## Bottomonia and charmonia from B-factories

## Pavel Krokovny*

Budker Institute of Nuclear Physics and Novosibirsk State University E-mail: krokovny@inp.nsk.su

We report the first observation of the three-body $\Upsilon(5 S) \rightarrow \Upsilon(1,2 S) \pi^{0} \pi^{0}$ decays. Strong evidence for the $Z_{b}^{0}(10610)$ with $4.9 \sigma$ significance is found in a Dalitz plot analysis of the $\Upsilon(5 S) \rightarrow$ $\Upsilon(2 S) \pi^{0} \pi^{0}$ decays. First results on the analysis of the three-body $\Upsilon(5 S) \rightarrow\left[B \bar{B}^{*}+\text { c.c. }\right]^{ \pm} \pi^{\mp}$ and $\Upsilon(5 S) \rightarrow\left[B^{*} \bar{B}^{*}\right]^{ \pm} \pi^{\mp}$ including first observation of $Z_{b}^{ \pm}(10610) \rightarrow\left[B \bar{B}^{*}+\text { c.c. }\right]^{ \pm}$and $Z_{b}^{ \pm}(10650) \rightarrow$ $\left[B^{*} \bar{B}^{*}\right]^{ \pm}$are also reported. The results are obtained with a $121.4 \mathrm{fb}^{-1}$ data sample collected with the Belle detector at the $\Upsilon(5 S)$ resonance at the KEKB asymmetric-energy $e^{+} e^{-}$collider.

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Figure 1: The $\pi^{0} \pi^{0}$ missing mass distribution for $\Upsilon(n S) \pi^{0} \pi^{0}$, (a) $\Upsilon(n S) \rightarrow \mu^{+} \mu^{-}$and (b) $\Upsilon(n S) \rightarrow e^{+} e^{-}$ candidates. The $M\left(\Upsilon(1 S) \pi^{+} \pi^{-}\right)$distribution for $\Upsilon(2 S) \rightarrow \Upsilon(1 S) \pi^{+} \pi^{-}$candidates is shown in (c). Histograms represent the data. The solid curves show the fit result while the dashed curves correspond to the background contributions.

## 1. Introduction

Two new charged bottomonium-like resonances, $Z_{b}(10610)$ and $Z_{b}(10650)$, have recently been observed by the Belle Collaboration in decays of $\Upsilon(10860)$ to five different final states: $\Upsilon(n S) \pi^{+} \pi^{-}, n=1,2,3$ and $h_{b}(m P) \pi^{+} \pi^{-}, m=1,2$ [1], $]$ ]. The analysis of the quark composition of the initial and final states allows to assert that these hadronic objects are the first unambiguous examples of states of an exotic nature: $Z_{b}$ should be comprised of (at least) four quarks. Several models have been proposed to describe the internal structure of these states. One suggests [3] that $Z_{b}(10610)$ and $Z_{b}(10650)$ states might be a loosely bound $B \bar{B}^{*}$ and $B^{*} \bar{B}^{*}$ systems, respectively. The proximity of the $Z_{b}(10610)$ and $Z_{b}(10650)$ masses to those of the sum of the $B$ and $B^{*}$ mesons and the sum of the two $B^{*}$ mesons, respectively, supports this hypothesis. In this case, it would be natural to expect that the $Z_{b}(10610)$ and $Z_{b}(10650)$ states decay respectively to $B \bar{B}^{*}$ and $B^{*} \bar{B}^{*}$ final states with substantial rates. In this analysis we use $121.4 \mathrm{fb}^{-1}$ of data accumulated by the Belle detector at a center-of-mass (c.m.) energy near the $\Upsilon(10860$ ) to study three-body $\Upsilon(10860) \rightarrow\left[B^{(*)} \bar{B}^{(*)}\right]^{ \pm} \pi^{\mp}$ decays and to search for $\Upsilon(10860) \rightarrow Z_{b}^{ \pm} \pi^{\mp} \rightarrow\left[B^{(*)} \bar{B}^{*}\right]^{ \pm} \pi^{\mp}$ decays. We also search for a neutral partner of $Z_{b}$ states in the resonant substructure of the $\Upsilon(5 S) \rightarrow \Upsilon(n S) \pi^{0} \pi^{0}$ decays.

## 2. $\Upsilon(5 S) \rightarrow \Upsilon(n S) \pi^{0} \pi^{0}$ decays

We reconstruct $\Upsilon(n S)$ candidates from pairs of leptons ( $e^{+} e^{-}$and $\mu^{+} \mu^{-}$). An additional decay channel is used for the $\Upsilon(2 S): \Upsilon(2 S) \rightarrow \Upsilon(1 S)\left[l^{+} l^{-}\right] \pi^{+} \pi^{-}$. Muon and electron candidates are required to be positively identified. Candidate $\pi^{0}$ mesons are selected from pairs of photons with an invariant mass within $15 \mathrm{MeV} / \mathrm{c}^{2}$ of the nominal $\pi^{0}$ mass. $\Upsilon(5 S) \rightarrow \Upsilon(n S)\left[l^{+} l^{-}\right] \pi^{0} \pi^{0}$ candidates are identified via the missing mass recoiling against the $\pi^{0} \pi^{0}$ system, $M_{\text {miss }}\left(\pi^{0} \pi^{0}\right)$. More details can be found in Ref. [4]. Figure 1] shows the extraction of the $\Upsilon(n S)$ signal yield. Results are summarized in Table 1 Branching fraction is calculated as $\mathscr{B}=\frac{N_{\text {sig }}}{\varepsilon \mathscr{L} \sigma\left(e^{+} e^{-} \rightarrow \mathrm{r}(5 S)\right)}$, where $N_{\text {sig }}$ is number of signal events, $\varepsilon$ is reconstruction efficiency, $\mathscr{L}$ is integrated luminosity. Weighted averages are found to be $\mathscr{B}\left(\Upsilon(5 S) \rightarrow \Upsilon(1 S) \pi^{0} \pi^{0}\right)=(2.25 \pm 0.11 \pm 0.20) \times 10^{-3}$ and $\mathscr{B}\left(\Upsilon(5 S) \rightarrow \Upsilon(2 S) \pi^{0} \pi^{0}\right)=(3.66 \pm 0.22 \pm 0.48) \times 10^{-3}$.

Table 1: Signal yield, MC efficiency, measured branching fraction, number of selected events and purity.

| Final state | Signal yield | $\varepsilon, \%$ | $\mathscr{B}, 10^{-3}$ | Events | Purity |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\Upsilon(1 S) \rightarrow \mu^{+} \mu^{-}$ | $261 \pm 15$ | 11.2 | $2.28 \pm 0.13$ | 247 | 0.95 |
| $\Upsilon(1 S) \rightarrow e^{+} e^{-}$ | $123 \pm 13$ | 5.61 | $2.15 \pm 0.23$ | 140 | 0.78 |
| $\Upsilon(2 S) \rightarrow \mu^{+} \mu^{-}$ | $241 \pm 18$ | 8.04 | $3.77 \pm 0.28$ | 253 | 0.87 |
| $\Upsilon(2 S) \rightarrow e^{+} e^{-}$ | $108 \pm 13$ | 3.58 | $3.84 \pm 0.46$ | 151 | 0.66 |
| $\Upsilon(2 S) \rightarrow \Upsilon(1 S) \pi^{+} \pi^{-}$ | $24 \pm 5$ | 2.27 | $2.85 \pm 0.60$ | 28 | 0.86 |

The amplitude analysis of the three-body $\Upsilon(5 S) \rightarrow \Upsilon(n S) \pi^{0} \pi^{0}$ decays utilizes an unbinned maximum likelihood fit. We parameterize the three-body decay amplitude as a sum of quasi-twobody amplitudes: $M\left(s_{1}, s_{2}\right)=A_{Z 1}+A_{Z 2}+A_{f_{0}}+A_{f_{2}}+A_{\mathrm{nr}}$, where $A_{Z 1}$ and $A_{Z 2}$ are amplitudes for contributions from the $Z_{b}^{0}(10610)$ and $Z_{b}^{0}(10650)$, respectively; the amplitudes $A_{f_{0}}, A_{f_{2}}$ and $A_{\mathrm{nr}}$ are the contributions from the $\pi^{0} \pi^{0}$ system in an $f_{0}(980), f_{2}(1275)$ and a non-resonant state, respectively. The masses and widths of $Z_{b}$ resonances are fixed at the values obtained from the $\Upsilon(n S) \pi^{+} \pi^{-}$analysis: $M\left(Z_{1}\right)=10607.2 \mathrm{MeV} / \mathrm{c}^{2}, \Gamma\left(Z_{1}\right)=18.4 \mathrm{MeV} / \mathrm{c}, M\left(Z_{2}\right)=10652.2 \mathrm{MeV} / \mathrm{c}^{2}$, $\Gamma\left(Z_{2}\right)=11.5 \mathrm{MeV} / \mathrm{c}$ [?]. We use a Flatté function for the $f_{0}(980)$ and a Breit-Wigner function for the $f_{2}(1275)$. The non-resonant amplitude $A_{\mathrm{nr}}$ is parameterized as $A_{\mathrm{nr}}=A_{\mathrm{nr}}^{1} e^{i \phi_{\mathrm{nr}}^{1}}+A_{\mathrm{nr}}^{2} e^{i \phi_{\mathrm{nr}}^{2}} S_{3}$. As the fit is sensitive only to the relative amplitudes and phases between decay modes, we fix $A_{\mathrm{nr}}^{1}=10.0$ and $\phi_{\mathrm{nr}}^{1}=0.0$. The logarithmic likelihood function is defined as $\mathscr{L}=-2 \sum \log \left\{\varepsilon\left(s_{1}, s_{2}\right) f_{\mathrm{sig}} S\left(s_{1}, s_{2}\right)+\right.$ $\left.\left(1-f_{\text {sig }}\right) B\left(s_{1}, s_{2}\right)\right\}$, where $S\left(s_{1}, s_{2}\right)$ denotes $\left|M\left(s_{1}, s_{2}\right)\right|^{2}$ convoluted with the detector resolution function, $\varepsilon\left(s_{1}, s_{2}\right)$ describes variation of the reconstruction efficiency over the Dalitz plot and $f_{\text {sig }}$ is the fraction of signal events in the data sample. The fraction $f_{\text {sig }}$ is determined separately for each $\Upsilon(n S)$ decay mode (see Table 11). The function $B\left(s_{1}, s_{2}\right)$ describes the distribution of background events over the phase space. Both $\varepsilon\left(s_{1}, s_{2}\right) \cdot S\left(s_{1}, s_{2}\right)$ and $B\left(s_{1}, s_{2}\right)$ are normalized to unity. Results of the fits are shown in Fig. $\because$ as one-dimensional projections that look similar to the corresponding distributions for the $\Upsilon(n S) \pi^{+} \pi^{-}$decays [?]. A $Z_{b}^{0}$ signal is most clearly seen in $M\left(\Upsilon \pi^{0}\right)_{\max }$. The values and errors of amplitudes and phases obtained from the fit are presented in [ 7 ]. The statistical significance of the $Z_{b}^{0}(10610)$ signal in the $\Upsilon(2 S) \pi^{0} \pi^{0}$ sample is $5.3 \sigma$. The signal for the $Z_{b}^{0}(10610)$ is not significant in the fit to the $\Upsilon(1 S) \pi^{0} \pi^{0}$ events due to the smaller relative branching fraction. The signal of the $Z_{b}^{0}(10650)$ is not significant in either $\Upsilon(1) \pi^{0} \pi^{0}$ or $\Upsilon(2 S) \pi^{0} \pi^{0}$ datasets.

We study possible uncertainties due to parameterization of the background PDF , variation of signal efficiency over the Dalitz plot and detector resolution function. The model uncertainty is estimated using various description of $S$-wave contribution. The significance of the $Z_{b}^{0}(10610)$ signal exceeds $4.9 \sigma$ in all cases. We use this value as the final value for the $Z_{b}^{0}(10610)$ significance.

## 3. $\Upsilon(10860) \rightarrow B^{(*)} \bar{B}^{*} \pi$ Decays

$B$ decays are reconstructed in the following channels: $B^{+} \rightarrow J / \psi K^{+}, B^{+} \rightarrow \overline{D^{0}} \pi^{+}, B^{0} \rightarrow$ $J / \psi K^{* 0}, B^{0} \rightarrow D^{(*)-} \pi^{+}$. We identify $B$ candidates by their invariant mass $M(B)$ and momentum $P(B)$ in the c.m. We require $M(B)$ to be within 30 to $40 \mathrm{MeV} / c^{2}$ (depending on the $B$ decay mode) of the nominal $B$ mass. Reconstructed $B^{+}$or $B^{0}$ candidates are then combined with a $\pi^{-}$candidate


Figure 2: Comparison of the fit results (open histograms) with experimental data (points with error bars) for the (a,b) $\Upsilon(1 S) \pi^{0} \pi^{0}$ and (c) $\Upsilon(2 S) \pi^{0} \pi^{0}$ events in the signal region. Red and blue open histograms show the fit with and without $Z_{b}^{0}$ 's, respectively. Hatched histograms show the background components.


Figure 3: (a) $M_{r}(B \pi)$ distributions for selected $B$ candidates in data. Hatched histogram shows distribution for events in the $M(B)$ sidebands. (b) $M_{r}(\pi)$ distribution for right-sign $B \pi$ combinations for $\Upsilon(10860) \rightarrow$ $B B^{*} \pi$ and (c) $\Upsilon(10860) \rightarrow B^{*} B^{*} \pi$ candidate events. Points with error bars are data, the solid line is the result of the fit with the nominal model, the dashed line - fit to pure non-resonant amplitude, the dotted line - fit to a single $Z_{b}$ state plus a non-resonant amplitude, and the dash-dotted - two $Z_{b}$ states and a non-resonant amplitude. The hatched histogram represents background component.
and a recoil mass to the $B \pi$ combination, $M_{r}(B \pi)$, is calculated as $M_{r}(B \pi)=\sqrt{E_{\mathrm{cms}}^{2}-P_{B \pi}^{2}}$, where $E_{\mathrm{cms}}$ is the c.m. energy and $P_{B \pi}$ is the measured three-momentum of the $B \pi$ combination. More details can be found in Ref. [5]. The $M_{r}(B \pi)+M(B)-M_{B}$ distribution for the data is shown in Fig. B(a), where clear peaks are visible in the $B B^{*} \pi$ and $B^{*} B^{*} \pi$ signal regions. The fit to this distribution gives $N_{B B \pi}=1 \pm 14, N_{B B^{*} \pi}=184 \pm 19$ and $N_{B^{*} B^{*} \pi}=82 \pm 11$ signal events. The statistical significance of the observed $B B^{*} \pi$ and $B^{*} B^{*} \pi$ signal is $9.3 \sigma$ and $5.7 \sigma$, respectively. For the subsequent analysis of the internal structures of the three-body decays, we require $\mid\left(M_{r}(B)+\right.$ $\left.M(B)-M_{B}\right)-M_{B^{*}} \mid<0.015 \mathrm{GeV} / c^{2}$ to select $\Upsilon(10860) \rightarrow B B^{*} \pi$ events and $\mid\left(M_{r}(B)+M(B)-\right.$ $\left.M_{B}\right)-\left(M_{B^{*}}+E_{\gamma}\right) \mid<0.015 \mathrm{GeV} / c^{2}$, where $E_{\gamma}=0.049 \mathrm{GeV}$, to select $\Upsilon(10860) \rightarrow B^{*} B^{*} \pi$ events. For selected $B^{(*)} B^{(*)} \pi$ candidate events, we calculate the mass recoiling against the charged pion: $M_{r}(\pi)=\sqrt{E_{\mathrm{cms}}^{2}-P_{\pi}^{2}}$, where $P_{B \pi}$ is the measured three-momentum of the charged pion.

The $M_{r}(\pi)$ distributions for right-sign $B \pi$ combinations in the $B B^{*} \pi$ and $B^{*} B^{*} \pi$ signal regions are shown in Fig. 3. Excesses of signal events over the expected background levels at lower mass edges of the $M_{r}(\pi)$ spectra are clearly visible for both final states. The distribution of signal $\Upsilon(10860) \rightarrow B B^{*} \pi$ events is parameterized with the following model $S_{B B^{*} \pi}(m)=\left(A_{Z_{b}(10610)}+\right.$ $\left.A_{N R}\right) \times E_{B B^{*} \pi}(m)$, where $A_{N R}$ is the non-resonant amplitude parameterized as a complex constant

Table 2: List of branching fractions for the $Z_{b}^{+}(10610)$ and $Z_{b}^{+}$(10650) decays.

| $\mathscr{B}, \%$ | $\Upsilon(1 S) \pi^{+}$ | $\Upsilon(2 S) \pi^{+}$ | $\Upsilon(3 S) \pi^{+}$ | $h_{b}(1 P) \pi^{+}$ | $h_{b}(2 P) \pi^{+}$ | $B^{(*)} \bar{B}^{*}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $Z_{b}(10610)$ | $0.32 \pm 0.09$ | $4.38 \pm 1.21$ | $2.15 \pm 0.56$ | $2.81 \pm 1.10$ | $4.34 \pm 2.07$ | $86.0 \pm 3.6$ |
| $Z_{b}(10650)$ | $0.24 \pm 0.07$ | $2.40 \pm 0.63$ | $1.64 \pm 0.40$ | $7.43 \pm 2.70$ | $14.8 \pm 6.22$ | $73.4 \pm 7.0$ |

and the $Z_{b}(10610)$ amplitude is a Breit-Wigner function. As a variation of this nominal model, we also add a second Breit-Wigner amplitude to account for possible $Z_{b}(10650) \rightarrow B B^{*} \pi$ decay. We also fit the data with only the $Z_{b}(10610)$ channel included in the decay amplitude. The results of these fits are shown in Fig. 3 (b). Two models give about equally good description of the data: nominal model and a model with additional non-resonant amplitude. However, we select the former one as our nominal model since adding a non-resonant amplitude does not improve the fit quality that much. The worst fit to the data is provided by a model with just a non-resonant amplitude. From this analysis, we find that the significance of the $Z_{b}(10610) \rightarrow B B^{*}$ signal is exceeding the $8 \sigma$ level.

As the nominal model for the $\Upsilon(10860) \rightarrow B^{*} B^{*} \pi$ decay, we use the following parameterization: $S_{B^{*} B^{*} \pi}(m)=\left(A_{Z_{b}(10650)}+A_{N R}\right) \mathrm{E}_{B^{*} B^{*} \pi}(m)$. We also fit the data without a non-resonant component and with a non-resonant amplitude alone. Results of the fits are shown in Fig. 3(c); numerical values are given in [5]. The best description of the $B^{*} B^{*} \pi$ data is achieved in a model with only the $Z_{b}(10650)$ amplitude included. The addition of a non-resonant amplitude does not provide any significant improvement of the fit quality. The fit with a non-resonant amplitude alone gives a much worse likelihood value. From this analysis, we determine the significance of the $Z_{b}(10650) \rightarrow B^{*} B^{*}$ signal to be $6.8 \sigma$. In all fits discussed above, the masses and widths of the $Z_{b}$ states were fixed at the values obtained from the analysis of the $\Upsilon(n S) \pi^{+} \pi^{-}$and $h_{b}(m P) \pi^{+} \pi^{-}-$ final states [?].

## 4. Conclusion

We report the first observation of three-body $\Upsilon(5 S) \rightarrow \Upsilon(1,2 S) \pi^{0} \pi^{0}$ decays. The measured branching fractions are $\mathscr{B}\left(\Upsilon(5 S) \rightarrow \Upsilon(1 S) \pi^{0} \pi^{0}\right)=(2.25 \pm 0.11 \pm 0.20) \times 10^{-3}$ and $\mathscr{B}(\Upsilon(5 S) \rightarrow$ $\left.\Upsilon(2 S) \pi^{0} \pi^{0}\right)=(3.66 \pm 0.22 \pm 0.48) \times 10^{-3}$. Evidence for a $Z_{b}^{0}(10610) \rightarrow \Upsilon(2 S) \pi^{0}$ decay has been obtained from the amplitude analysis of the $\Upsilon(5 S) \rightarrow \Upsilon(2 S) \pi^{0} \pi^{0}$ decay. The statistical significance of the $Z_{b}^{0}(10610)$ signal is $4.9 \sigma$ including model and systematic uncertainties. Its measured mass, $M\left(Z_{b}^{0}(10610)\right)=10609_{-6}^{+8} \pm 6 \mathrm{MeV} / \mathrm{c}^{2}$, is consistent with that measured in the analysis of $\Upsilon(5 S) \rightarrow \Upsilon(n S) \pi^{+} \pi^{-}$decays. The $Z_{b}^{0}(10650)$ signal is not significant in either $\Upsilon(1 S) \pi^{0} \pi^{0}$ or $\Upsilon(2 S) \pi^{0} \pi^{0}$ final decays. We also report measurement of branching fractions for three-body decays: $\mathscr{B}\left(\Upsilon(10860) \rightarrow\left[B \bar{B}^{*}+\text { c.c. }\right]^{+} \pi^{-}\right)=(28.3 \pm 2.9 \pm 4.6) \times 10^{-3}$ and $\mathscr{B}\left(\Upsilon(10860) \rightarrow\left[B^{*} \bar{B}^{*}\right]^{+} \pi^{-}\right)=$ $(14.1 \pm 1.9 \pm 2.4) \times 10^{-3}$. For the $\Upsilon(10860) \rightarrow B \bar{B} \pi$ decay, we calculate a $90 \%$ confidence level upper limit of $\mathscr{B}\left(\Upsilon(10860) \rightarrow[B \bar{B}]^{+} \pi^{-}\right)<4.0 \times 10^{-3}$ (including systematic uncertainty). In addition, we report the ratio of the branching fractions $\frac{\mathscr{B}\left(Z_{b}(10610) \rightarrow B B^{*}\right)}{\sum_{n} \mathscr{B}\left(Z_{b}(10610) \rightarrow \mathrm{Y}(n S) \pi\right), h_{b}(m P) \pi}=6.2 \pm 0.7 \pm$ $1.3_{-1.8}^{+0.0}$ and $\frac{\mathscr{B}\left(Z_{b}(10650) \rightarrow B^{*} B^{*}\right)}{\sum_{n} \mathscr{B}\left(Z_{b}(10650) \rightarrow \mathrm{Y}(n S) \pi, h_{b}(m P) \pi\right)}=2.8 \pm 0.4 \pm 0.6_{-0.4}^{+0.0}$. We calculate the relative fractions for $Z_{b}$ decays assuming that are saturated by the already observed $\Upsilon(n S)(n=1,2,3), h_{b}(m P)$
$(m=1,2)$, and $B^{*} B^{(*)}$ channels. Combining results reported here with results on amplitude analysis from Ref. [h] one calculate relative fractions summarized in Table All presented results are preliminary.

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[^0]:    *Speaker.

