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Forward neutrino-induced meson productions in the resonance region

Satoshi X. Nakamura[*]
Department of Physics, Osaka University, Toyonaka, Osaka 560-0043, Japan
E-mail: `nakamura@kern.phys.sci.osaka-u.ac.jp`

Hiroyuki Kamano
Research Center for Nuclear Physics, Osaka University, Ibaraki, Osaka 567-0047, Japan

T.-S.Harry Lee
Physics Division, Argonne National Laboratory, Argonne, Illinois 60439, USA

Toru Sato
Department of Physics, Osaka University, Toyonaka, Osaka 560-0043, Japan

The forward neutrino-induced meson productions off the nucleon is studied by applying the PCAC hypothesis to our dynamical coupled-channels (DCC) model. The DCC model reasonably describes $\pi N, \gamma N \to \pi N, \eta N, K\Lambda, K\Sigma$ data in the resonance region. We give a prediction for $\nu N \to \pi N, \pi\pi N, \eta N, K\Lambda, K\Sigma$ reactions cross sections. We compare our results with those from the Rein-Sehgal model, and find a significant difference.

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[*] Speaker.

1. Introduction

The last year has seen the discovery of non-zero θ_{13}, and neutrino physics research entered a next stage. Next generation experiments will be targeting the leptonic CP violation and the mass hierarchy of the neutrino. To achieve this goal, it is essential to understand the neutrino-nucleus interaction more precisely, 10% or even better, over a rather wide kinematical region that covers quasi-elastic, resonance, and deep inelastic scattering (DIS) regions.

In this contribution, we are concerned with the resonance region, from the $\Delta(1232)$ through second and third resonance regions, up to $W \lesssim 2$ GeV. Several models have been developed for the neutrino-induced single pion production off the nucleon in the resonance region, and have been used as a basic ingredient to construct neutrino-nucleus interaction models [1, 2]. So far, most models deal with only the single pion production. However, the neutrino-nucleon interaction in the resonance region is a multi-channel reaction. Two-pion production has a contribution comparable to the single pion production. η and kaon productions can also happen. In order to deal with this kind of multi-channel reaction, an ideal approach is to develop a unitary coupled-channels model; this is what we will pursue.

Recently we developed a unitary dynamical coupled-channels (DCC) model that can be extended to the neutrino reactions [3]. Our DCC model is based on a comprehensive analysis of $\pi N, \gamma N \to \pi N, \eta N, K\Lambda, K\Sigma$ reactions in the resonance region, taking account of the coupled-channels unitarity including the $\pi\pi N$ channel. In this contribution, we report our first step of extending the DCC model to the neutrino reactions [4]. For that, we invoke the Partially Conserved Axial Current (PCAC) hypothesis that allows us to relate cross sections of the pion-induced meson productions to those of the corresponding neutrino-induced meson productions in the forward limit.

2. Dynamical coupled-channels model

In our DCC model [3], we consider 8 channels: $\gamma N, \pi N, \eta N, \pi\Delta, \rho N, \sigma N, K\Lambda, K\Sigma$. The $\pi\pi N$ channel is included in the $\pi\Delta, \rho N, \sigma N$ channels using Feshbach's projection method, thus maintaining the three-body unitarity. Meson-exchange driving terms are derived from meson-baryon Lagrangian. The driving terms as well as bare N^* excitation mechanisms are implemented in a coupled-channels Lippmann-Schwinger equation from which we obtain unitary reaction amplitudes. We analyzed $\pi N, \gamma N \to \pi N, \eta N, K\Lambda, K\Sigma$ reaction data simultaneously up to $W = 2.1$ GeV (W : total energy). The analysis includes fitting about 20,000 data points. To see the quality of the fit, we show in Fig. 1 the single pion photoproduction observables from the DCC model compared with data. As seen in the figure, our DCC model gives a reasonable description of meson production data in the resonance region. As a consequence, the DCC model contains all four-star resonances (and more) listed by the Particle Data Group [5]. Thus the DCC model provides a good basis with which we proceed to the neutrino reactions.

3. PCAC and neutrino-induced forward meson productions

Kinematic variables used in the following discussion are as follows. We consider the inclusive $l(k) + N(p) \to l'(k') + X(p')$ reactions ($X = \pi N, \pi\pi N, \eta N$... etc.), where $(l, l') = (\nu_e, e^-), (\bar{\nu}_e, e^+)$

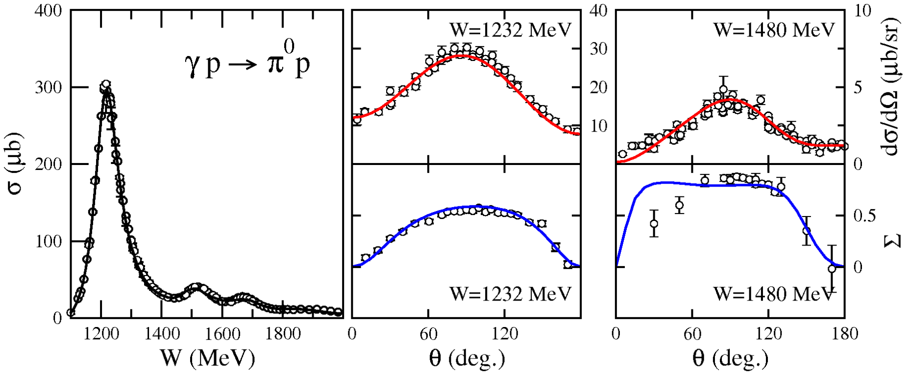

Figure 1: Total cross sections (σ), unpolarized differential cross sections ($d\sigma/d\Omega$) and photon asymmetry (Σ) for $\gamma p \to \pi^0 p$ from the DCC model [3] are compared with data. The total energy is denoted by W, and the scattering angle of the pion by θ.

for the charged-current (CC) reactions. Although we do not show a result, the neutral-current reactions can be studied in a similar manner. We assume that leptons are massless. In the laboratory frame, the four-momentum are defined to be $k = (E, \vec{k})$, $p = (m_N, 0, 0, 0)$, $k' = (E', \vec{k}')$ and $p' = k + p - k'$. With the momentum transfer between l and l', $q = k' - k = (\omega, \vec{q})$, we define the positive quantity Q^2 by $Q^2 = -q^2 = 4EE' \sin^2\frac{\theta}{2}$, where θ is the scattering angle of l' with respect to l in the laboratory frame.

For later use, we also define another frame where X is at rest. In this frame, q and p are denoted as $q = (\omega_c, \vec{q}_c)$ and $p = (E_N, -\vec{q}_c)$, respectively, where $E_N = \sqrt{m_N^2 + |\vec{q}_c|^2}$ and m_N is the nucleon mass. Also, we set $\vec{q}_c = (0, 0, |\vec{q}_c|)$ so that $\vec{q}_c$ defines the z-direction of this frame.

The cross sections for the inclusive neutrino and anti-neutrino reactions are expressed as

$$\frac{d\sigma_\alpha}{dE'd\Omega'} = \frac{G_F^2 V_{ud}^2}{2\pi^2} E'^2 \left[2W_{1,\alpha} \sin^2\frac{\theta}{2} + W_{2,\alpha} \cos^2\frac{\theta}{2} \pm W_{3,\alpha} \frac{E+E'}{m_N} \sin^2\frac{\theta}{2} \right] , \tag{3.1}$$

with the label $\alpha = \mathrm{CC}\nu$ or $\mathrm{CC}\bar{\nu}$; Ω' is the solid angle of l' in the laboratory frame; V_{ud} is the CKM matrix element; the sign in front of $W_{3,\alpha}$ is taken to be $+$ $(-)$ for ν $(\bar{\nu})$ induced reactions. The structure functions, $W_{i,\alpha}$ $(i = 1, 2, 3)$, are Lorentz-invariant functions of two independent variables, (Q^2, W), where W is the total energy of X at its rest frame. In the forward limit, $\theta \to 0$, only the W_2 term survives. The structure function $W_{2,\alpha}$ is expressed in terms of matrix elements of the weak current between the initial nucleon N and the final state X, $\langle X | J^\mu_\alpha | N \rangle$, as

$$W_{2,\alpha} = \frac{Q^2}{\vec{q}^2} \sum \left[\frac{1}{2} \left(|\langle X | J^x_\alpha | N \rangle|^2 + |\langle X | J^y_\alpha | N \rangle|^2 \right) + \frac{Q^2}{\vec{q}_c^2} \left| \langle X | \left(J^0_\alpha + \frac{\omega_c}{Q^2} q \cdot J_\alpha \right) | N \rangle \right|^2 \right] , \tag{3.2}$$

where the summation symbol indicates all possible final states X, integration over momentum states of X, the average of initial nucleon spin state, and some kinematical factors including the phase-space factor. In the forward limit where $Q^2 = 0$, what survives in Eq. (3.2) is only the last term that contains the divergence of the current. The weak current consists of the vector (V^μ) and axial (A^μ) currents. Because of the vector current conservation $\langle X | q \cdot V | N \rangle = 0$ in the isospin limit, the

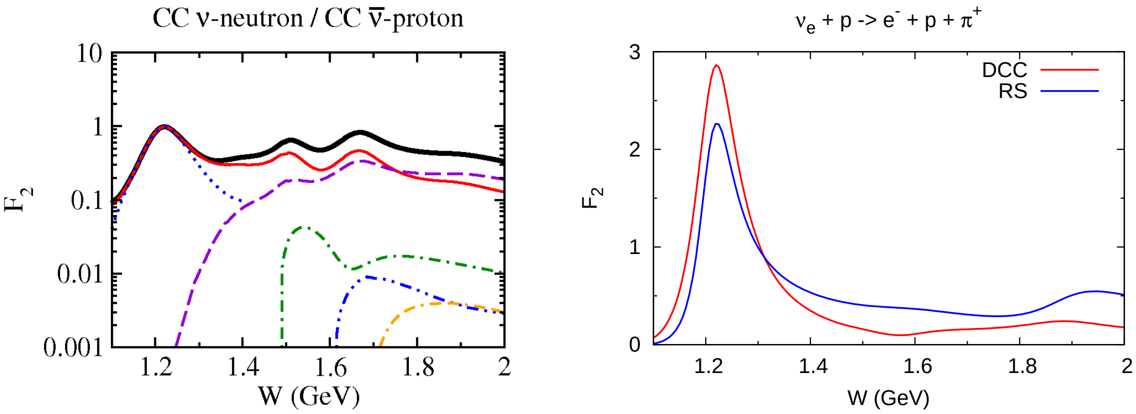

Figure 2: (Left) The structure function $F_2(Q^2=0)$ for the neutrino-induced meson productions from the DCC model [4]. The solid (red), dashed (purple), dash-dotted (green), two-dotted dash (blue), and two-dash dotted (orange) curves are for the πN, $\pi\pi N$, ηN, $K\Lambda$ and $K\Sigma$ reactions, respectively. The sum of them is given by the thick solid (black) curve. The SL model [1] is shown by the dotted (blue) curve. (Right) Comparison of $F_2(Q^2=0)$ between the DCC model and Rein-Sehgal (RS) model.

divergence of the axial current remains. According to Refs. [6, 7, 8], we can define the pion field with the divergence of the axial currents as

$$\langle X(p')|q\cdot A^a|N(p)\rangle = f_\pi m_\pi^2 \langle X(p')|\hat{\pi}^a|N(p)\rangle, \tag{3.3}$$

where f_π (m_π) is the pion decay constant (pion mass), and $\hat{\pi}^a$ is the normalized interpolating pion field with the isospin state a. Furthermore, the matrix element $\langle X(p')|\hat{\pi}^a|N(p)\rangle$ at $Q^2=0$ can be expressed as

$$\langle X(p')|\hat{\pi}^a|N(p)\rangle = \frac{\sqrt{2\omega_c}}{m_\pi^2}\mathscr{T}_{\pi^a N\to X}(0). \tag{3.4}$$

Here, $\mathscr{T}_{\pi^a N\to X}(q^2)$ is the T-matrix element of the $\pi^a(q)+N(p)\to X(p')$ reaction in the πN center-of-mass frame, and the incoming pion is off-mass-shell $q^2=0\neq m_\pi^2$. Using Eqs. (3.3), (3.4) and $\mathscr{T}_{\pi^a N\to X}(q^2=0)\sim\mathscr{T}_{\pi^a N\to X}(q^2=m_\pi^2)$, the structure function $W_{2,\alpha}$ is related to the total cross section for $\pi N\to X$. Now we can evaluate neutrino-induced forward meson production cross sections at $\theta=0$ using the $\pi N\to X$ total cross sections of the DCC model. In the next section, we show the dimensionless structure function F_2 defined by $F_2=\omega W_2$.

4. Result

We show the structure functions F_2 for the neutrino-induced meson productions off the nucleon in Fig. 2 (left). The figure shows F_2 for the CC neutrino-neutron or antineutrino-proton scattering where both $I=1/2$ and $3/2$ states give contributions. While the πN production is the dominant process up to $W=1.5$ GeV, above that energy, the $\pi\pi N$ production becomes comparable to πN, showing the importance of the $\pi\pi N$ channel in the resonance region above $\Delta(1232)$. Also, we observe that the πN and $\pi\pi N$ spectra above the Δ have rather bumpy structure, reflecting contributions from many nucleon resonances. This structure cannot be simulated by a naive extrapolation of the DIS model to the resonance region, as has been often done in previous analyses of neutrino oscillation experiments. Other meson productions, ηN, $K\Lambda$, and $K\Sigma$ reactions have much smaller contribution, about $[O(10^{-1})$-$O(10^{-2})]$ of πN and $\pi\pi N$ contributions. We remark that this is the first prediction of the neutrino-induced $\pi\pi N$, ηN, KY production rates based on a model that has been extensively tested by data.

It is also interesting to compare our result with F_2 from the Rein-Sehgal (RS) model [9, 10] that has been extensively used in many Monte Carlo simulators for analyzing neutrino experiments. Such a comparison is shown in Fig. 2 (right). We can see that the RS model underestimates the $\Delta(1232)$ peak by $\sim 20\%$. On the other hand, in higher energies, the RS model significantly overestimates F_2. Our result is based on the DCC model tested by lots of data in the resonance region while the RS model has not but based on a quark model. Considering that, the current Monte Carlo simulators using the RS model should be improved. In this work, the comparison with the RS model is done only in the forward limit. More comparison for non-forward kinematics, as well as full description of neutrino reactions needs development of a dynamical axial current model. Such a development is currently underway.

Acknowledgments

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