer able to provide a good description of pulse phases, and we are only able to find a solution based on the analysis of the spin frequency evolution (solution B, see Table 1). We then use timing solution A (up to MJD 56594.1) and solution B (from MJD 56709.5 onwards) to fold all background-subtracted and exposure-corrected light curves at the neutron star spin period during the corresponding observation (see the left panel of Fig. 1). This allows us to extract the temporal evolution of the pulsed fraction, defined as $PF = [Max - Min]/[Max + Min]$ (Max and Min being the maximum and the minimum count rate of the pulse profile, respectively; see the right-hand panel of Fig. 1).

Table 1: Timing solutions. Errors were evaluated at the 1σ confidence level, scaling the uncertainties by the value of the rms ($\sqrt{\chi^2_{\dot{\nu}}}$) of the respective fit to account for the presence of unfitted residuals.

Solution	Rea et al. (2013) [10]	Kaspi et al. (2014) [12]	This work (solution A)	This work (solution B)
Epoch T_0 (MJD)	56424.5509871	56513.0	56513.0	56710.0
Validity range (MJD)	56411.6 – 56475.3	56457 – 56519	56500.1 – 56594.1	56709.5 – 56929
$P(T_0)$ (s)	3.7635537(2)	3.76363824(13)	3.76363799(7)	3.7639772(12)
$\dot{P}(T_0)$	$6.61(4) \times 10^{-12}$	$1.385(15) \times 10^{-11}$	$1.360(6) \times 10^{-11}$	$3.27(7) \times 10^{-11}$
\ddot{P} (s^{-1})	$4(3) \times 10^{-19}$	$3.9(6) \times 10^{-19}$	$3.7(2) \times 10^{-19}$	$(-1.8 \pm 0.8) \times 10^{-19}$
$\nu(T_0)$ (Hz)	0.265706368(14)	0.265700350(9)	0.26570037(5)	0.26567642(9)
$\dot{\nu}(T_0)$ (Hz s^{-1})	$-4.67(3) \times 10^{-13}$	$-9.77(10) \times 10^{-13}$	$-9.60(4) \times 10^{-13}$	$-2.31(5) \times 10^{-12}$
$\ddot{\nu}$ (Hz s^{-2})	$-3(2) \times 10^{-20}$	$-2.7(4) \times 10^{-20}$	$-2.6(1) \times 10^{-20}$	$(1.3 \pm 0.6) \times 10^{-20}$
rms residual	0.15 s	51 ms	0.396 s	1.0 μHz
$\chi^2_{\dot{\nu}}$ (d.o.f.)	0.85 (5)	1.27 (41)	6.14 (44)	0.66 (10)

**Figure 1:** Left-hand panel: pulse profiles of SGR 1745–2900 in the 0.3–10 keV energy range obtained from *XMM-Newton*/EPIC-pn observations. Two cycles are shown for clarity. Right-hand panel: temporal evolution of the pulsed fraction (see text for our definition) in the 0.3–10 keV band. Uncertainties on the values were obtained by propagating the errors on the maximum and minimum count rates.

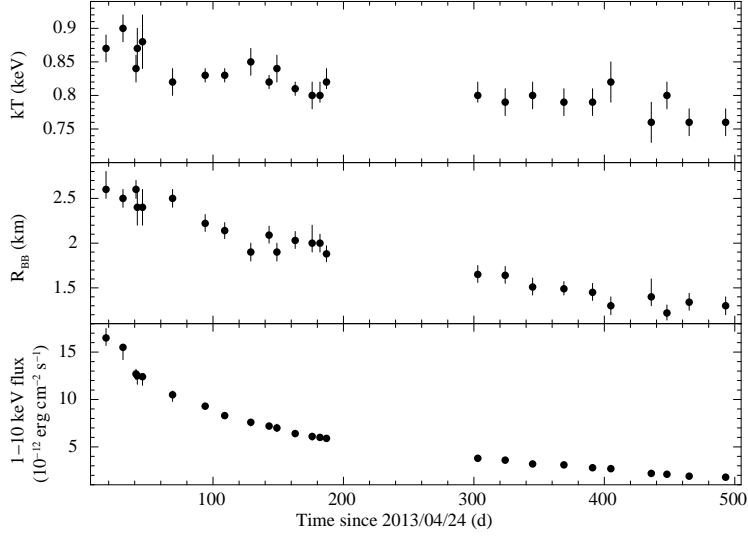


Figure 2: Temporal evolution of the spectral parameters for the blackbody model and of the absorbed intrinsic blackbody flux of SGR 1745–2900 in the 1–10 keV energy range from *Chandra* observations. The blackbody emitting radius is calculated assuming a source distance of 8.3 kpc. All errors are reported at a 90% confidence level for a single parameter of interest ($\Delta\chi^2 = 2.706$).

2.2 Spectral analysis

A joint fit of all *Chandra* non-grating spectra with an absorbed blackbody model (in the 0.3–8 keV energy range, with the hydrogen column density tied to be the same between all the observations) yields $\chi^2_{\nu} = 1.00$ for 2282 d.o.f., with $N_{\text{H}} = 1.90(2) \times 10^{23} \text{ cm}^{-2}$ (at a 90% confidence level). When an absorbed power law model is used ($\chi^2_{\nu} = 1.05$ for 2282 d.o.f.), we obtain large values for the photon index ($\Gamma = 4.2 - 4.9$) and the photoelectric absorption ($N_{\text{H}} \sim 3 \times 10^{23} \text{ cm}^{-2}$). These are likely an artifact of the fitting process which tends to increase the absorption to compensate the large flux at low energies defined by the power law. The addition of a second component to the blackbody (another blackbody or a power law), is not statistically required. A single absorbed blackbody thus provides the best modeling of the source spectrum in the 0.3–8 keV energy range. Zeroth-order spectral data of the three grating observations were fitted together and independently with this model, fixing N_{H} to that obtained in non-grating fit (see Fig. 2).

Based on the results of the *Chandra* analysis, we fit jointly all the *XMM-Newton*/EPIC-pn spectra in the 2–12 keV band with an absorbed blackbody model. We obtain $\chi^2_{\nu} = 2.2$ for 636 d.o.f., with large residuals at high energies. The latter disappear if an absorbed power law component is added ($\chi^2_{\nu} = 1.13$ for 624 d.o.f.; see the left-hand panel of Fig. 3). We also apply a 3D resonant cyclotron scattering model ([13], [14], [15]), obtaining $\chi^2_{\nu} = 1.14$ for 624 d.o.f. (see the right-hand panel of Fig. 3). Both models successfully reproduce the soft X-ray part of the SGR 1745–2900 spectra up to ~ 12 keV, implying that, similar to other magnetars, the reprocessing of the thermal emission by a dense, twisted magnetosphere produces a non-thermal component ([16]). The power law detected by *XMM-Newton* is consistent with that observed by *NuSTAR* ([12], and its very low contribution below 8 keV is consistent with its non-detection in our *Chandra* data.

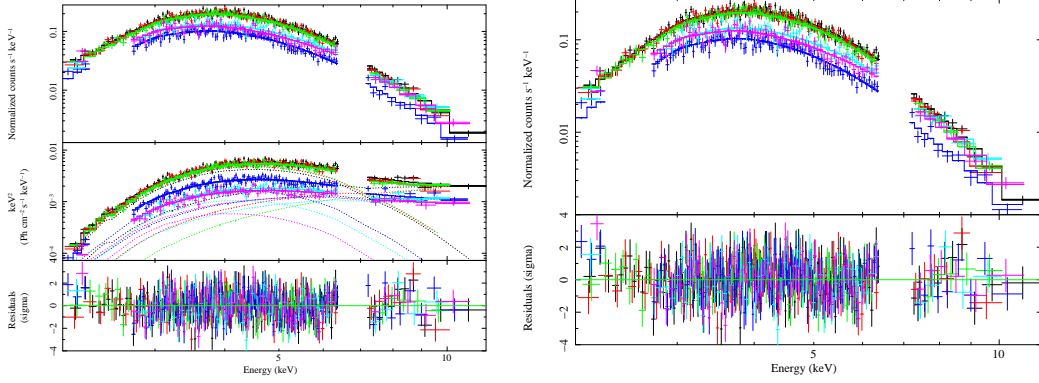


Figure 3: Results of the phase-averaged spectral analysis for the *XMM-Newton*/EPIC-pn observations of SGR 1745–2900. Spectra were fitted together in the 2–12 keV energy range and after removal of the Fe XXV and S XV lines from the supernova remnant Sgr A east ([17]). Left-hand panel: spectra fitted with an absorbed blackbody plus power law model. $E^2 f(E)$ unfolded spectra together with the contributions of the two additive components and residuals (in units of standard deviations) are also shown. Right-hand panel: spectra fitted with an absorbed 3-D resonant cyclotron scattering model. Residuals (in units of standard deviations) are also shown.

3. Discussion

The past decade has seen a great success in detecting magnetar outbursts, mainly thanks to the prompt response and monitoring of the *Swift* mission, and to the dedicated follow-up programs of *Chandra*, *XMM-Newton*, and more recently *NuSTAR*. The detailed study of about 10 outbursts has shown many common characteristics (see [2] for a review), although the precise triggering mechanism of these events, as well as the energy reservoir responsible for sustaining the emission over many months, remain uncertain.

The initial behavior of the 2013 outburst decay of SGR 1745–2900 was compatible with those observed in other magnetars. The outburst peak, the thermal emission peaked at about 1 keV, the small radiating surface (about 2 km in radius) and the overall evolution in the first few months were consistent with the behavior observed for other outbursts. However, after an additional year of X-ray monitoring, it became clear that the subsequent evolution of SGR 1745–2900 showed distinct characteristics. The flux decay appears extremely slow: it is the first time that we observe a magnetar with a quiescent luminosity $< 10^{34}$ erg s $^{-1}$ remaining at a luminosity $> 10^{35}$ erg s $^{-1}$ for more than 1 yr and with a temperature decreasing from the initial ~ 1 keV by less than 10%.

3.1 Crustal cooling modeling

In Fig. 4 (left-hand panel, lower curves) we show an example of the expected cooling curve of a magnetar with the same characteristics of SGR 1745–2900 ([18]). We assume that (i) a sudden large energy release, $\simeq 10^{45}$ erg, heats up a layer of the outer crust up to 3×10^9 K; (ii) the event affects the entire magnetar surface; (iii) the layer where the energy is injected extends from an external boundary at $\rho_{\text{OUT}} \sim 3 \times 10^9$ g cm $^{-3}$ to an inner boundary at $\rho_{\text{IN}} \sim 2$ and 4×10^{10} g cm $^{-3}$ (we show these two cases in the two lower curves of Fig. 4, left-hand panel). Even in this most favorable case, the high luminosities observed at late times are difficult to reconcile with any

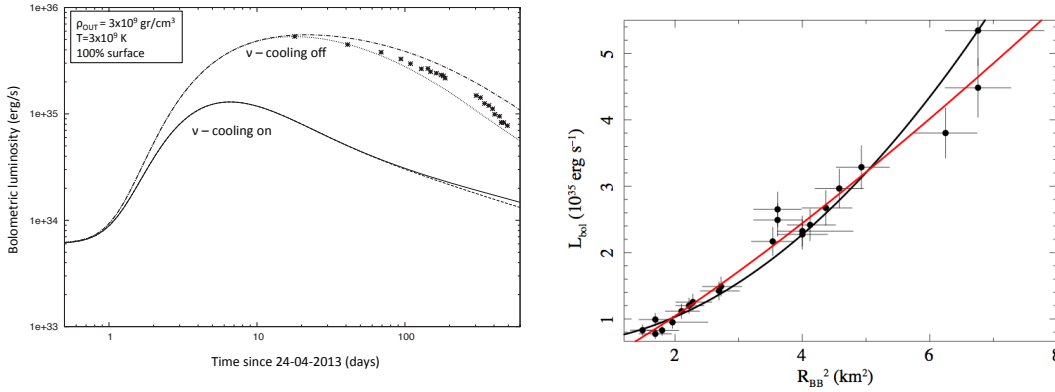


Figure 4: Left-hand panel: crustal cooling curves attempting at modelling the luminosity decrease of SGR 1745–2900. Luminosities are bolometric and calculated assuming a distance of 8.3 kpc. For the neutrino-cooling on and off set of curves, the lower and upper curves are relative to $\rho_{\text{IN}} = 2$ and $4 \times 10^{10} \text{ g cm}^{-3}$, respectively. Right-hand panel: bolometric luminosity as a function of the square of the blackbody radius at infinity. Solid lines represent the fits with a quadratic function (black) and a generic power law with index $\alpha = 1.23(8)$ (red).

cooling model. Injecting more energy or changing ρ_{OUT} only affects the peak luminosity during the first days or weeks, and injecting energy deeper into the crust (i.e. at higher ρ_{IN}) is expected to change the late time evolution only slightly. This can be seen by comparing the solid and dashed lines in the left-hand panel of Fig. 4, which correspond to $\rho_{\text{IN}} = 2$ and $4 \times 10^{10} \text{ g cm}^{-3}$, respectively.

For illustrative purposes, we also show the cooling curves obtained when plasmon and synchrotron neutrino processes are switched off (see the upper curves in the left-hand panel of Fig. 4). These provide a much closer match to the data, but there is no clear reason why these neutrino processes should not operate in these conditions. Another possibility to fit the data is to tune the energy injection, which must be maintained during the first ~ 200 d, resulting in a higher luminosity at late times. If we assume that only a region 5 km in radius is affected (this is closer to the ~ 2 km emitting region observed), we need a continuous injection of at least $\sim 10^{44} \text{ erg s}^{-1} \text{ d}^{-1}$ for about 200 d. However, a physical mechanism that can operate for such a long time-scale is not known. A possibility might be a continuous injection of energy to keep the surface at high temperatures for so long, although in this latter case we should possibly expect more SGR-like bursts during the first hundreds days.

3.2 Bombardment by magnetospheric currents in a bundle

A valid alternative model to the crustal cooling scenario invokes the presence of magnetospheric currents flowing along a gradually shrinking magnetic bundle, and heating the surface from outside. In this scenario, a quasi steady-state outflow of electrons and positrons is maintained thanks to magnetic pair production close to the surface. The non-negligible electric voltage along the magnetic field lines and the radiative force due to Compton scattering regulate the streams of positrons and electrons along the field line ([19]).

The presence of a non-thermal component observed by *NuSTAR* ([9], [12]), and confirmed also by our *XMM-Newton* observations on a much longer temporal baseline, is suggestive of a large density of magnetospheric particles which boost thermal photons emitted from the surface via resonant Compton scattering, providing the power law component. In this context, the observed ~ 2 km size of the emitting blackbody is consistent with a relatively small twisted magnetic bundle. In the scenario in which the outburst evolution is dominated by an untwisting bundle and the poloidal magnetic field has a dipole geometry, the luminosity is expected to decrease with the square of the blackbody area ($A_{\text{BB}} = 4\pi R_{\text{BB}}^2$; [20]). A flatter dependence may arise from a more complex field geometry. In Fig. 4 we show the fits of the bolometric luminosity as a function of R_{BB}^2 with two different models, a quadratic function $L_{\text{bol}} \propto A_{\text{BB}}^2$ (black line; $\chi^2_{\nu} = 1.3$ for 23 d.o.f.) and a power law $L_{\text{bol}} \propto A_{\text{BB}}^{\alpha}$ (red line; $\chi^2_{\nu} = 0.8$ for 23 d.o.f.). For the latter we find $\alpha = 1.23(8)$.

4. Conclusions

The spectacular angular resolution of *Chandra* and the large effective area of *XMM-Newton* allowed us to collect an unprecedented data set covering the outburst of SGR 1745–2900.

We found three different timing solutions between 2013 April 29 and 2014 August 30, which show that the source period derivative has changed at least twice, from 6.6×10^{-12} s s $^{-1}$ in 2013 April at the outburst onset, to 3.3×10^{-11} s s $^{-1}$ in 2014 August. While the first \dot{P} change could be related with the occurrence of an SGR-like burst ([12]), no burst has been detected from the source close in time to the second \dot{P} variation. This further change in the rotational evolution of the source might be related with the timing anomaly observed in the radio band around the end of 2013 ([11]), unfortunately during our observing gap.

The 0.3–8 keV source spectrum is perfectly modeled by a single blackbody with temperature cooling from ~ 0.9 to 0.75 keV in about 1.5 yr. A faint non-thermal component is observed with *XMM-Newton*. It dominates the flux at energies $\gtrsim 8$ keV at all the stages of the outburst decay, with a power law photon index ranging from ~ 1.7 to ~ 2.6 . It is most probably due to resonant Compton scattering on to non-relativistic electrons in the magnetosphere.

Crustal cooling models have difficulty in explaining the high luminosity of this outburst and its extremely slow flux decay. If the outburst evolution is indeed due to crustal cooling, then magnetic energy injection needs to be continuous over at least the first ~ 200 d. The presence of a small twisted bundle sustaining currents bombarding the surface region at the base of the bundle, and keeping the outburst luminosity so high, appears a viable scenario to explain this particular outburst. However, detailed numerical simulations are needed to confirm this possibility.

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