

# Jet Energy Loss and Mach Cones in pQCD vs. AdS/CFT

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**Barbara Betz**<sup>\*†</sup>

*Institut für Theoretische Physik, Goethe - Universität, 60438 Frankfurt, Germany*

*E-mail: betz@th.physik.uni-frankfurt.de*

**Jorge Noronha**<sup>‡</sup>

*Department of Physics, Columbia University, New York, 10027, USA*

*E-mail: noronha@phys.columbia.edu*

**Miklos Gyulassy**

*Department of Physics, Columbia University, New York, 10027, USA*

*E-mail: gyulassy@phys.columbia.edu*

**Giorgio Torrieri**

*Institut für Theoretische Physik, Goethe - Universität, 60438 Frankfurt, Germany*

*E-mail: torrieri@th.physik.uni-frankfurt.de*

We compare away-side hadron correlations with respect to tagged heavy quark jets computed within a weakly coupled pQCD and a strongly coupled AdS/CFT model. While both models feature similar far zone Mach and diffusion wakes, the far zone stress features are shown to be too weak to survive thermal broadening at hadron freeze-out. Observable away-side conical correlations are dominated by the jet-induced transverse flow in near zone “Neck” region, which differs significantly for both models. Unlike in AdS/CFT, the induced transverse flow in the Neck zone is too weak in pQCD to produce conical correlations after Cooper-Frye freeze-out. The observation of conical correlations violating Mach’s law would favor the strongly-coupled AdS/CFT string drag dynamics, while their absence would favor weakly-coupled pQCD-based hydrodynamics.

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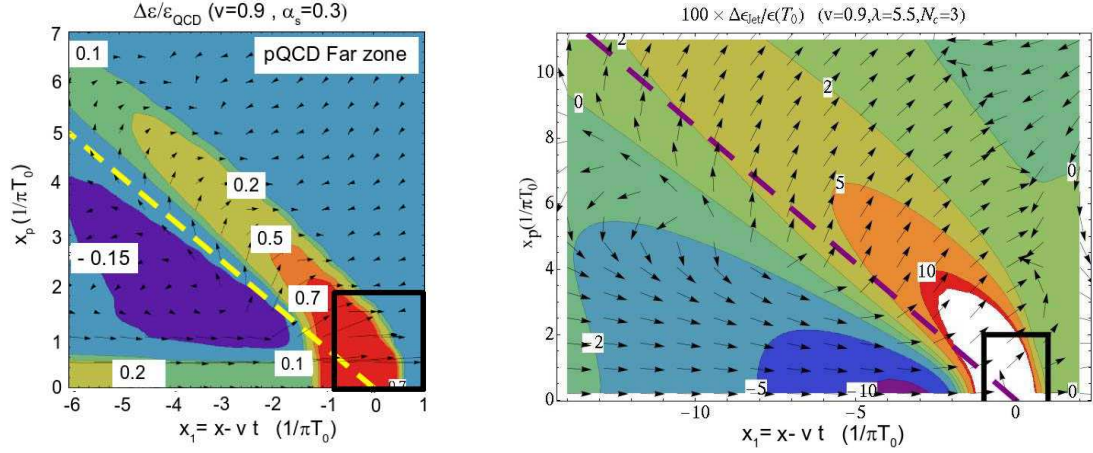
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<sup>\*</sup>Speaker.

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**Figure 1:** The fractional energy density perturbation (in the lab frame) due to a heavy quark with  $v = 0.9$  in a pQCD plasma of temperature  $T_0 = 200$  MeV, calculated using (3+1)d hydrodynamics with the pQCD source of Neufeld (left panel) and AdS/CFT (right panel). The ideal Mach cone for a point source is represented by the dashed lines, the box indicates the Neck region.

## 1. Introduction

Energetic back-to-back jets produced in the early stages of a heavy ion collision traverse the sQGP and deposit energy and momentum along their path in a way that depends on the non-equilibrium details of the physics of the field-plasma coupling. In the case when one of the jets is produced near the surface (the trigger jet), the other supersonic away-side jet moves through the plasma and generates in the far zone a Mach-like disturbance as seen in Fig. 1. Recent interest in Mach-like di-jet correlations [1] is due to suggestions [2] that a measurement of the dependence of the cone angle on the supersonic jet velocity  $v$  could provide via Mach's law ( $\cos \phi_M = c_s/v$ ) a constraint on the average speed of sound in the strongly coupled Quark-Gluon Plasma (sQGP) [3] created at the Relativistic Heavy Ion Collider (RHIC). The observation of strong elliptic flow in non-central Au+Au collisions consistent with fluid dynamical predictions suggest that a thermalized medium that evolves hydrodynamically is created in these collisions. Moreover, since the average momentum of particles emitted on the away-side approaches the value of the thermalized medium with decreasing impact parameter, the energy lost by the jet should quickly thermalize [4]. Thus, the disturbance caused by the jet may also be described hydrodynamically, which requires solving

$$\partial_\mu T^{\mu\nu} = S^\nu \quad (1.1)$$

to determine the time evolution of the medium that was disturbed by the moving jet. The source term that correctly depicts the interaction of the jet with the sQGP is unknown from first principles although recent calculations in pQCD and in AdS/CFT [5] have shed some light on this problem. Here, we summarize the striking difference between pQCD and AdS/CFT models by solving numerically the full nonlinear (3+1)d relativistic hydrodynamic equations using the SHASTA hydro code [6], supplemented with pQCD source derived in Refs. [7, 8] and comparing the results with those computed in [9], which used the  $\mathcal{N} = 4$  SYM AdS/CFT data computed by Gubser, Pufu,

and Yarom in Ref. [10] for the energy-momentum disturbances caused by the heavy-quark which was created at  $t \rightarrow -\infty$  and has been moving through the infinitely extended  $\mathcal{N} = 4$  SYM static background plasma since then. For the hydrodynamical results, the initial away-side heavy quark jet is assumed to start  $t = 0$  at  $x_1 = -4.5$  fm and the freeze-out is done (as for the AdS/CFT results) when the heavy quark reaches the origin of the coordinates at time  $t_f = 4.5/v$  fm. In the hydro calculations, we specialize to the ideal fluid case to minimize the dissipative broadening of any conical correlations. Moreover, we neglect here the near-side associated correlations and use  $\alpha_s = 1/\pi$  as well as  $x_{pmax} = 1/m_D$  as an infrared cutoff while the minimum lattice spacing naturally provided an ultraviolet cutoff. The background temperature is set to  $T_0 = 0.2$  GeV.

Given the large theoretical systematic uncertainty inherent in any phenomenological model of hadronization, we consider here two simple limits for modeling the fluid decoupling and freeze-out. In one often used limit, computational fluid cells are frozen out via the Cooper–Frye (CF) method where the conversion of the fluid flow velocity field  $U^\mu(x)$ , associated (massless) momentum distribution  $P^\mu(X)$  and temperature profile  $T(X)$  into free particles (at mid-rapidity) is achieved instantaneously at a critical surface  $d\Sigma_\mu$  via

$$\frac{dN}{p_T dp_T dy d\phi} \Big|_{y=0} = \int_\Sigma d\Sigma_\mu P^\mu [f_0(U^\mu, P^\mu, T) - f_{eq}], \quad (1.2)$$

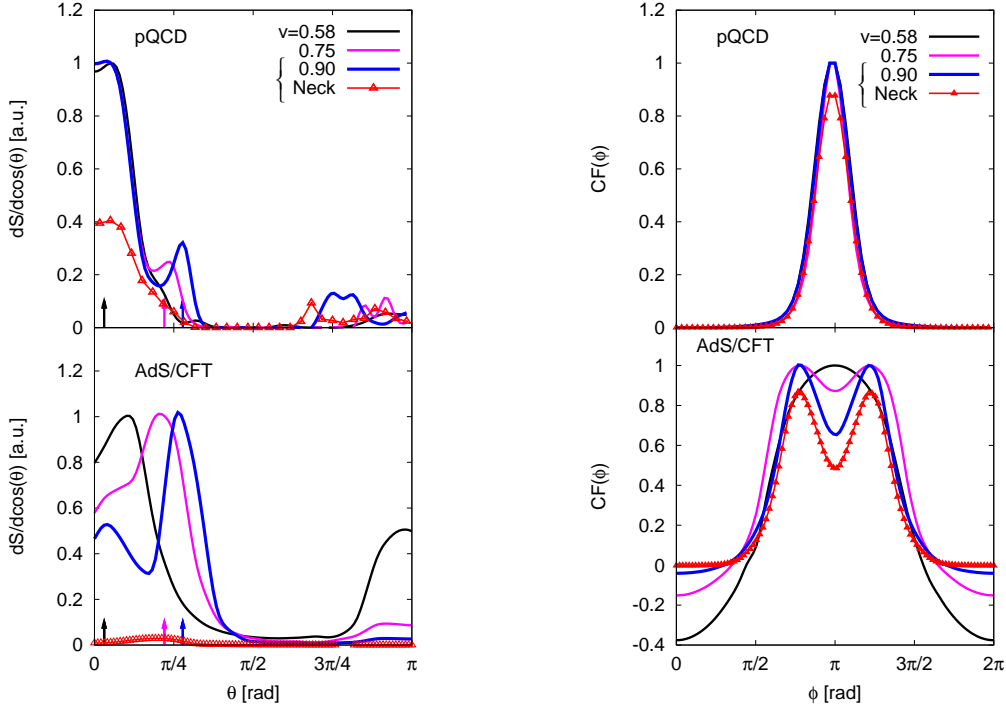
where  $p_T$  is the transverse momentum,  $\Sigma(X)$  is the isochronous freeze-out hypersurface, and  $f_0 = \exp(-U^\mu P_\mu / T(X))$  is a local Boltzmann equilibrium distribution. As an independent calorimetric-like observable of collective flow we also investigate the bulk momentum weighted polar angle distribution (in the laboratory frame)

$$\frac{dS}{d\cos\theta} = \sum_{cells} |\vec{\mathcal{P}}_c| \delta(\cos\theta - \cos\theta_c) = \int d^3\mathbf{x} |\mathbf{M}(X)| \delta\left(\cos\theta - \frac{M_x(X)}{|\mathbf{M}(X)|}\right) \Big|_{t_f} \quad (1.3)$$

where  $\theta = 0$  corresponds to the jet direction and  $\theta \in [0, \pi]$ . This quantity measures the angular distribution of fluid momentum at freeze-out time,  $t_f$ , in each fluid cell [8]. The strong assumption in this decoupling scheme is that the frozen cells do not break up (unlike in the CF case) but preserve their momentum  $\mathcal{P}_c^i = d^3\mathbf{x} T^{0i}(\mathbf{x}, t_f)$  to the detector. Here  $\theta$  is the polar angle with respect to the away-side heavy quark jet.

## 2. Comparing pQCD and AdS/CFT

The results for the normalized bulk flow according to Eq. (1.3) in pQCD are shown in the upper left panel in Fig. 2. For all velocities studied here, the pQCD bulk energy flow distribution has a large forward moving component in the direction of the jet. In the far zone, this forward moving energy flow corresponds to the diffusion wake. The red curve with triangles in the upper panel in Fig. 2 shows the yield solely from the Neck region for  $v = 0.9$ , a novel nonequilibrium near zone featured by the AdS/CFT string drag solution where especially strong transverse flow relative to the jet axis appears (cf. box region in Fig. 1). The relatively small transverse energy flow in the Neck region is evident on the left panel of see Fig. 1 in contrast to the much larger transverse flow predicted via AdS in that near zone (right panel of Fig. 1). The Mach cone emphasized in



**Figure 2:** (Color online) The (normalized) momentum weighted bulk flow angular distribution (left panel) and Cooper-Frye freezeout (right panel) for a jet with  $v = 0.58$  (black),  $v = 0.75$  (magenta), and  $v = 0.90$  (blue) comparing a pQCD and AdS/CFT string drag model. The red line with triangles represents the Neck contribution for a jet with  $v = 0.9$  and the arrows indicate the location of the ideal Mach-cone for  $c_s = 1/\sqrt{3}$ . The negative yield in the lower right panel is due to the presence of the vortices discussed in the text.

Ref. [7] is also clearly seen but its amplitude relative to the mostly forward diffusion plus Neck contribution is much smaller than in the AdS/CFT case. However, when  $v = 0.58$  the finite angle from the Mach cone is overwhelmed by the strong bow shock formed in front of the quark, which itself leads to small conical dip not at the ideal Mach angle (black arrow). The bottom left panel in Fig. 2 shows that in the AdS/CFT case more cells are pointing in a direction near the Mach cone angle than in the forward direction (diffusion wake) when  $v = 0.9$  and  $v = 0.75$ . The red line with triangles in the bottom panel of Fig. 2 shows that the relative magnitude of the contribution from the Neck region to the final bulk flow result in AdS/CFT is much smaller than in pQCD. However, note that small amplitude peak in the AdS/CFT Neck curve is located at a much larger angle than the corresponding peak in the pQCD Neck, as one would expect from the transverse flow shown Fig. 1. Moreover, for all velocities studied here, a peak occurs in direction of the trigger particle, representing the backward flow that is always present vortex-like structures created by the jet as discussed in detail in Ref. [11].

The right panel of Fig. 2 shows our normalized CF freeze-out results for the associated away-side azimuthal distribution for light hadrons with  $v = 0.58, 0.75, 0.9$  at mid-rapidity and  $p_T = 5\pi T_0 \sim 3.14$  GeV. The pQCD angular distribution displays only a sharp peak at  $\phi = \pi$  for all velocities. Note that the different peaks found in the bulk flow analysis of the pQCD data shown in the upper left panel in Fig. 2 do not survive CF freeze-out. We conclude that the strong forward

moving diffusion wake as well as the mostly forward bow shock Neck zone dominate the away-side peak and that the thermal broadened Mach correlations are too weak in  $pQCD$  to contribute to the final angular correlations. In the  $AdS/CFT$  case (see lower right panel of Fig. 2), a double peak structure can be seen for  $v = 0.9$  and  $v = 0.75$ . Note, however, that the peaks in the  $AdS/CFT$  correlation functions do not obey Mach's law. This is because these correlations come from the Neck region where there is a strong transversal non-Mach flow [9]. This is explicitly shown in the red curve with triangles that represents the Neck contribution for a jet with  $v = 0.9$  as in Fig. 2. For  $v = 0.58$ , the resulting flow is not strong enough to lead to non-trivial angular correlations.

### 3. Conclusions

In this paper, we compared the away-side angular hadron correlations associated with tagged heavy quark jets obtained in  $pQCD$  and  $AdS/CFT$ . In both cases the true Mach wakes are not observable after the standard CF method. Mach-like peaks are only observable in the sudden shattering freeze-out scenario described in Eqn. (1.3). Moreover, the Neck region gives the largest contribution to the total yield in CF freeze-out while its contribution in the other extreme case involving the bulk flow hadronization is not as relevant. We propose that the measurement of the jet velocity dependence of the associated away-side correlations with identified heavy quark triggers at RHIC and LHC will provide important constraints on possible on the jet-medium coupling dynamics.

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